Unpacking DPO and PPO: Disentangling Best Practices for Learning from Preference Feedback

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RLHF

Step1

Collect demonstration data. and train a supervised policy.

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SFT

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Step 2

Collect comparison data, and train a reward model.

A prompt and several model outputs are sampled.

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Explain the moon

landing to a 6 year old

 $0.0.000$

 $\mathbf{0}$ > $\mathbf{0}$ > $\mathbf{0}$ = $\mathbf{0}$

A labeler ranks the outputs from best to worst.

This data is used to train our reward model.

Step 3

Optimize a policy against the reward model using reinforcement learning.

A new prompt is sampled from the dataset.

The policy generates an output.

The reward model calculates a reward for the output.

The reward is used to update the policy using PPO.

Training language models to follow instructions with human feedback

RLHF

Limitations?

- 1. Complex: involves training multiple LMs
- 2. Significant computational costs: need to sample from LM policy in the loop of training
- 3. Hard to implement: many hyper-parameters

Training language models to follow instructions with human feedback

PPO -> DPO

Intuition?

Directly optimize a language model to align to human preferences, without explicit reward modeling or reinforcement learning

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DPO derivation

Goal: implicitly optimizes the same objective as existing RLHF algorithms

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$$
\sum\{\sum_{\text{DPO}(\pi_{\theta};\,\pi_{\text{ref}})=-\mathbb{E}_{(x,y_w,y_l)\sim\mathcal{D}}\left[\log\sigma\left(\beta\log\frac{\pi_{\theta}(y_w\mid x)}{\pi_{\text{ref}}(y_w\mid x)}-\beta\log\frac{\pi_{\theta}(y_l\mid x)}{\pi_{\text{ref}}(y_l\mid x)}\right)\right]}
$$

RLHF objective:
$$
\max_{\pi_{\theta}} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi_{\theta}} [r(x, y)] - \beta KL [\pi_{\theta}(y|x), \pi_{\theta_{old}}(y|x)]
$$

\nget high reward
\n $\left\{\sum_{\pi_{\theta}} \min_{\pi_{\theta} \in \mathcal{D}} \mathbb{E}_{x \sim \mathcal{D}} \mathbb{E}_{y \sim \pi_{\theta}(\cdot|x)} \left[\log \frac{\pi_{\theta}(y|x)}{\pi_{\theta_{old}}(y|x) \exp (\frac{1}{\beta}r(x, y))} \right] \right\}$
\nDenote $Z(x) = \sum_{y} \pi_{\theta_{old}}(y|x) \exp (\frac{1}{\beta}r(x, y))$ and $\pi^*(y|x) = \frac{1}{Z(x)} \pi_{\theta_{old}}(y|x) \exp (\frac{1}{\beta}r(x, y))$
\n $(1) \pi^*(y|x) > 0 \quad (\forall y > 0); (2) \sum_{y} \pi^*(y|x) = 1$

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$$
\n
$$
\xrightarrow{\text{Stay close to reference model}}
$$
\n
$$
\xleftarrow{\text{KL function}}
$$
\n
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$$
\n
$$
\sum_{\pi_{\theta}} \min \mathbb{E}_{x \sim \mathcal{D}} \mathbb{E}_{y \sim \pi_{\theta}(\cdot|x)} \left[\log \frac{\pi_{\theta}(y|x)}{\pi_{\theta_{\text{old}}}(y|x) \exp \left(\frac{1}{\beta}r(x, y) \right)} \right]
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$$
\n
$$
\xleftarrow{\text{min } \mathbb{E}_{x \sim \mathcal{D}} \left[\text{KL} \left[\pi_{\theta}(y|x), \pi^*(y|x) \right] - \log Z(x) \right]}
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$$
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\xrightarrow{\text{set high reward}} \text{Sign reward} \left[\text{Stay close to reference model} \right]
$$
\n
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\n
$$
\xrightarrow{\text{optimal policy}} \pi_r(y|x) = \pi^*(y|x) = \frac{1}{Z(x)} \pi_{\theta_{\text{old}}}(y|x) \exp \left(\frac{1}{\beta}r(x, y) \right)
$$

Step 2: Write any reward function as function of optimal policy

Optimal policy:
$$
\pi_r(y|x) = \pi^*(y|x) = \frac{1}{Z(x)} \pi_{\theta_{old}}(y|x) \exp\left(\frac{1}{\beta}r(x, y)\right)
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\iff r(x, y) = \beta \log\left(\frac{\pi_r(y|x)}{\pi_{\theta_{old}}(y|x)}\right) + \beta \log\left(Z(x)\right)
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Ratio is positive if the optimal policy likes response **more** than reference model, negative if policy likes response **less** than reference model.

And the **more** the policy favors this response, the **higher** this ratio will be.

A loss function on reward functions:

Derived from the Bradley-Terry model of human preferences:

$$
\mathcal{L}_R(r, \mathcal{D}) = -\mathbb{E}_{(x, y_w, y_l) \sim \mathcal{D}}\left[\log \sigma(r(x, y_w) - r(x, y_l))\right]
$$

+

Transformation between reward functions and policies:

=

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$$

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$$

reward of preferred response

reward of dispreferred response

Explorations beyond DPO

PPO vs DPO

A Recipe for Learning from Preferences

Preference data

Preference Learning Algorithm

Reward model

Policy training prompt

Experiments: Benchmarks

Experiments: Preference Data

Table 1: Preference data: Performance of TÜLU 2 13B models trained on various preference datasets using DPO. Blue indicates improvements over the SFT baseline, orange degradations. Overall, synthetic data works best. DPO training improves truthfulness and instruction-following most, with limited to no improvements in factuality and reasoning.

Experiments: Preference Data

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Experiments: Preference Data

- Synthetic data with *per-aspect annotations* performs best (*i.e., UltraF.*)
- Per-aspect annotations (i.e., *UltraF, HelpSteer*): Datasets collected by first getting per-aspect annotations (e.g., helpfulness, harmlessness) then averaging

A Recipe for Learning from Preferences

Preference data

High-quality, synthetic preference dataset

Preference Learning Algorithm

Reward model

Policy training prompt

Experiments: Preference Learning Algorithm (DPO vs. PPO)

Figure 2: Left. The frontier of expected reward vs KL to the reference policy. DPO provides the highest expected reward for all KL values, demonstrating the quality of the optimization. Right. TL; DR summarization win rates vs. human-written summaries, using GPT-4 as evaluator. DPO exceeds PPO's best-case performance on summarization, while being more robust to changes in the sampling temperature.

R. Rafailov, A. Sharma, E. Mitchell, S. Ermon, C. D. Manning, and C. Finn. *Direct preference optimization: Your language model is secretly a reward model*

Experiments: Preference Learning Algorithm (DPO vs. PPO)

Table 2: DPO vs PPO: Average performance of 13B models trained using DPO and PPO across different datasets, along with the performance difference between DPO and PPO (Δ) . Blue indicates improvements over the SFT baseline, orange degradations. All datasets are downsampled to 60,908 examples (except ChatArena, which is made up of 20,465 responses). PPO outperforms DPO by an average of 0.7 points, where most improvements are in reasoning, coding, and chat capabilities.

A Recipe for Learning from Preferences

Experiments: Reward Models

- Scaling up the training data for RM:
	- **Mix RM**: Construct a data mixture of the top performing preference datasets (i.e., UltraFeedback, HelpSteer, Nectar, StackExchange, HH-RLHF, PRM800k)
	- **UltraF. RM**: Reward model trained only on UltraFeedback

● Scaling up the reward model size: 13B and 70B

Experiments: Reward Models

- Best-of-N:
	- Sample 16 responses for each evaluation task
	- Pick the top-scoring response according to the RM as the final output
- RewardBench: evaluating if the relative scores given by reward models match a test set of chosen-rejected pairs from diverse sources

Experiments: Reward Models

- It is difficult to translate improvements in reward models to the underlying policy
- Increasing scale and data improves reward models, but these only minimally impact the average downstream performance

A Recipe for Learning from Preferences

Experiments: Policy Training Prompts

- UltraF. Prompts: 20 random prompts from UltraFeedback
- Mined Math: math-related prompts from varied dataset
- GSM train: prompts from GASM train set

Figure 3: Policy training prompt math evaluation: Performance of models trained on 20K prompts from varying sources using PPO and evaluated on GSM. Training with larger RMs trained on more data benefits more from indomain prompts (i.e., prompts directly from the GSM train set), while weaker RMs struggle to generalize beyond their training prompts.

Experiments: Policy Training Prompts

- **Mixed:** mix math- and code-related prompts with UltraFeedback prompts, then downsample to the same size of UF
- **UF**: UltraFeedback

Table 4: Policy training prompt overall eval**uation:** Performance of PPO policy models trained with the given reward models on 60K prompts from either UltraFeedback or the remixed prompt set that adds additional unlabeled math and coding-related prompts. Using the remixed prompt set does not improve performance, either on specific evaluations (math, code) or in terms of overall performance.

A Recipe for Learning from Preferences

A Recipe for Learning from Preferences

Table 5: Putting together a recipe for preference-based learning: Performance of our bestperforming models along with popular open models based on Llama 2 13B. 'MP' refers to using the mixed prompt set described in §4. Using PPO with a large reward model performs best overall.

Summary

Figure 1: Performance improvements resulted by changing different components in the preference training of TÜLU. Left: Accuracy on GSM [9], for testing math capabilities. Right: Overall performance, aggregated over the 11 benchmarks described in §2.2.