CSE 5525 Artificial Intelligence II Homework #2: Markov Decision Process Wei Xu, Ohio State University

Your Name: _____ OSU ID: _____

1 Markov Decision Processes

Questions:

1) Write out the equations to be used to compute Q_i^* from R, T, V_{i-1}^*, γ and to compute V_i^* from R, T, Q_i^*, γ .

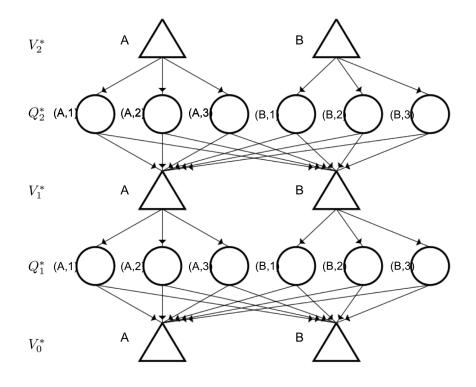
 $Q_i^*(s,a) =$

 $V_i^*(s) =$

2) Consider the MDP with transition model and reward function as given in the table below. Assume the discount factor $\gamma = 1$, i.e., no discounting. Fill in the values for $V_0^*, V_1^*, V_2^*, Q_1^*, Q_2^*$ in the graph below.

| s | a | s' | T(s,a,s') | R(s,a,s') |
|---|---|----|-----------|-----------|
| Α | 1 | А | 0 | 0 |
| Α | 1 | В | 1 | 0 |
| Α | 2 | А | 1 | 1 |
| Α | 2 | В | 0 | 0 |
| Α | 3 | А | 0.5 | 0 |
| А | 3 | В | 0.5 | 0 |

| s | a | \mathbf{s}' | T(s,a,s') | R(s,a,s') |
|---|---|---------------|-----------|-----------|
| В | 1 | A | 0.5 | 10 |
| В | 1 | В | 0.5 | 0 |
| В | 2 | А | 1 | 0 |
| В | 2 | В | 0 | 0 |
| В | 3 | А | 0.5 | 2 |
| В | 3 | В | 0.5 | 4 |



3) Let $\pi_i^*(s)$ be the optimal action in state s with i time steps to go. Fill in the following tables:

(s)

| s | $\pi_1^*(s)$ | s | π_2^* |
|---|--------------|---|-----------|
| A | | A | |
| B | | В | |