

(many slides from Greg Durrett)

Neural Networks

Wei Xu

Linear Transformation (math review)

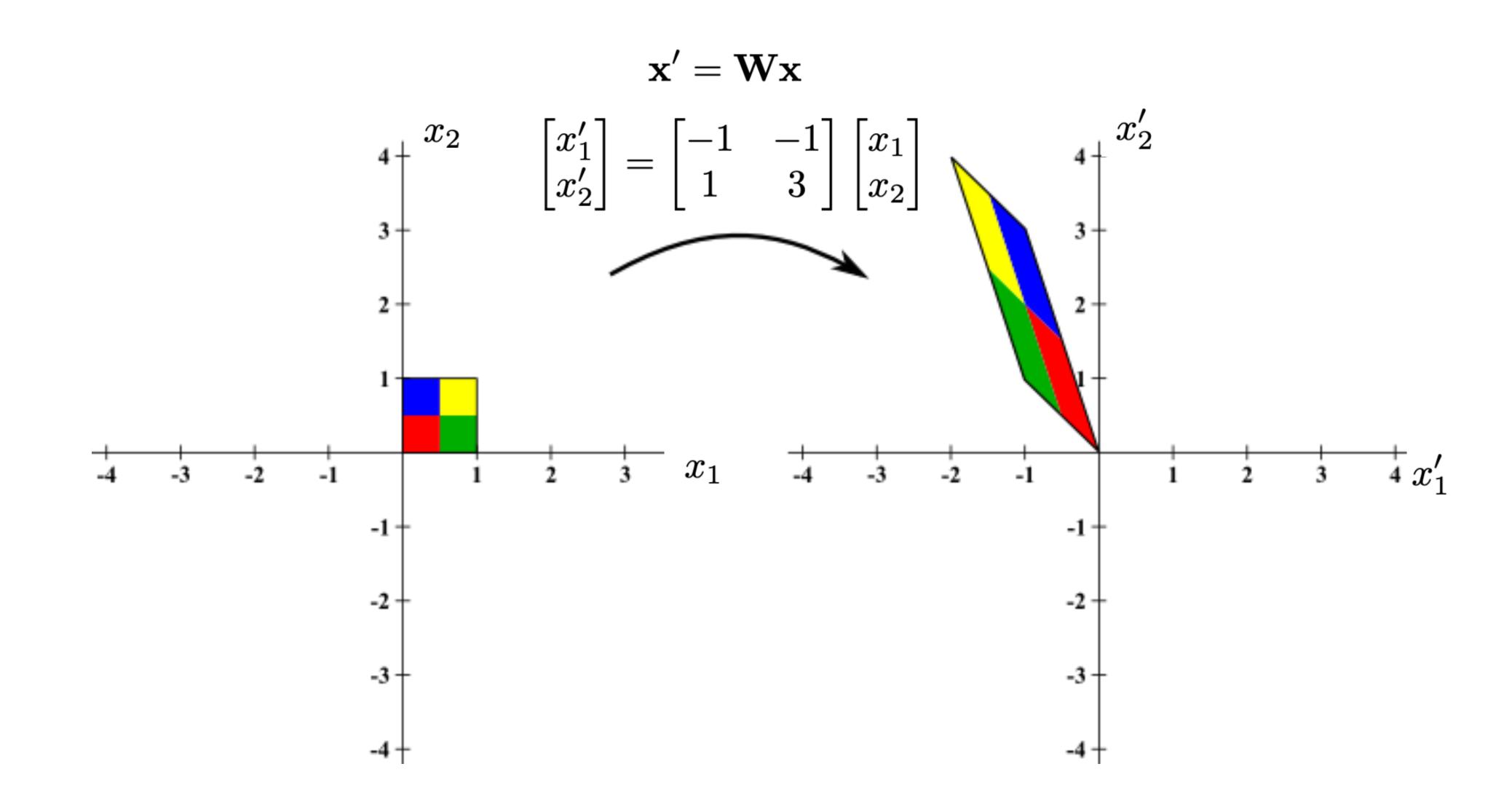


Image adopted from Duane Q. Nykamp

- Problem Set 1 is released
- Reading: <u>Eisenstein 2.6, 3.1-3.3</u>, <u>J+M 7</u>, <u>Goldberg 1-4</u>

PyTorch Tutorial can also be found on the course project

This and Next Lectures

- Neural network history
- Neural network basics
- Feedforward neural networks
- Applications
- Training of neural networks backpropagation, more optimization
- Implementing neural networks

A Bit of History

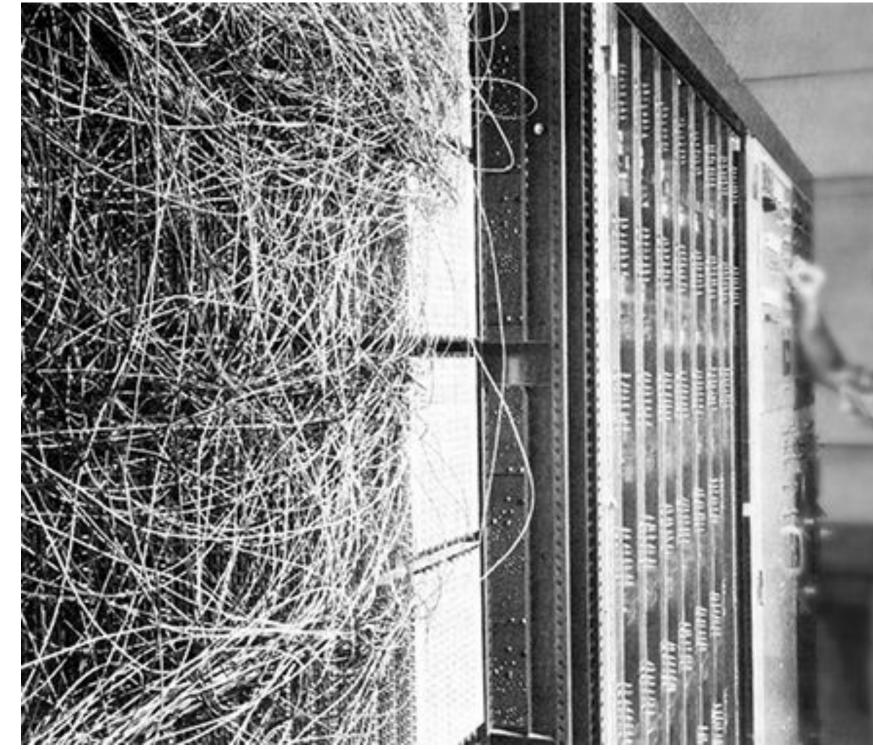
- The Mark I Perceptron machine was the first implementation of the perceptron algorithm.
- Perceptron (Frank Rosenblatt, 1957)
- Artificial Neuron (McCulloch & Pitts, 1943)

McCulloch Pitts Neuron (assuming no inhibitory inputs)

$$y = 1 \quad if \sum_{i=0}^{n} x_i \ge 0$$
$$= 0 \quad if \sum_{i=0}^{n} x_i < 0$$

Perceptron

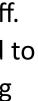
$$y = 1 \quad if \sum_{i=0}^{n} w_i * x_i \ge 0$$
$$= 0 \quad if \sum_{i=0}^{n} w_i * x_i < 0$$



The IBM Automatic Sequence Controlled Calculator, called Mark I by Harvard University's staff. It was designed for image recognition: it had an array of 400 photocells, randomly connected to the "neurons". Weights were encoded in potentiometers, and weight updates during learning were performed by electric motors.

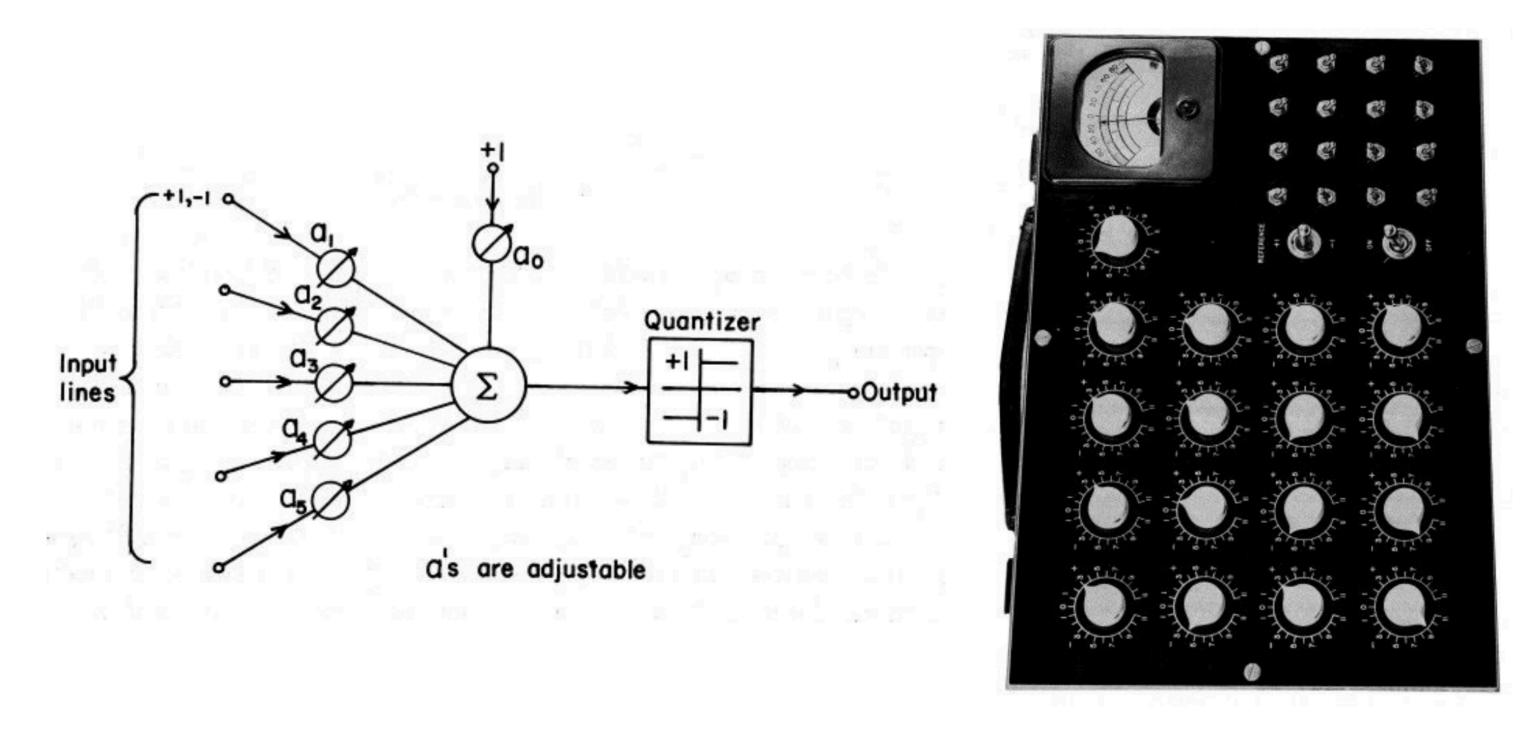
https://www.youtube.com/watch?time_continue=71&v=cNxadbrN_al&feature=emb_logo

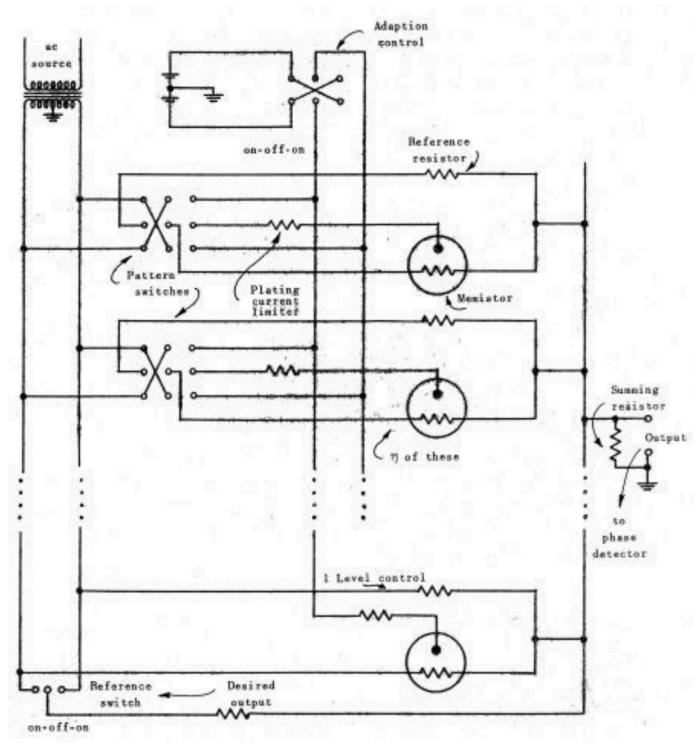




A Bit of History

Adaline/Madeline - single and multi-layer "artificial neurons" (Widrow and Hoff, 1960)





A Bit of History

First time back-propagation became popular (Rumbelhart et al, 1986)

Learning representations by back-propagating errors

David E. Rumelhart*, Geoffrey E. Hinton† & Ronald J. Williams*

* Institute for Cognitive Science, C-015, University of California, San Diego, La Jolla, California 92093, USA [†] Department of Computer Science, Carnegie-Mellon University, Pittsburgh, Philadelphia 15213, USA

We describe a new learning procedure, back-propagation, for networks of neurone-like units. The procedure repeatedly adjusts the weights of the connections in the network so as to minimize a measure of the difference between the actual output vector of the net and the desired output vector. As a result of the weight adjustments, internal 'hidden' units which are not part of the input or output come to represent important features of the task domain, and the regularities in the task are captured by the interactions of these units. The ability to create useful new features distinguishes back-propagation from earlier, simpler methods such as the perceptron-convergence procedure¹.

There have been many attempts to design self-organizing y_i , of the units that are connected to j and of the weights, w_{ii} , neural networks. The aim is to find a powerful synaptic on these connections modification rule that will allow an arbitrarily connected neural network to develop an internal structure that is appropriate for a particular task domain. The task is specified by giving the desired state vector of the output units for each state vector of Units can be given biases by introducing an extra input to each the input units. If the input units are directly connected to the unit which always has a value of 1. The weight on this extra output units it is relatively easy to find learning rules that input is called the bias and is equivalent to a threshold of the iteratively adjust the relative strengths of the connections so as opposite sign. It can be treated just like the other weights. A unit has a real-valued output, y_j , which is a non-linear to progressively reduce the difference between the actual and desired output vectors². Learning becomes more interesting but function of its total input

more difficult when we introduce hidden units whose actual or desired states are not specified by the task. (In perceptrons, there are 'feature analysers' between the input and output that are not true hidden units because their input connections are fixed by hand, so their states are completely determined by the input vector: they do not learn representations.) The learning procedure must decide under what circumstances the hidden units should be active in order to help achieve the desired input-output behaviour. This amounts to deciding what these units should represent. We demonstrate that a general purpose and relatively simple procedure is powerful enough to construct appropriate internal representations.

The simplest form of the learning procedure is for layered networks which have a layer of input units at the bottom; any number of intermediate layers; and a layer of output units at the top. Connections within a layer or from higher to lower layers are forbidden, but connections can skip intermediate layers. An input vector is presented to the network by setting the states of the input units. Then the states of the units in each layer are determined by applying equations (1) and (2) to the connections coming from lower layers. All units within a layer have their states set in parallel, but different layers have their states set sequentially, starting at the bottom and working upwards until the states of the output units are determined.

The total input, x_i , to unit j is a linear function of the outputs,

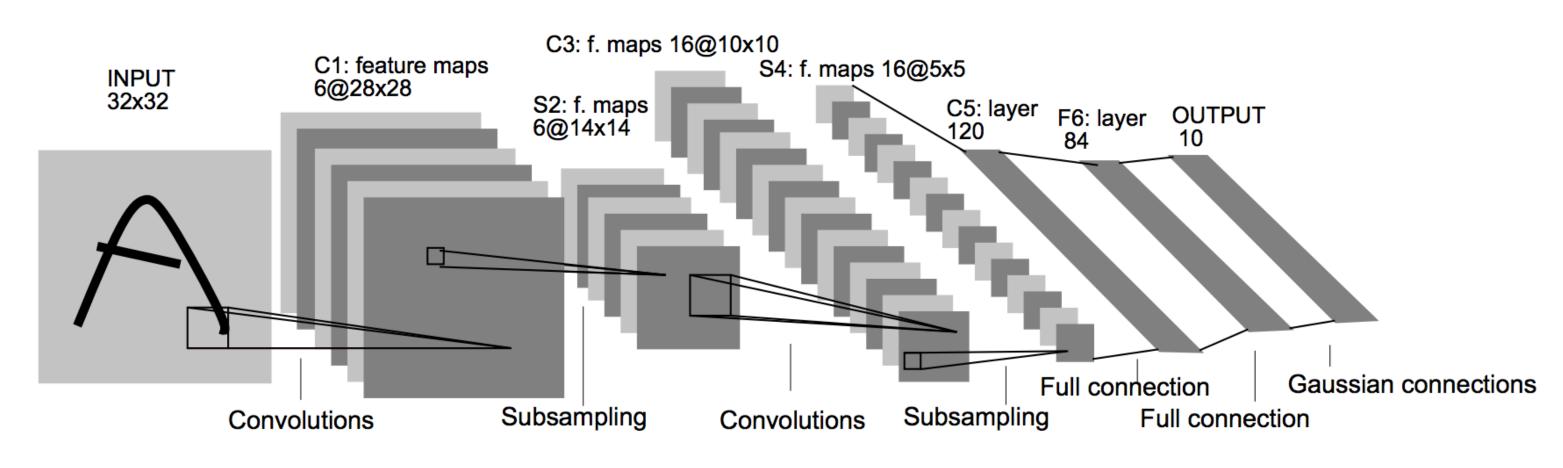
$$x_j = \sum y_i w_{ji} \tag{1}$$

$$y_j = \frac{1}{1 + e^{-x_j}}$$
(2)

©1986 Nature Publishing Group

[†] To whom correspondence should be addressed.

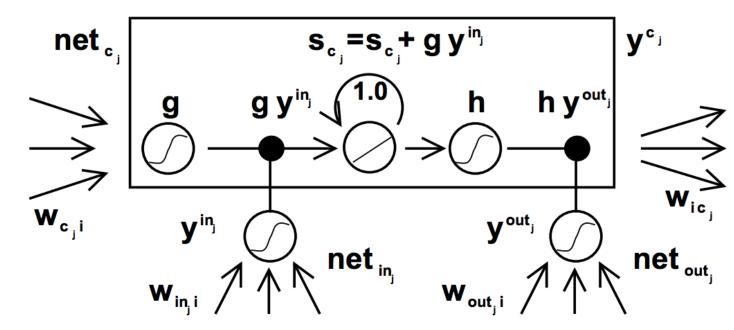
ConvNets: applied to MNIST by LeCun in 1990s



LSTMs: Hochreiter and Schmidhuber (1997)

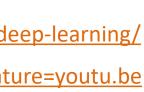
Henderson (2003): neural shift-reduce parser, not SOTA

History: NN "dark ages"



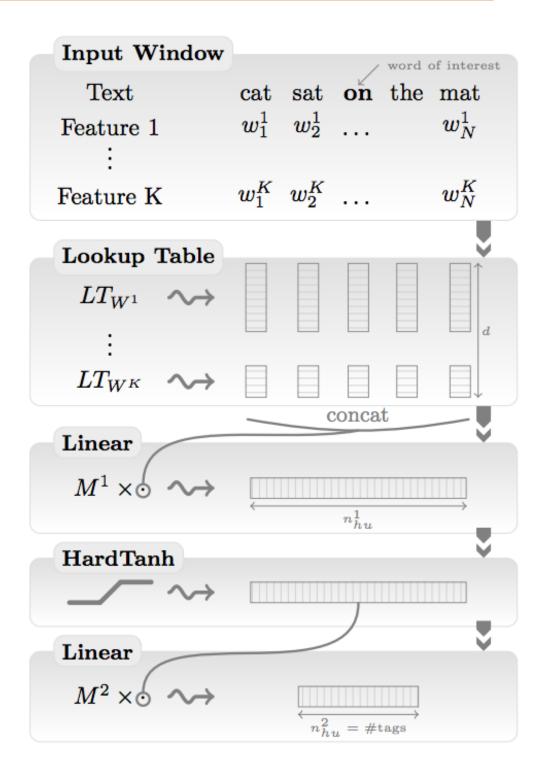
https://www.andreykurenkov.com/writing/ai/a-brief-history-of-neural-nets-and-deep-learning/

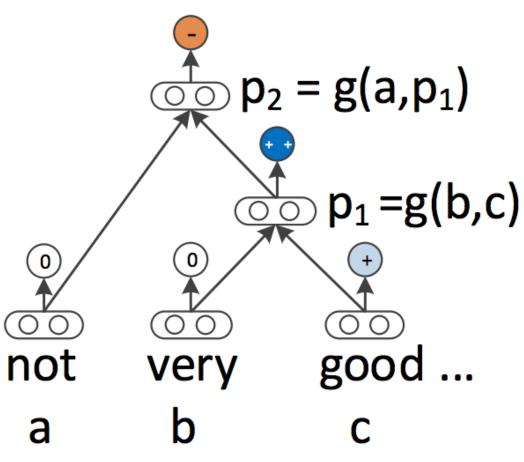
https://www.youtube.com/watch?v=FwFduRA L6Q&feature=youtu.be



2008-2013: A glimmer of light...

- Collobert and Weston 2011: "NLP (almost) from scratch"
 Feedforward neural nets induce features for
 - Feedforward neural nets induce sequential CRFs ("neural CRF")
 - 2008 version was marred by bad experiments, claimed SOTA but wasn't, 2011 version tied SOTA
- Krizhevskey et al. (2012): AlexNet for vision
- Socher 2011-2014: tree-structured RNNs working okay





•••

2014: Stuff starts working

- (convnets work for NLP?)
- neural MT (LSTMs work for NLP?)
- feedforward networks work well for NLP?)
- 2015: explosion of neural nets for everything under the sun

Kim (2014) + Kalchbrenner et al. (2014): sentence classification / sentiment

Sutskever et al. (2014) + Bahdanau et al. (2015) : seq2seq + attention for

Chen and Manning (2014) transition-based dependency parser (even



Why didn't they work before?

- Datasets too small: for MT, not really better until you have 1M+ parallel sentences (and really need a lot more)
- Optimization not well understood: good initialization, per-feature scaling + momentum (AdaGrad / AdaDelta / Adam) work best out-of-the-box
 - Regularization: dropout (2012) is pretty helpful
 - Computers not big enough: can't run for enough iterations
- Inputs: need word representations to have the right continuous semantics
- Libraries: TensorFlow (firs released in Nov 2015), PyTorch (Sep 2016)



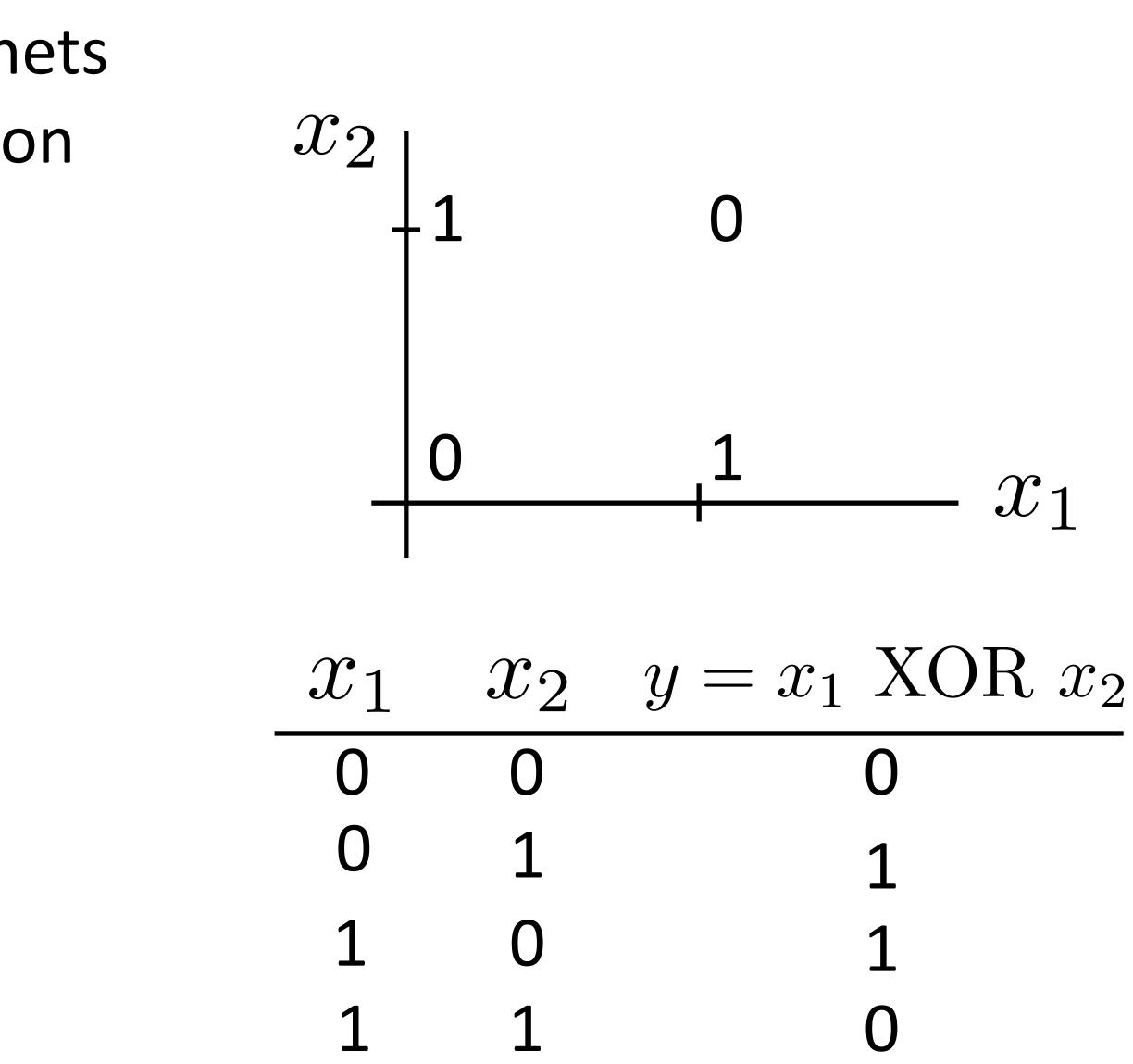
Neural Net Basics

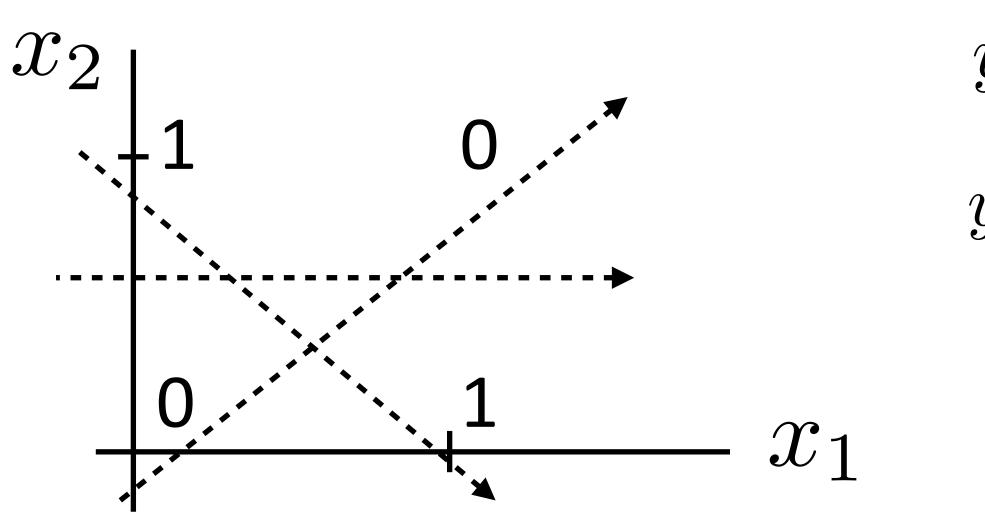
Neural Networks: motivation

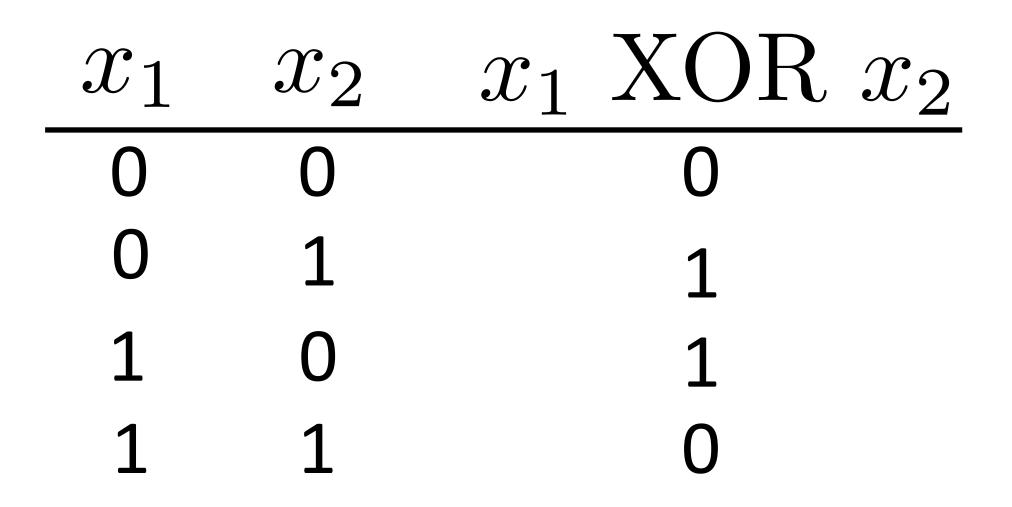
- Linear classification: $\operatorname{argmax}_{y} w^{\top} f(x, y)$
- How can we do nonlinear classification? Kernels are too slow...
- Want to learn intermediate conjunctive features of the input
 - the movie was **not** all that **good**
 - [[contains *not* & contains *good*]

- Let's see how we can use neural nets to learn a simple nonlinear function
- Inputs x_1, x_2 (generally $\mathbf{x} = (x_1, \ldots, x_m)$)
- Output y (generally $\mathbf{y} = (y_1, \ldots, y_n)$)

Neural Networks: XOR





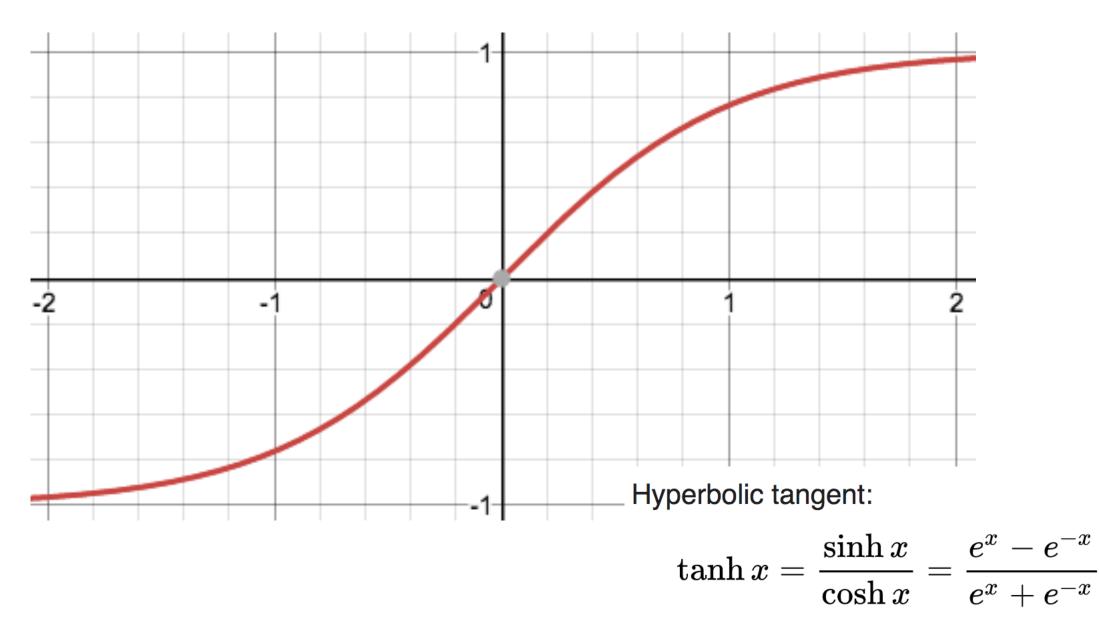


Neural Networks: XOR

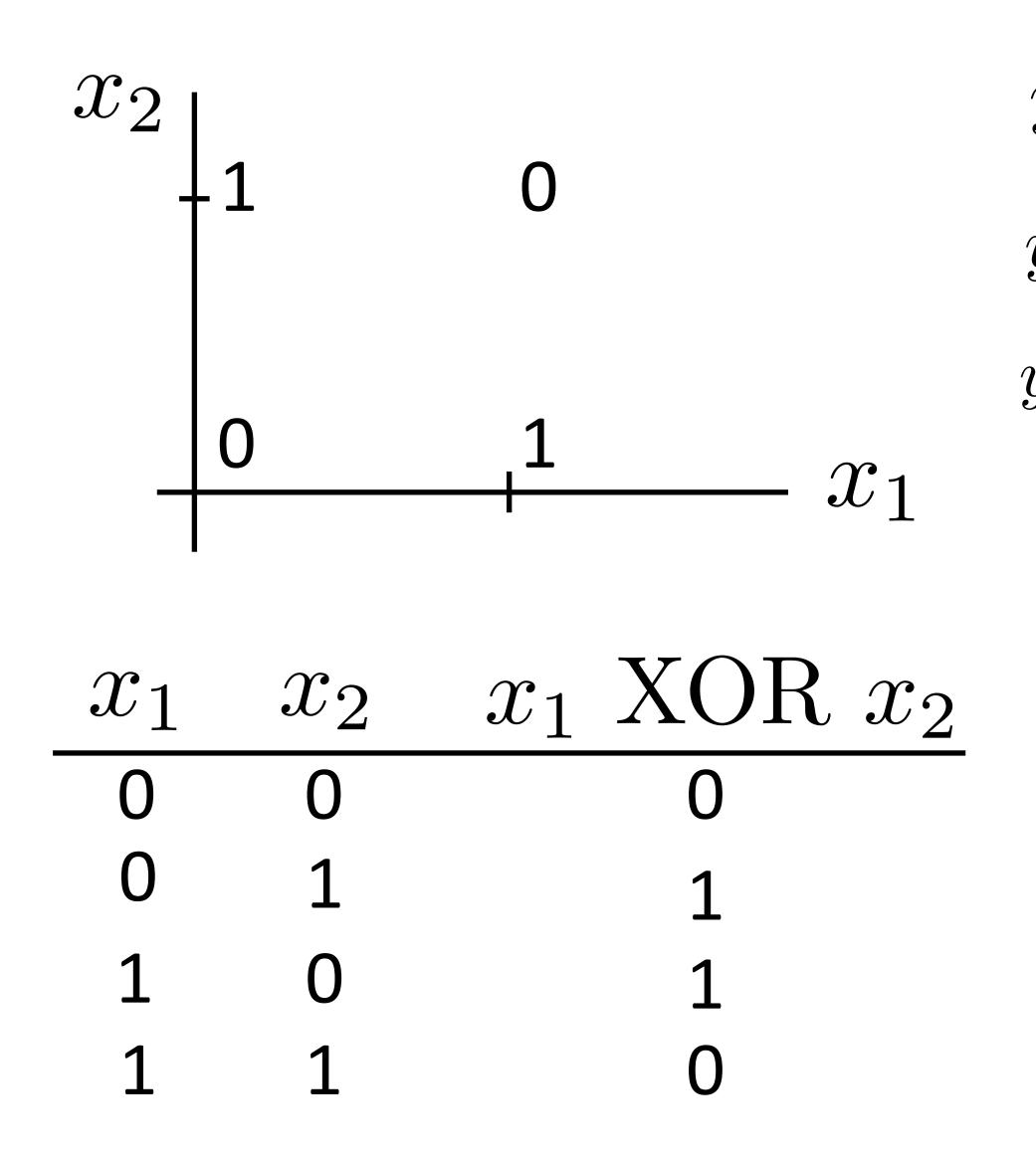
 $y = a_1 x_1 + a_2 x_2$

 $y = a_1 x_1 + a_2 x_2 + a_3 \tanh(x_1 + x_2)$ "or"

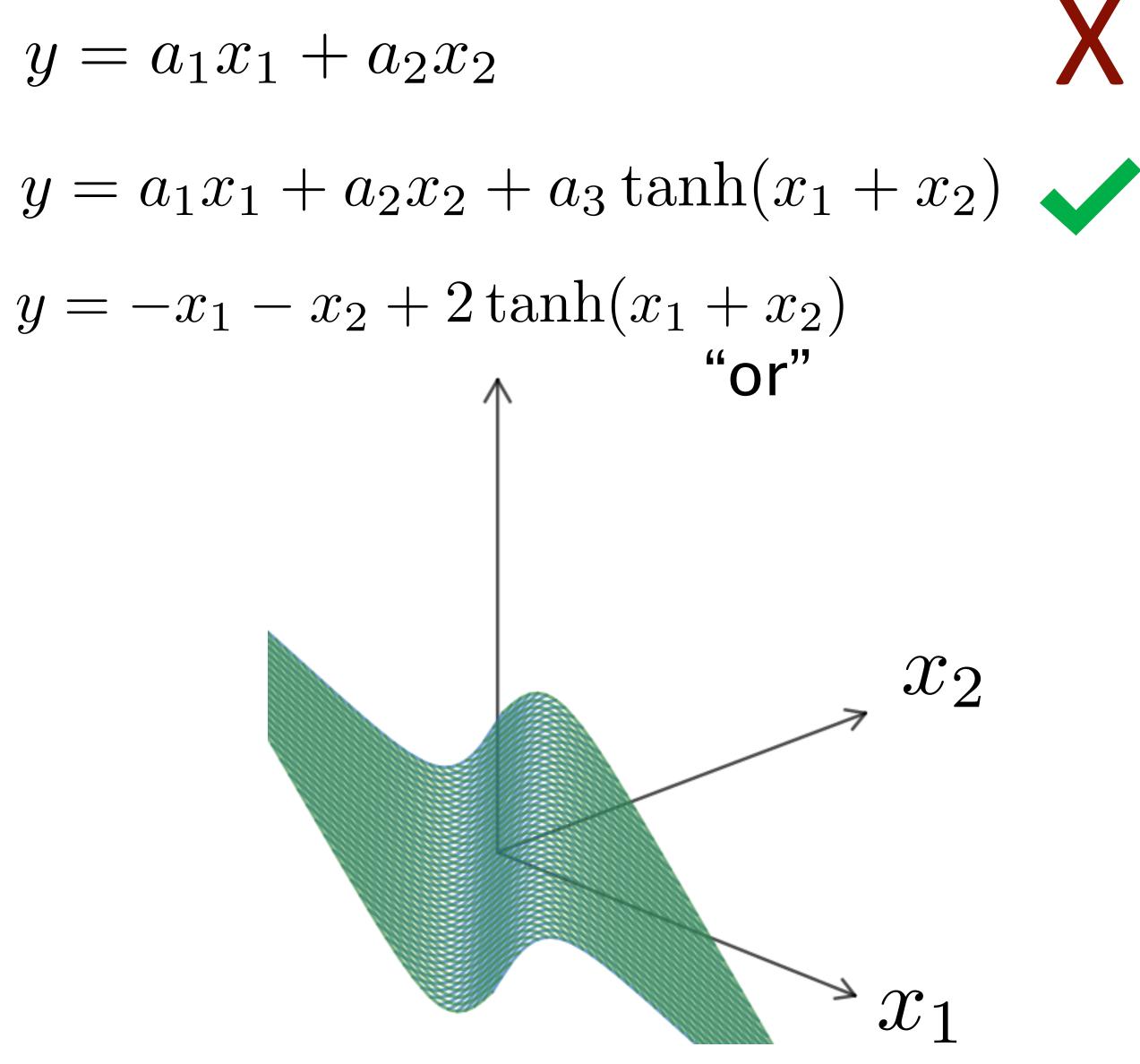
(looks like action potential in neuron)



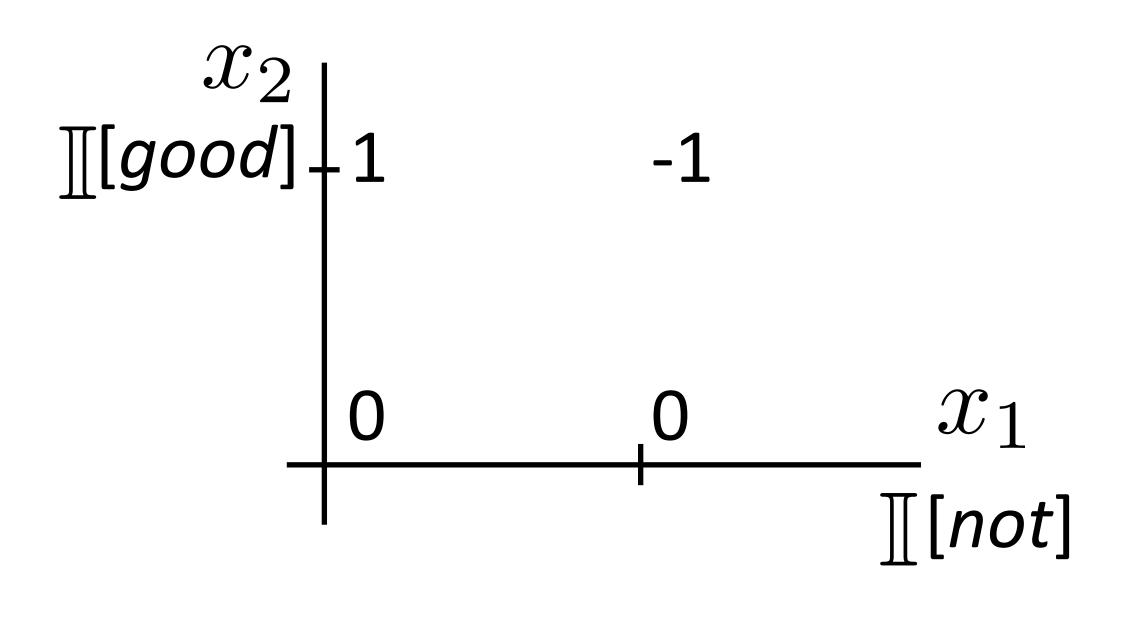




Neural Networks: XOR

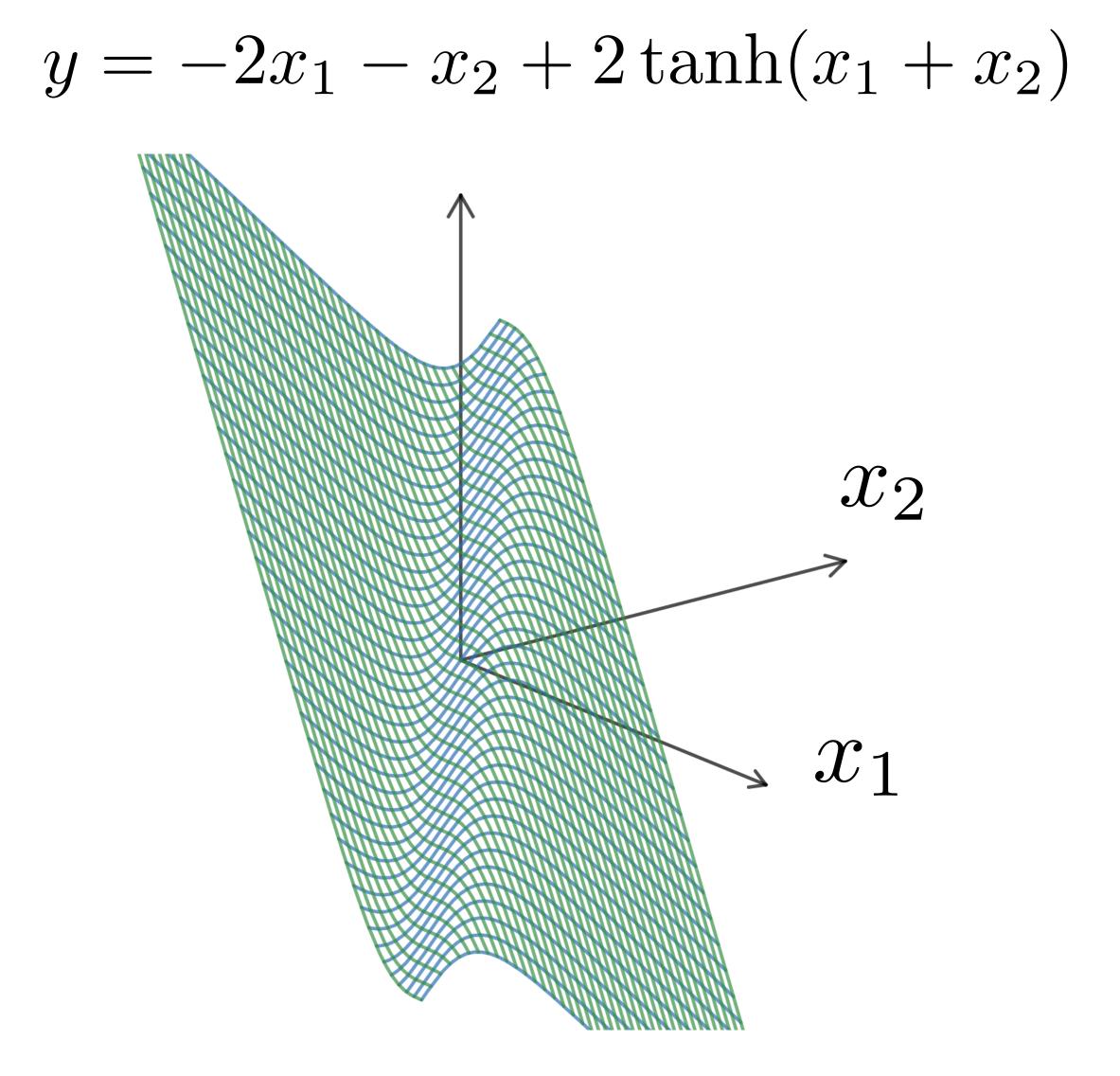




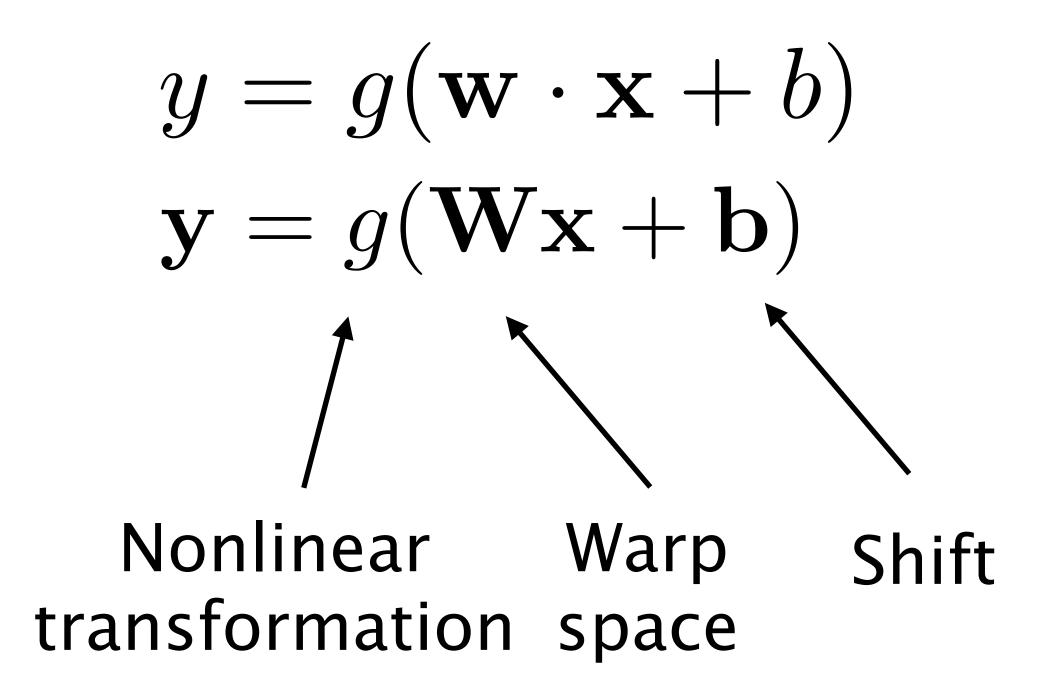


the movie was **not** all that **good**

Neural Networks: XOR

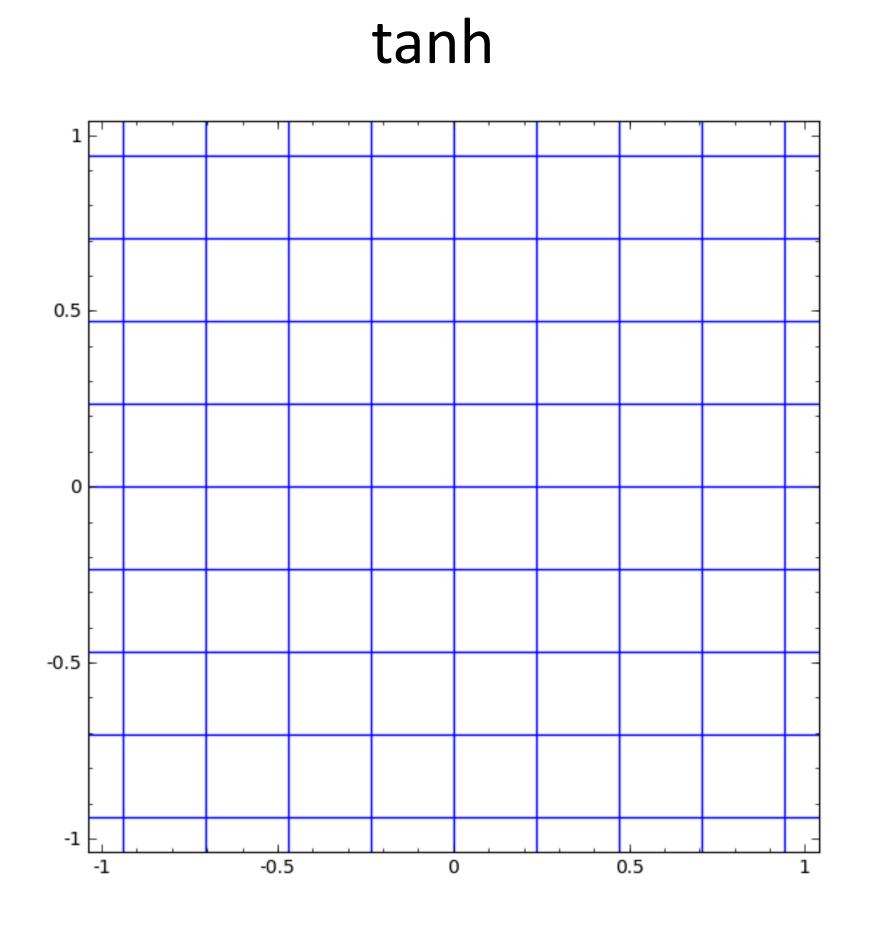


Linear model: $y = \mathbf{w} \cdot \mathbf{x} + b$



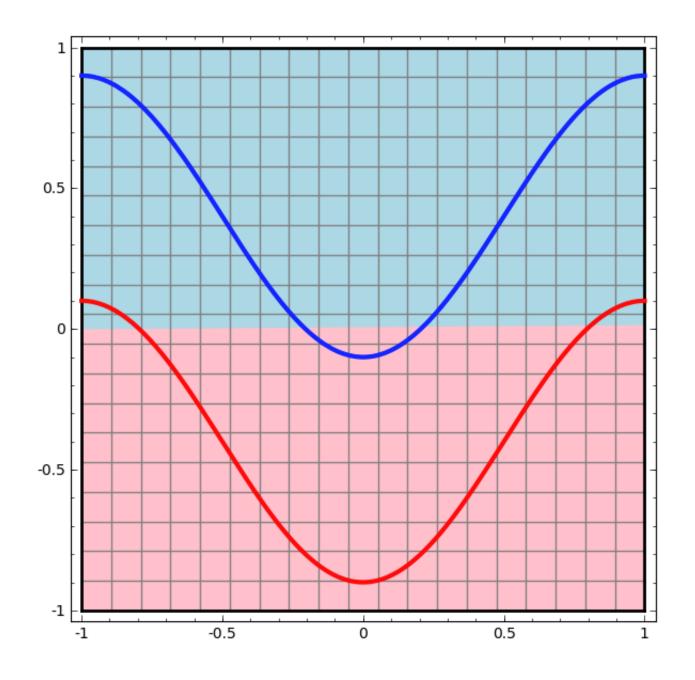
Taken from http://colah.github.io/posts/2014-03-NN-Manifolds-Topology/

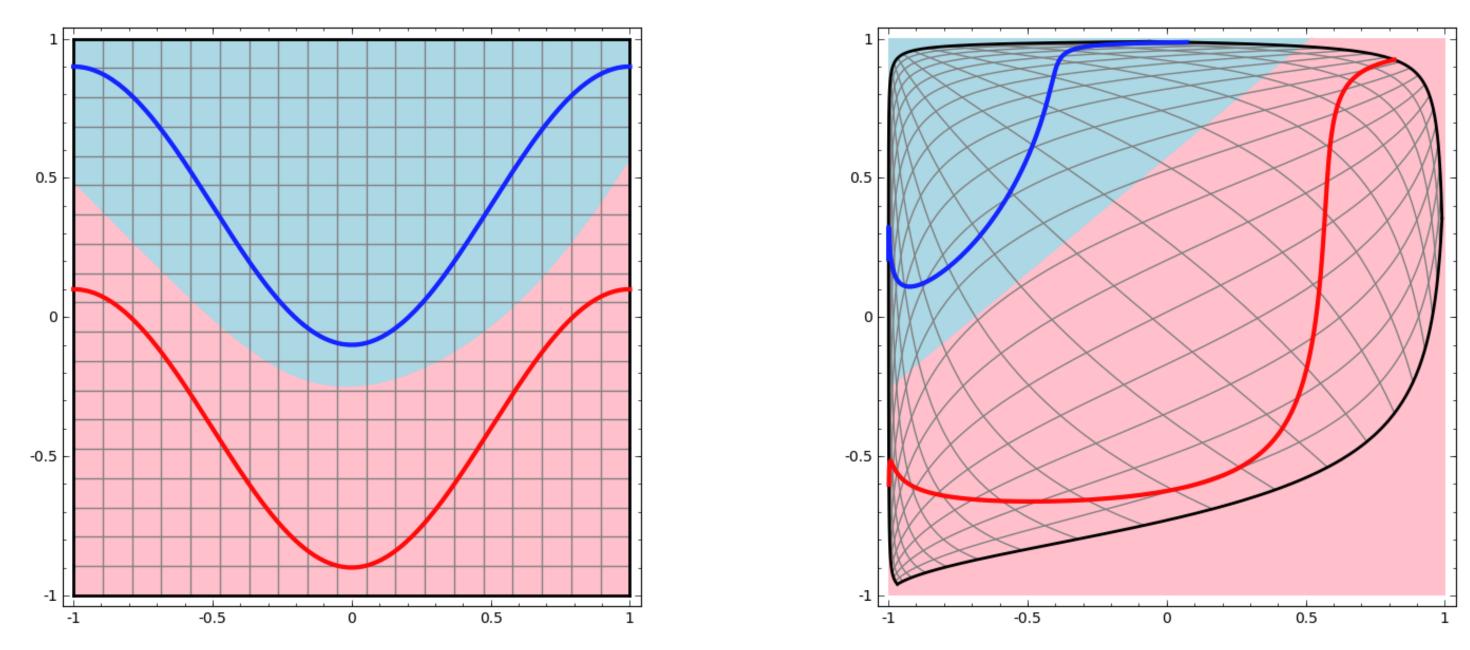
Neural Networks





Linear classifier





Taken from http://colah.github.io/posts/2014-03-NN-Manifolds-Topology/

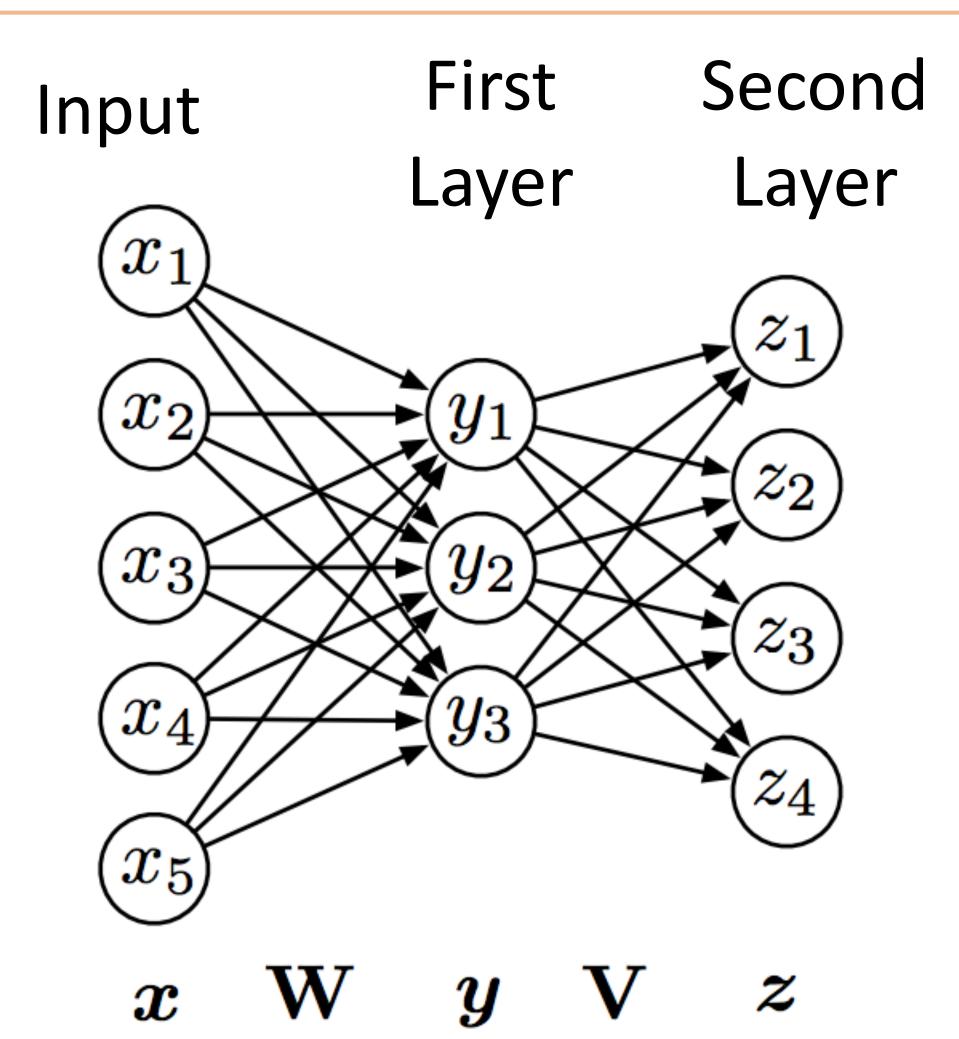
Neural Networks

Neural network

...possible because we transformed the space!



Deep Neural Networks



$$y = g(Wx + b)$$

$$z = g(Vy + c)$$

$$z = g(Vg(Wx + b) + c)$$

output of first layer

"Feedforward" computation (not recurrent)

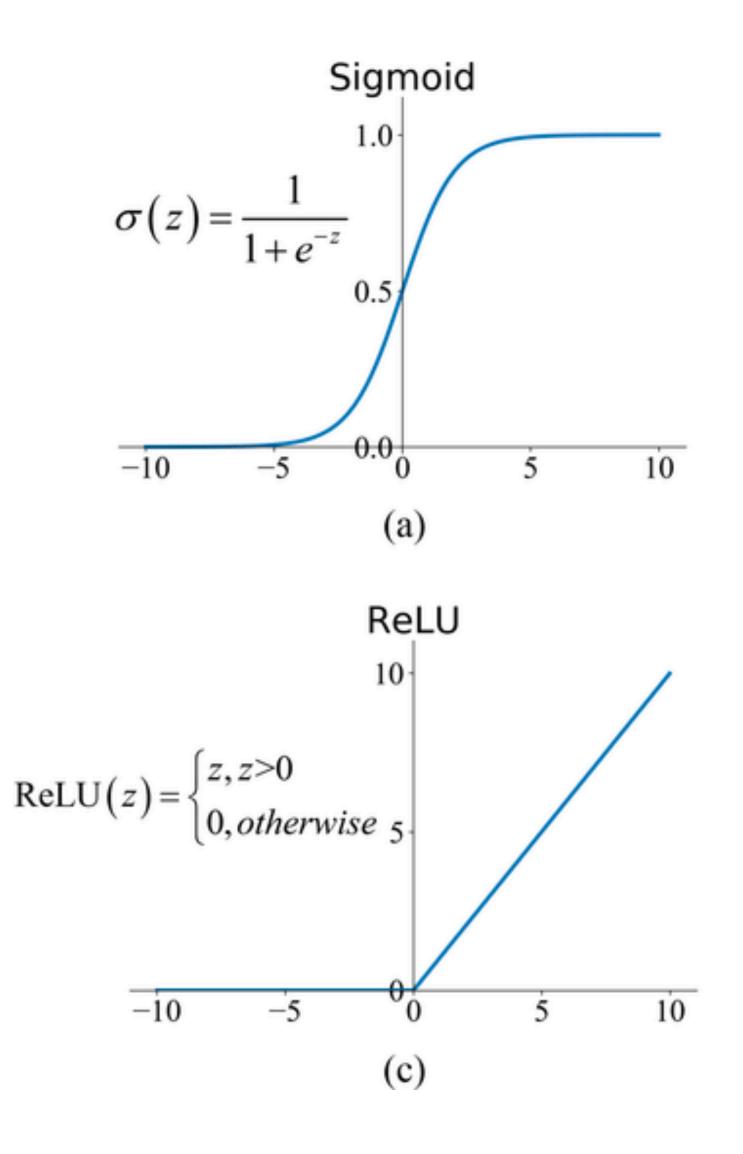
Check: what happens if no nonlinearity? More powerful than basic linear models?

$$z = V(Wx + b) + c$$

Adopted from Chris Dyer



Activation Functions



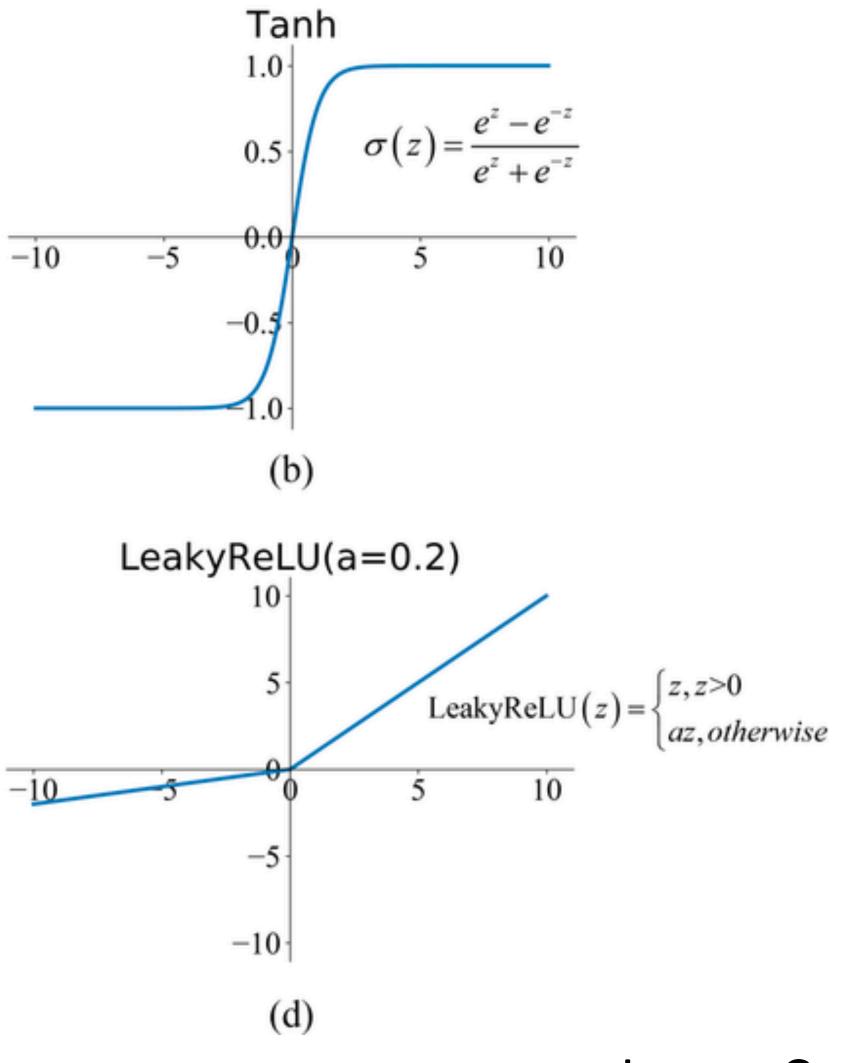
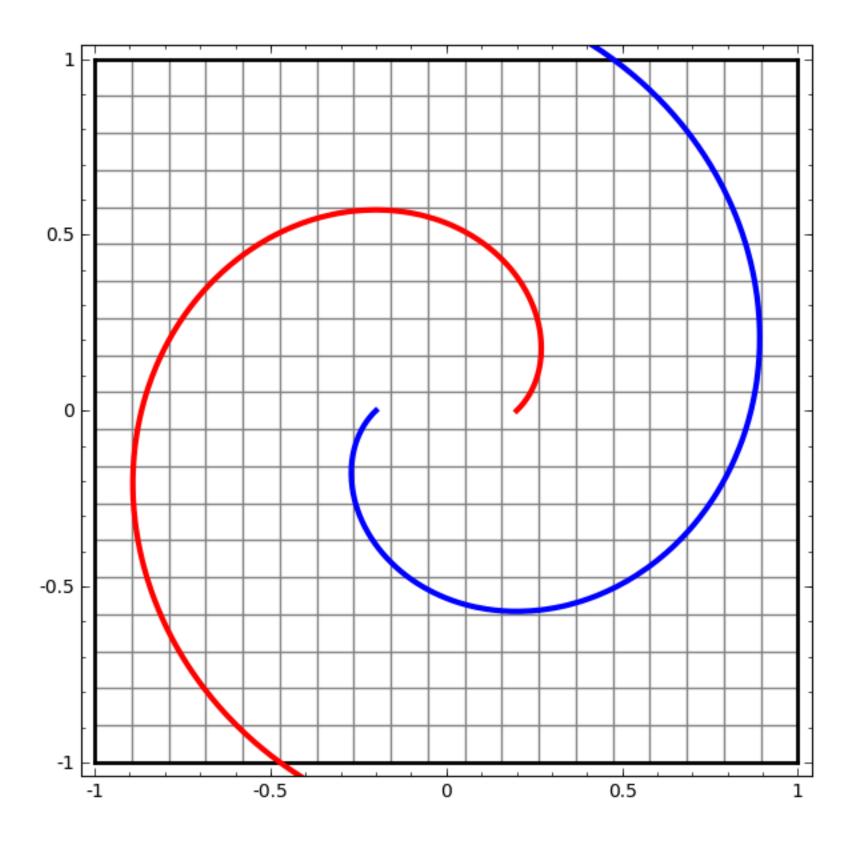


Image Credit: Junxi Feng



Deep Neural Networks

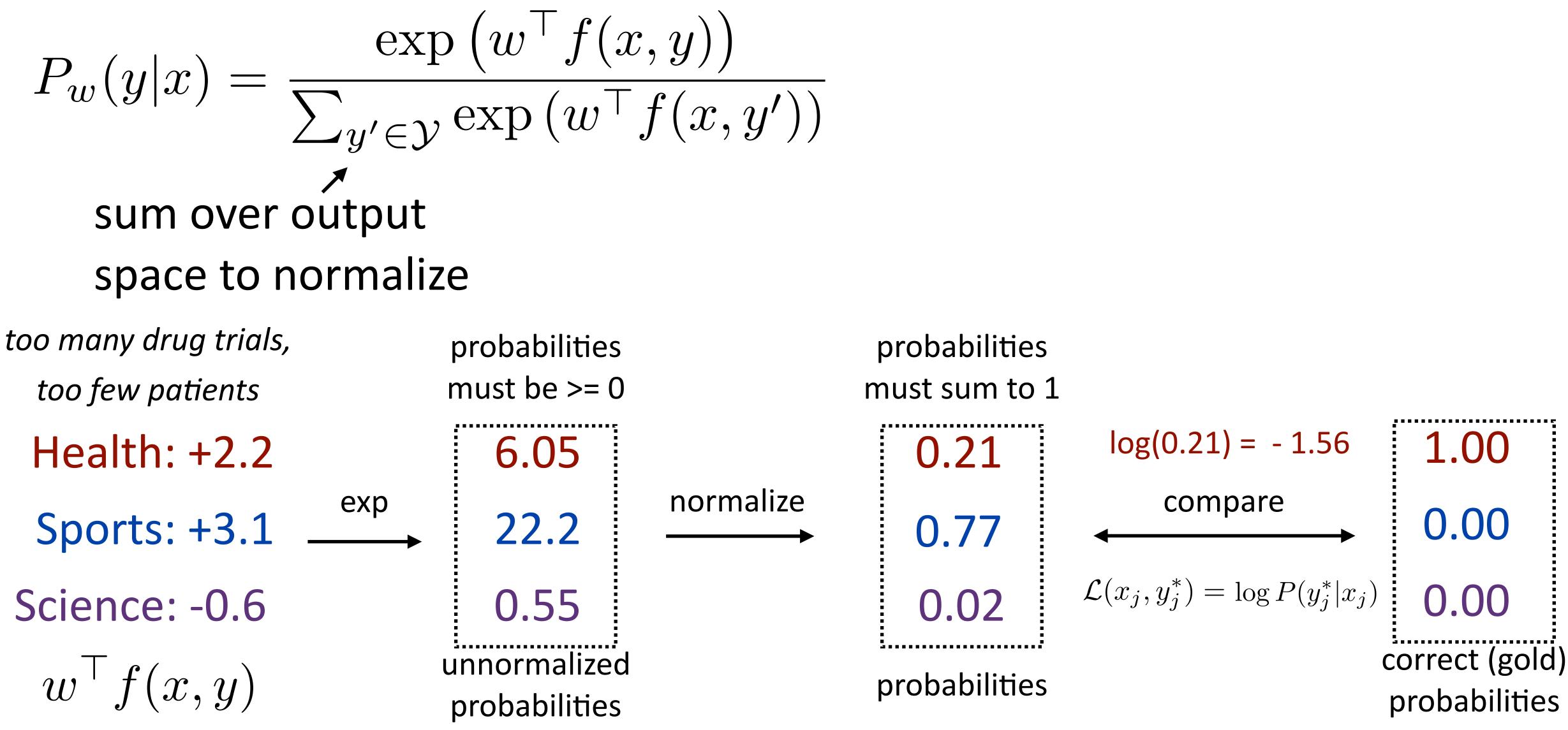


Taken from http://colah.github.io/posts/2014-03-NN-Manifolds-Topology/



Feedforward Networks, Backpropagation

Recap: Multiclass Logistic Regression



Logistic Regression with NNs

$$P(y|\mathbf{x}) = \frac{\exp(w^{\top} f(\mathbf{x}, y))}{\sum_{y'} \exp(w^{\top} f(\mathbf{x}, y'))}$$

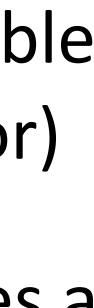
 $P(\mathbf{y}|\mathbf{x}) = \operatorname{softmax}\left([w^{\top}f(\mathbf{x}, y)]_{y \in \mathcal{Y}}\right)$

$$\operatorname{softmax}(p)_i = \frac{\exp}{\sum_{i'} \exp}$$

 $P(\mathbf{y}|\mathbf{x}) = \operatorname{softmax}(Wf(\mathbf{x}))$

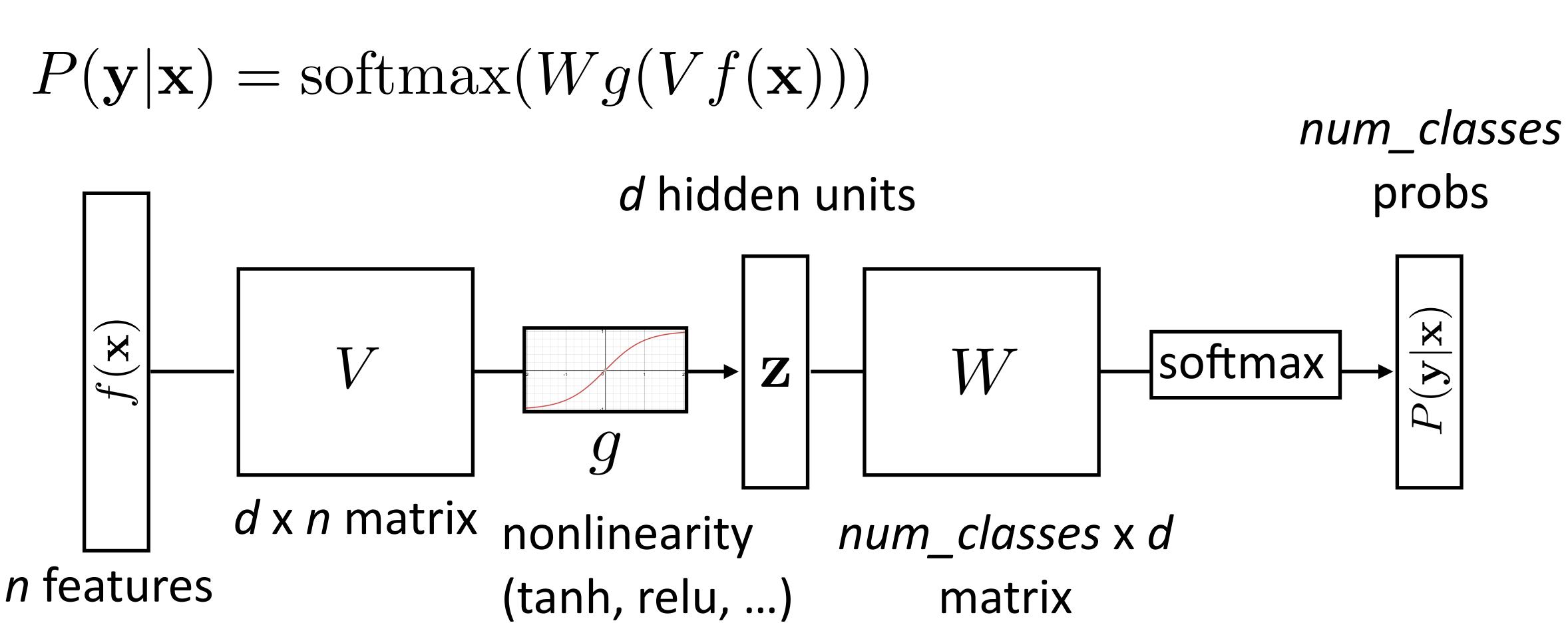
 $P(\mathbf{y}|\mathbf{x}) = \operatorname{softmax}(Wg(Vf(\mathbf{x})))$

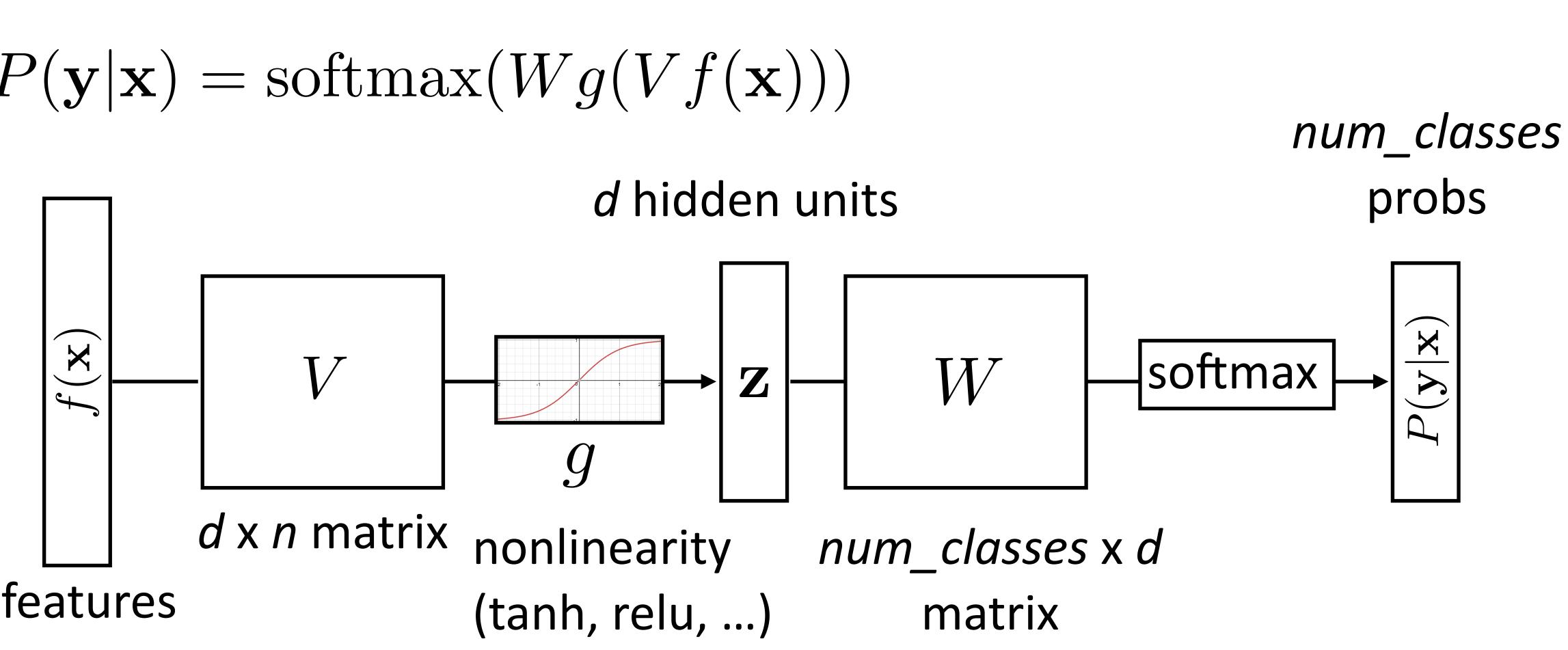
- Single scalar probability
- Compute scores for all possible labels at once (returns vector)
- (p_i) $\exp(p_{i'})$
- softmax: exps and normalizes a given vector
- Weight vector per class; W is [num classes x num feats]
- Now one hidden layer





Neural Networks for Classification





We can think of a neural network classifier with one hidden layer as building a vector z which is a hidden layer representation (i.e. latent features) of the input, and then running standard logistic regression on the features that the network develops in z.

Training Neural Networks

$$P(\mathbf{y}|\mathbf{x}) = \operatorname{softmax}(W\mathbf{z})$$

Maximize log likelihood of training data

$$\mathcal{L}(\mathbf{x}, i^*) = \log P(y = i^* | \mathbf{x}) =$$

*i**: index of the gold label *e_i*: 1 in the *i*th row, zero elsewhere. Dot by this = select *i*th index

one-hot vector

 $\mathbf{z} = g(Vf(\mathbf{x}))$

 $= \log (\operatorname{softmax}(W\mathbf{z}) \cdot e_{i^*})$

Training Neural Networks

$$P(\mathbf{y}|\mathbf{x}) = \operatorname{softmax}(W\mathbf{z})$$

Maximize log likelihood of training data

$$\mathcal{L}(\mathbf{x}, i^*) = \log P(y = i^* | \mathbf{x}) =$$

- i*: index of the gold label
- e_i : 1 in the *i*th row, zero elsewhere. Dot by this = select *i*th index

$$\mathcal{L}(\mathbf{x}, i^*) = W\mathbf{z} \cdot e_{i^*} - \log \sum_{i \in \mathcal{L}} V_i \mathbf{x} \cdot e_$$

 $\mathbf{z} = g(Vf(\mathbf{x}))$

 $= \log (\operatorname{softmax}(W\mathbf{z}) \cdot e_{i^*})$

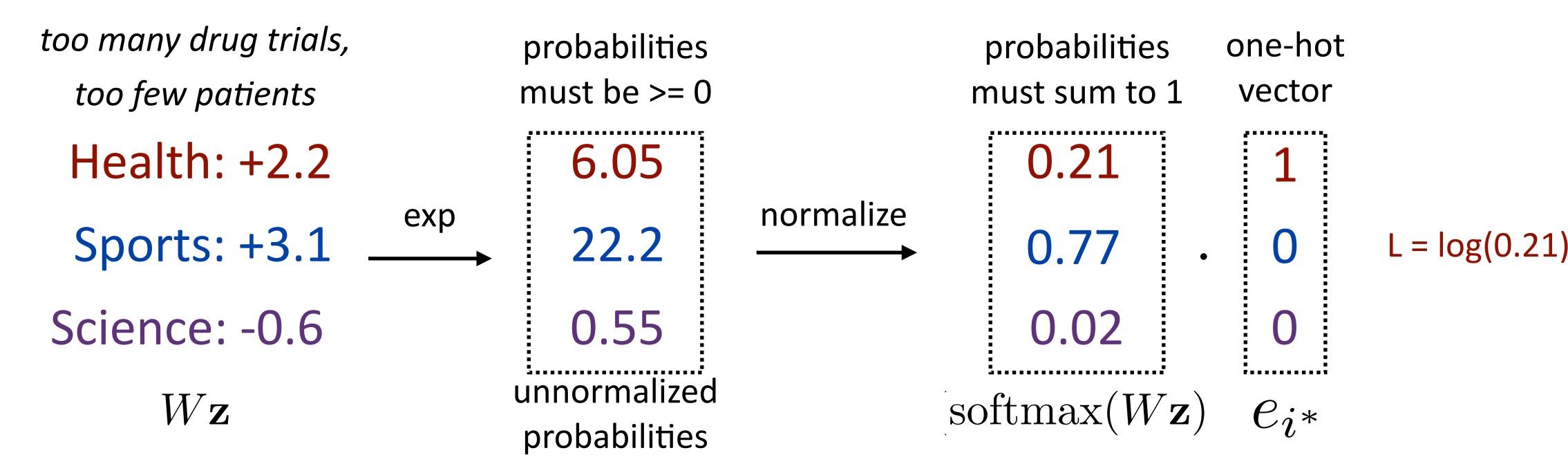
 $\sum \exp(W\mathbf{z}) \cdot e_j$

Training Neural Networks

Maximize log likelihood of training data

$$\mathcal{L}(\mathbf{x}, i^*) = \log P(y = i^* | \mathbf{x}) =$$

i*: index of the gold label • e_i : 1 in the *i*th row, zero elsewhere. Dot by this = select *i*th index



 $= \log (\operatorname{softmax}(W\mathbf{z}) \cdot e_{i^*})$



Computing Gradients

$$\mathcal{L}(\mathbf{x}, i^{*}) = W\mathbf{z} \cdot e_{i^{*}} - \log \sum_{j} \exp(W\mathbf{z}) \cdot e_{j} \qquad num_classes \mathbf{x}$$

$$\mathbf{w} \qquad \text{matrix}$$

$$\mathbf{W} \qquad \mathbf{w} \qquad$$

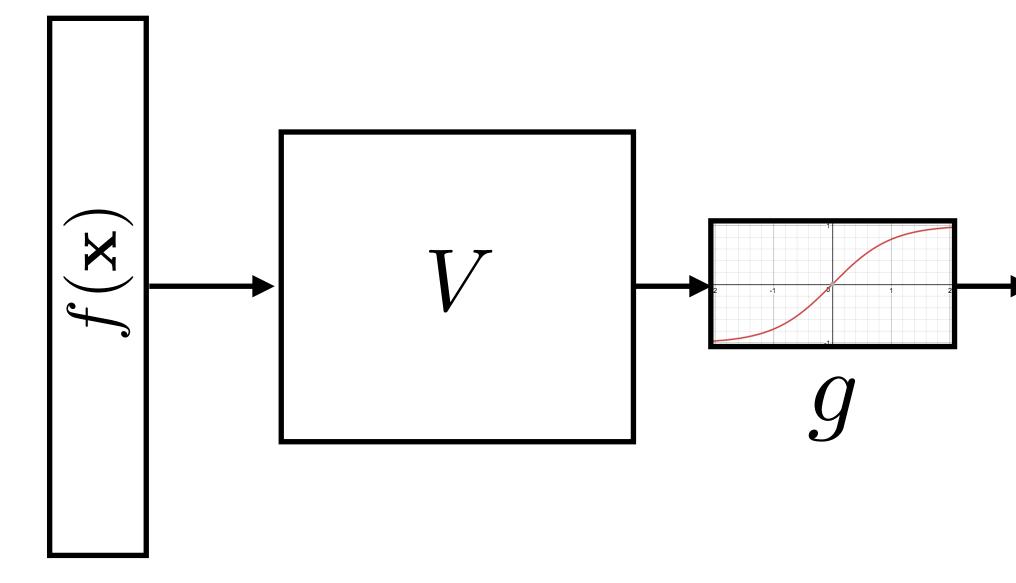
Looks like logistic regression with z as the features!

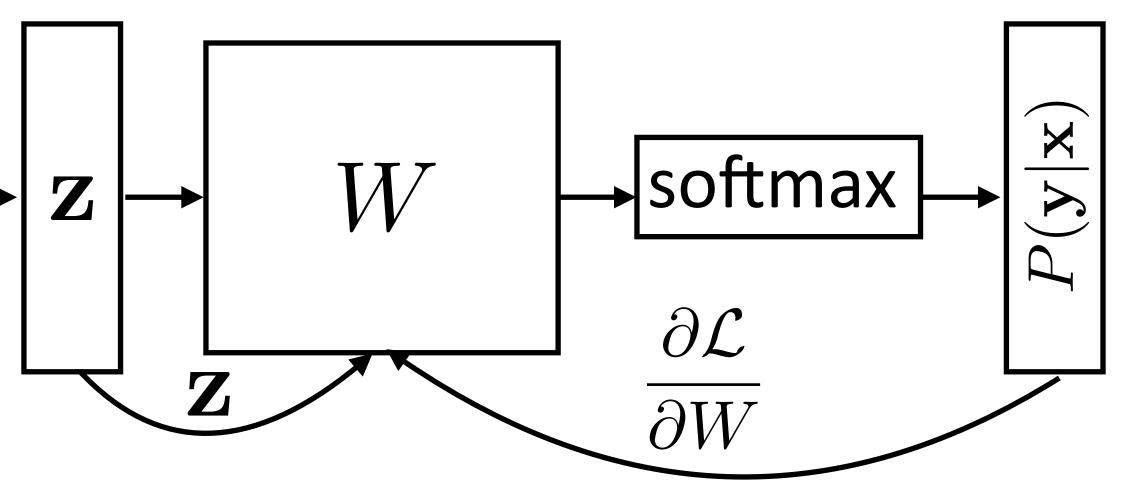




Neural Networks for Classification



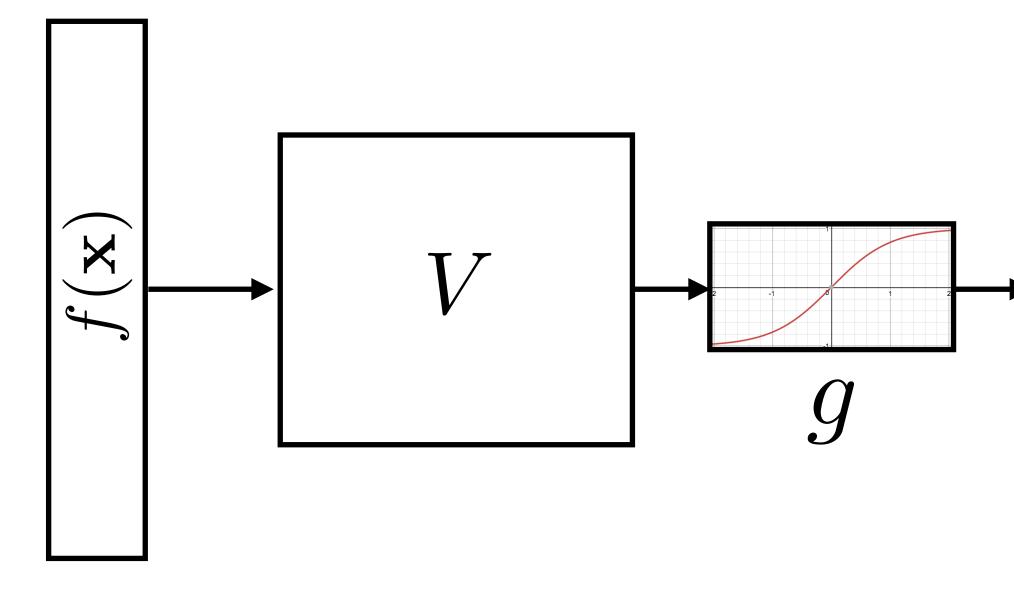


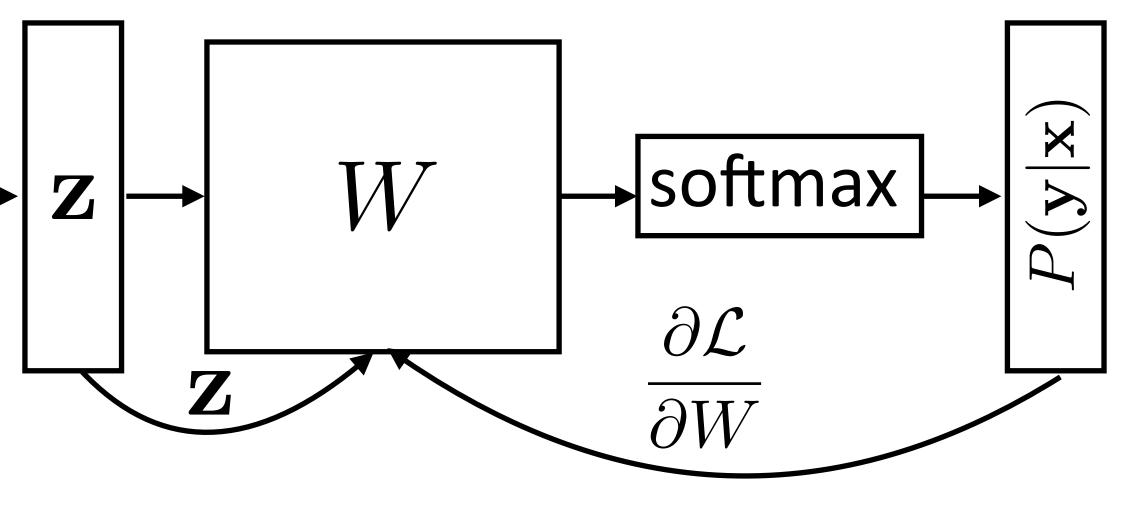


Gradient w.r.t. W: looks like logistic regression with *z* as the features!

Neural Networks for Classification



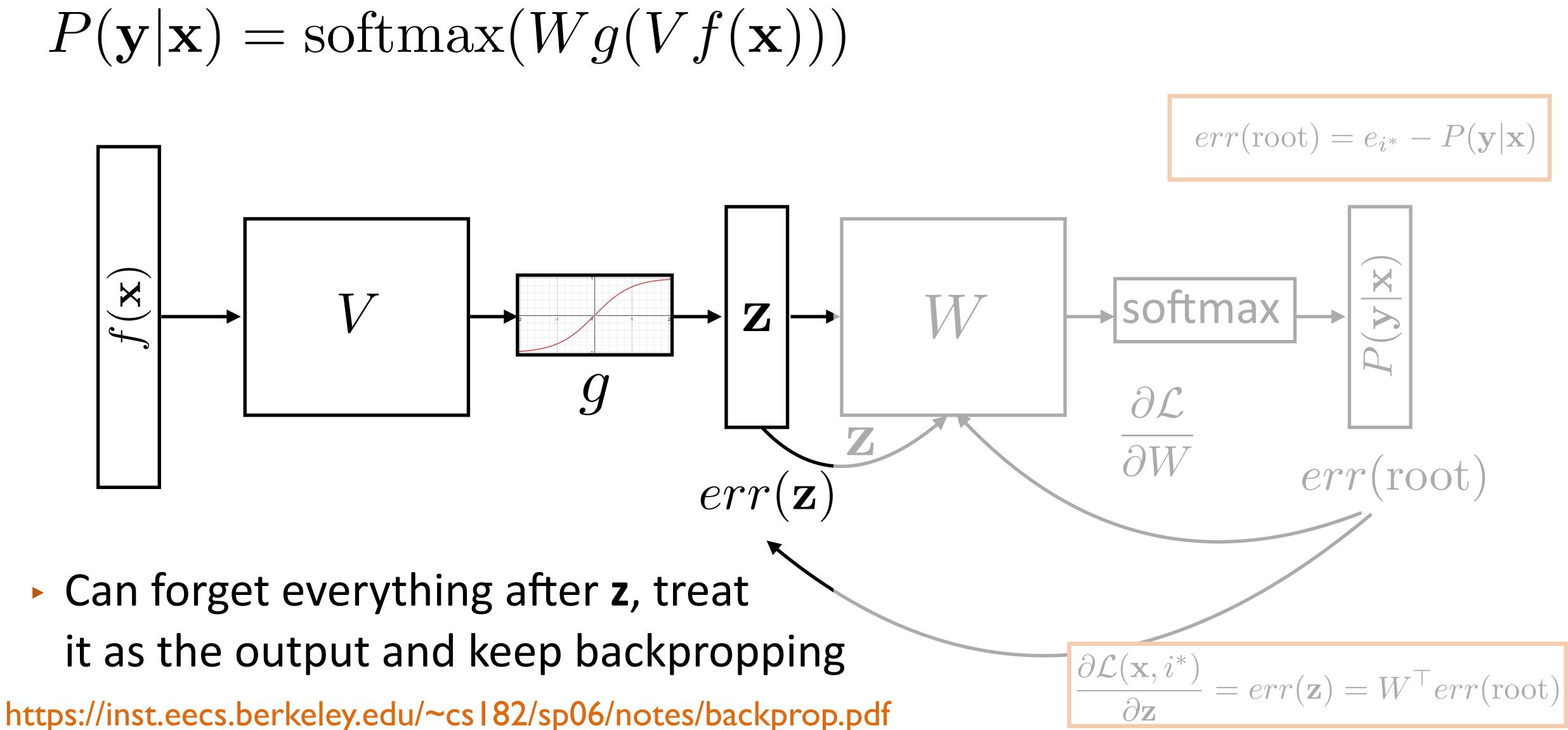


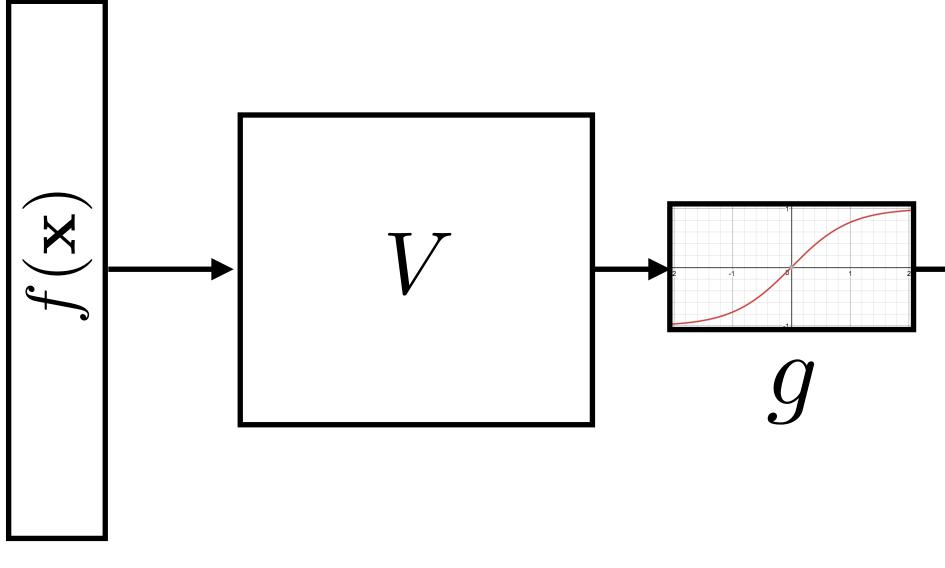


 $\frac{\partial \mathcal{L}(\mathbf{x}, i^*)}{\partial \mathbf{W}} = \mathbf{z}(e_{i^*} - P(\mathbf{y}|\mathbf{x})) = \mathbf{z} \cdot err(\text{root})$



Backpropagation: Picture

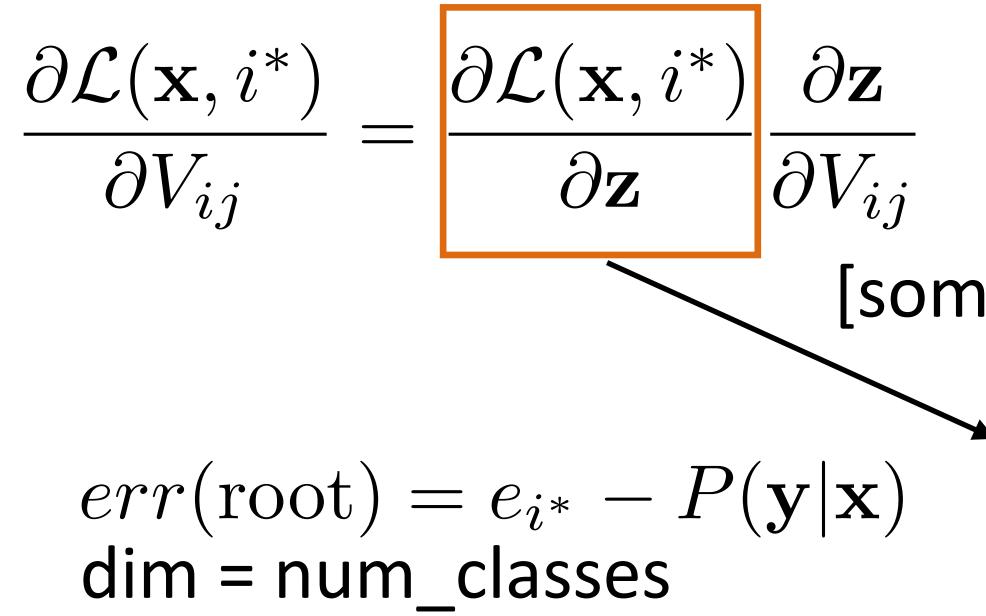




Computing Gradients: Backpropagation

$$\mathcal{L}(\mathbf{x}, i^*) = W\mathbf{z} \cdot e_{i^*} - \log \sum_j \exp(W\mathbf{z}) \cdot e_j$$

Gradient with respect to V: apply the chain rule



 $\mathbf{z} = g(Vf(\mathbf{x}))$ Activations at hidden layer

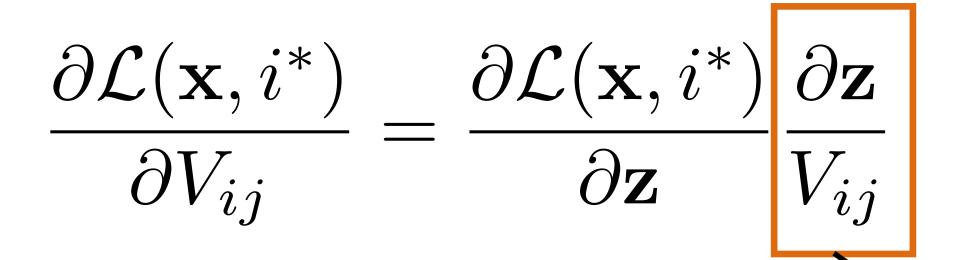
[some math...]

$$\frac{\partial \mathcal{L}(\mathbf{x}, i^*)}{\partial \mathbf{z}} = err(\mathbf{z}) = W^{\top} err(\text{root})$$
$$\dim = d$$

Computing Gradients: Backpropagation

$$\mathcal{L}(\mathbf{x}, i^*) = W\mathbf{z} \cdot e_{i^*} - \log \sum_{j=1}^{\infty} \frac{1}{j} = 1$$

Gradient with respect to V: apply the chain rule

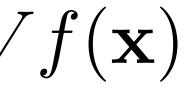


- First term: gradient of nonlinear activation function at *a* (depends on current value)
- Second term: gradient of linear function
- Straightforward computation once we have err(z)

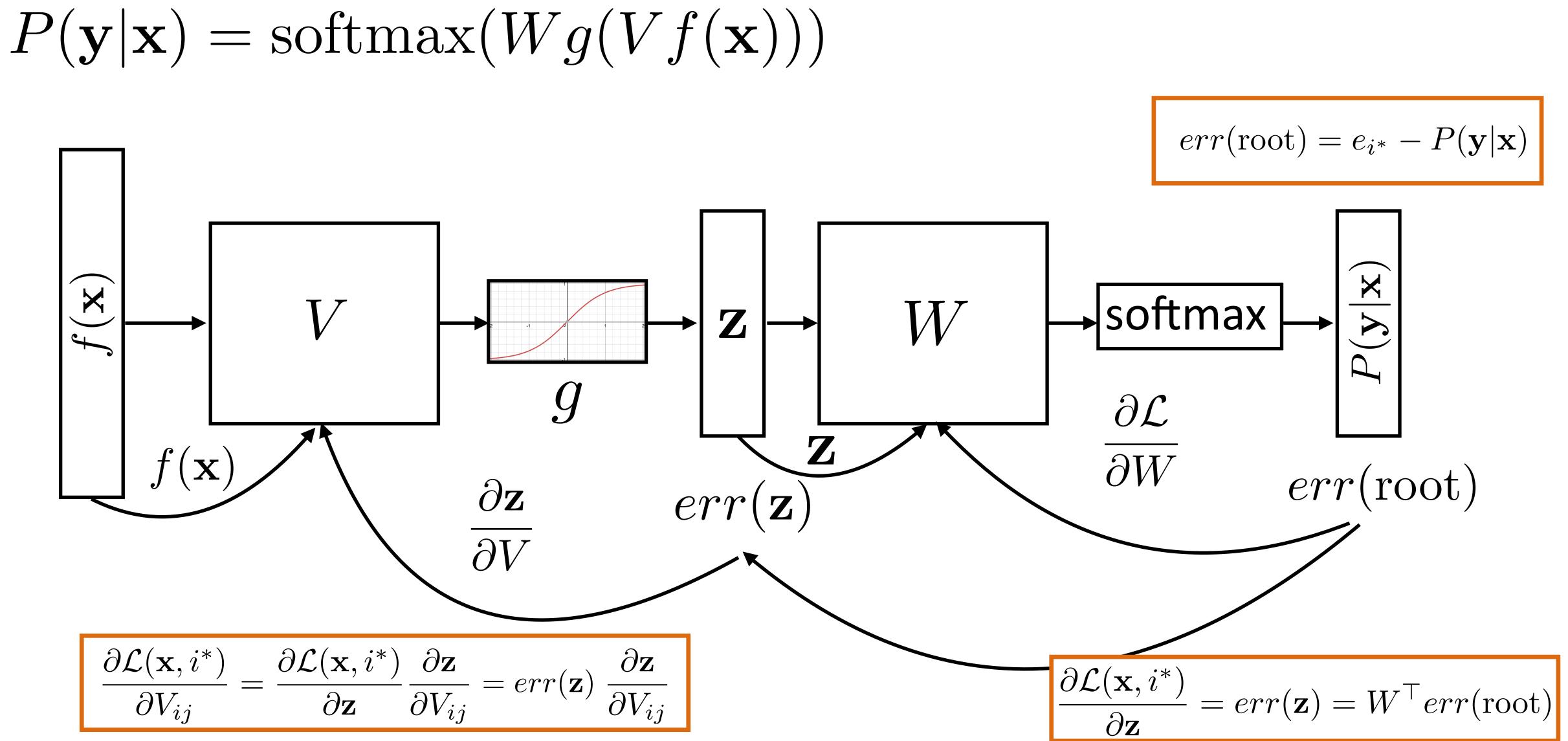
- ${m}$
 - $\sum_{j=1}^{N} \exp(W\mathbf{z} \cdot e_j)$

$\mathbf{z} = g(Vf(\mathbf{x}))$ Activations at hidden layer

$$\frac{\partial \mathbf{z}}{V_{ij}} = \frac{\partial g(\mathbf{a})}{\partial \mathbf{a}} \frac{\partial \mathbf{a}}{\partial V_{ij}} \quad \mathbf{a} = V$$



Backpropagation: Picture



Backpropagation

$$P(\mathbf{y}|\mathbf{x}) = \operatorname{softmax}(Wg(Vf$$

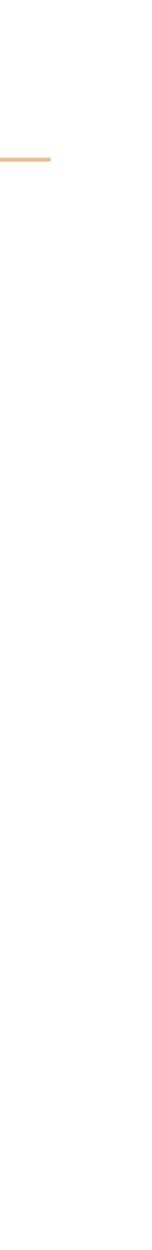
- Step 1: compute $err(root) = e_{i^*} P(\mathbf{y}|\mathbf{x})$ (vector)
- Step 2: compute derivatives of W using err(root) (matrix)
- Step 3: compute $\frac{\partial \mathcal{L}(\mathbf{x}, i^*)}{\partial \mathbf{z}} = err(\mathbf{z}) = W^{\top} err(root)$ (vector)
- Step 4: compute derivatives of V using err(z) (matrix)
- Step 5+: continue backpropagation (compute err(f(x)) if necessary...)

 $f(\mathbf{x})))$

Backpropagation: Takeaways

- Gradients of output weights W are easy to compute looks like logistic regression with hidden layer z as feature vector
- Can compute derivative of loss with respect to z to form an "error signal" for backpropagation
- Easy to update parameters based on "error signal" from next layer, keep pushing error signal back as backpropagation
- Need to remember the values from the forward computation

https://inst.eecs.berkeley.edu/~cs182/sp06/notes/backprop.pdf



Applications

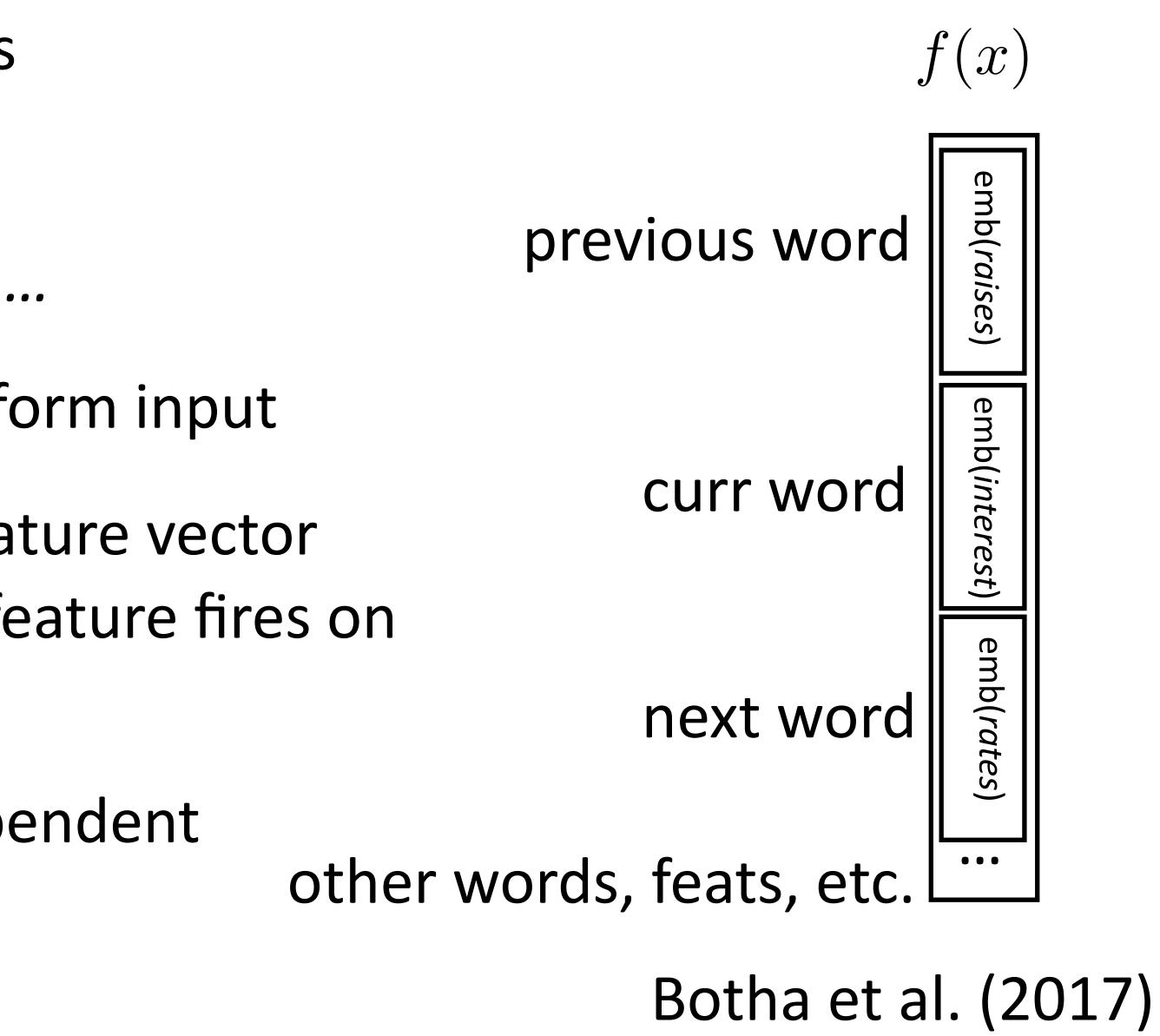
NLP with Feedforward Networks

Part-of-speech tagging with FFNNs

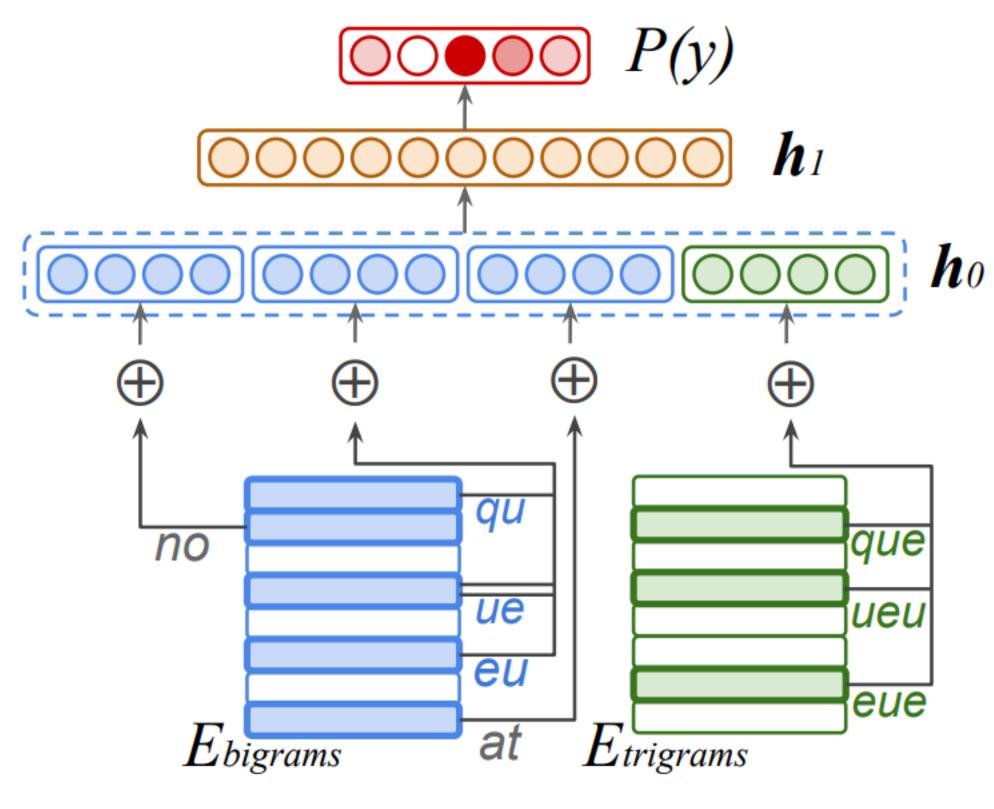
??

Fed raises interest rates in order to ...

- Word embeddings for each word form input
- ~1000 features here smaller feature vector than in sparse models, but every feature fires on every example
- Weight matrix learns position-dependent processing of the words



NLP with Feedforward Networks



There was no <u>queue</u> at the ...

Hidden layer mixes these different signals and learns feature conjunctions

Botha et al. (2017)



NLP with Feedforward Networks

Multilingual tagging results:

	Acc.			-
Gillick et al. (2016)	95.06	900k	-	6.63m
Small FF	94.76	241k	0.6	0.27m
+Clusters	95.56	261k	1.0	0.31m
$\frac{1}{2}$ Dim.	95.39	143k	0.7	6.63m 0.27m 0.31m 0.18m

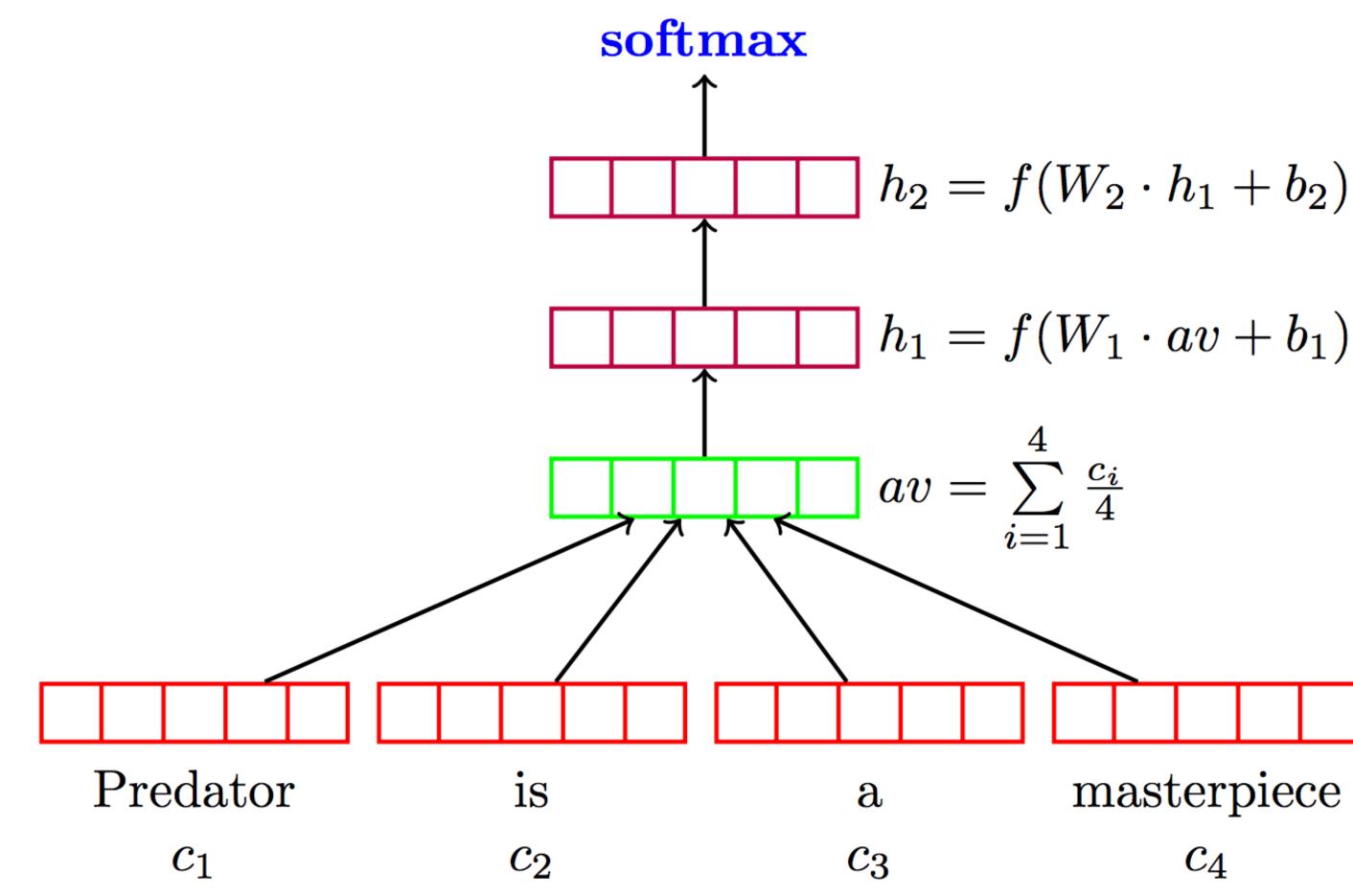
Gillick used LSTMs; this is smaller, faster, and better

Botha et al. (2017)



Sentiment Analysis

word embeddings from input



Deep Averaging Networks: feedforward neural network on average of

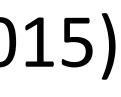
$$h_2 = f(W_2 \cdot h_1 + b_2)$$

$$h_1 = f(W_1 \cdot av + b_1)$$



Sentiment Analysis

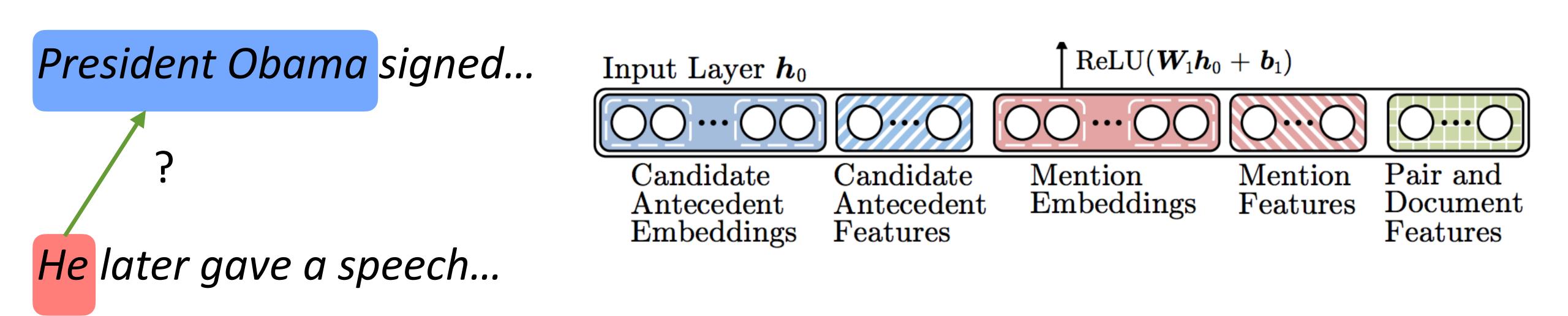
	Model	RT	SST	SST	IMDB	Time	
			fine	bin		(s)	
	DAN-ROOT		46.9	85.7		31	
	DAN-RAND	77.3	45.4	83.2	88.8	136	
	DAN	80.3	47.7	86.3	89.4	136	lyyer et al. (202
Bag-of-words {	NBOW-RAND	76.2	42.3	81.4	88.9	91	
	NBOW	79.0	43.6	83.6	89.0	91	
	BiNB		41.9	83.1			Wang and
	NBSVM-bi	79.4			91.2		Manning (2012
Tree RNNs / CNNS / LSTMS	RecNN*	77.7	43.2	82.4			· Manning (2012
	RecNTN*		45.7	85.4			
	DRecNN		49.8	86.6		431	
	TreeLSTM		50.6	86.9			
	DCNN*		48.5	86.9	89.4		
	PVEC*		48.7	87.8	92.6		
	CNN-MC	81.1	47.4	88.1		2,452	Kim (2014)
	WRRBM*				89.2		-
							_





Coreference Resolution

Feedforward networks identify coreference arcs

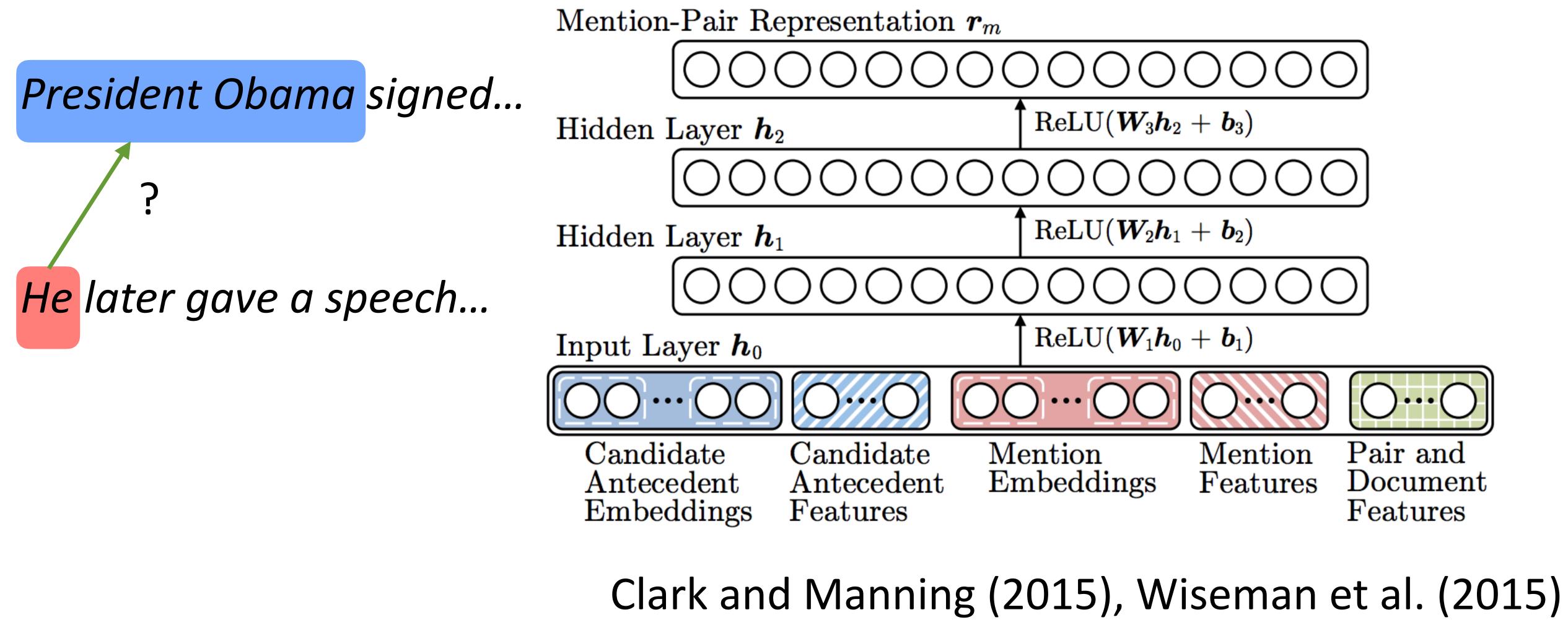


- Mention features include: type of mention (pronoun, nominal, proper), the mention's position in the article, length of the mention in words ...
 - Clark and Manning (2015), Wiseman et al. (2015)



Coreference Resolution

Feedforward networks identify coreference arcs







Coreference Resolution

Input Layer. For each mention, the model extracts various words and groups of words that are fed into the neural network. Each word is represented by a vector $\boldsymbol{w}_i \in \mathbb{R}^{d_w}$. Each group of words is represented by the average of the vectors of each word in the group. For each mention and pair of mentions, a small number of binary features and distance features are also extracted. Distances and mention lengths are binned into one of the buckets [0, 1, 2, 3, 4, 5-7, 8-15, 16-31, 32-63, 64+] and then encoded in a one-hot vector in addition to being included as continuous features. The full set of features is as follows:

Embedding Features: Word embeddings of the head word, dependency parent, first word, last word, two preceding words, and two following words of the mention. Averaged word embeddings of the five preceding words, five following

Clark and Manning (2015), Wiseman et al. (2015)

words, all words in the mention, all words in the mention's sentence, and all words in the mention's document.

Additional Mention Features: The type of the mention (pronoun, nominal, proper, or list), the mention's position (index of the mention divided by the number of mentions in the document), whether the mentions is contained in another mention, and the length of the mention in words.

Document Genre: The genre of the mention's document (broadcast news, newswire, web data, etc.).

Distance Features: The distance between the mentions in sentences, the distance between the mentions in intervening mentions, and whether the mentions overlap.

Speaker Features: Whether the mentions have the same speaker and whether one mention is the other mention's speaker as determined by string matching rules from Raghunathan et al. (2010).

String Matching Features: Head match, exact string match, and partial string match.



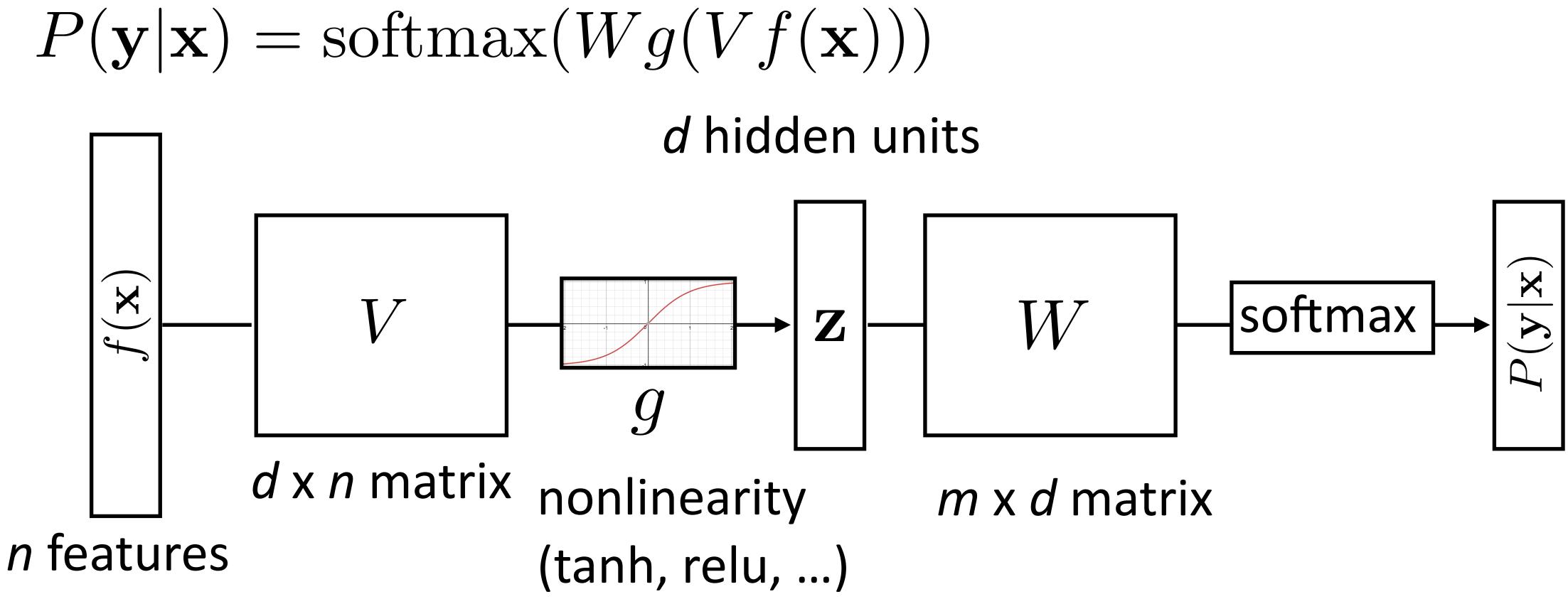
Training Tips

Training Basics

- Basic formula: compute gradients on batch, use first-order optimization method (SGD, Adagrad, etc.)
- How to initialize? How to regularize? What optimizer to use?
- This lecture: some practical tricks. Take deep learning or optimization courses to understand this further



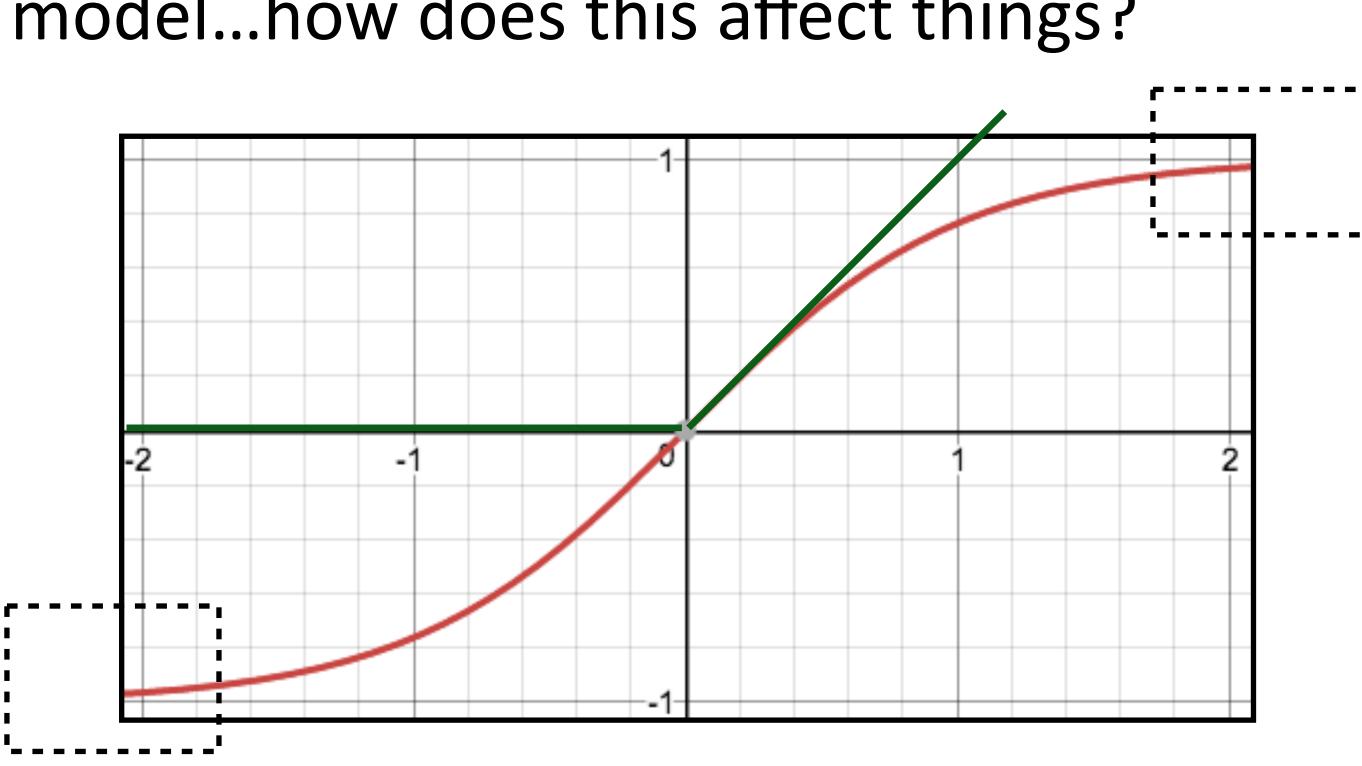
How does initialization affect learning?



- How do we initialize V and W? What consequences does this have?
- Nonconvex problem, so initialization matters!

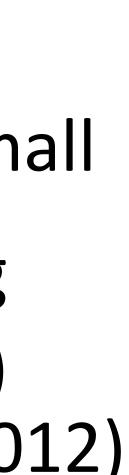
How does initialization affect learning?

Nonlinear model...how does this affect things?



- Tanh: If cell activations are too large in absolute value, gradients are small

ReLU: larger dynamic range (all positive numbers), but can produce big values, and can break down if everything is too negative ("dead" ReLU) Krizhevsky et al. (2012)

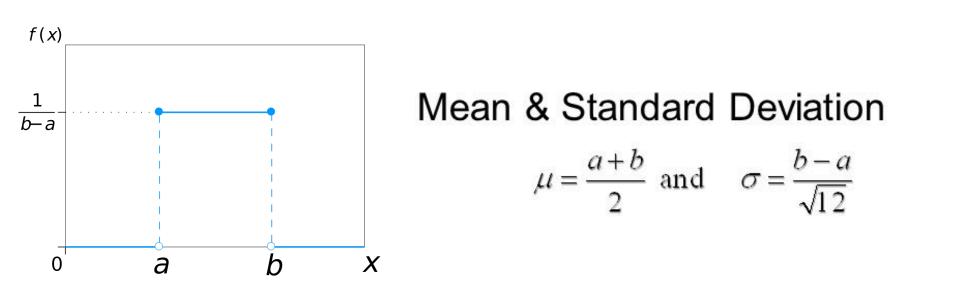


Initialization

1) Can't use zeroes for parameters to produce hidden layers: all values in that hidden layer are always the same (0 if tanh) and have same gradients (0 if tanh), and can't break symmetry (or never change)

- 2) Initialize too large and cells are saturated

Want variance of inputs and gradients for each layer to be the same



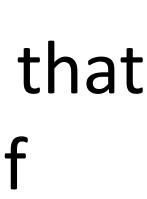
Maverick Meerkat's answer - https://stats.stackexchange.com/questions/27112/danger-of-setting-all-initial-weights-to-zero-in-backpropagation

Can do random uniform / normal initialization with appropriate scale

• Xavier initializer: $U \left[-\sqrt{\frac{6}{\text{fan-in} + \text{fan-out}}}, +\sqrt{\frac{6}{\text{fan-in} + \text{fan-out}}} \right]$

Glorot & Bengio (2010)

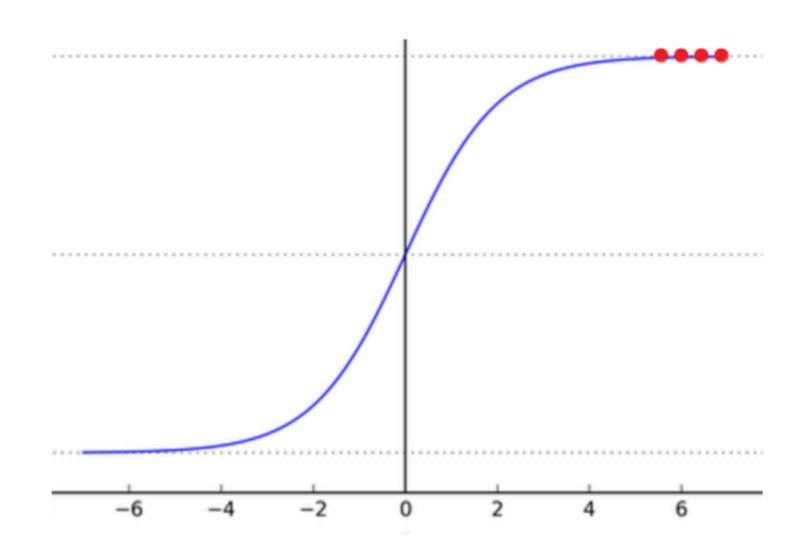
https://mmuratarat.github.io/2019-02-25/xavier-glorot-he-weight-init





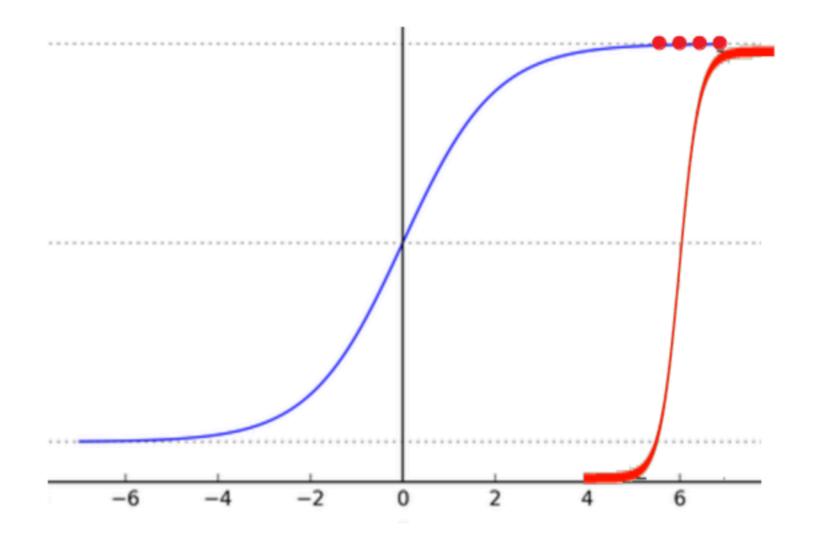


Batch Normalization



https://medium.com/@shiyan/xavier-initialization-and-batch-normalization-my-understanding-b5b91268c25c

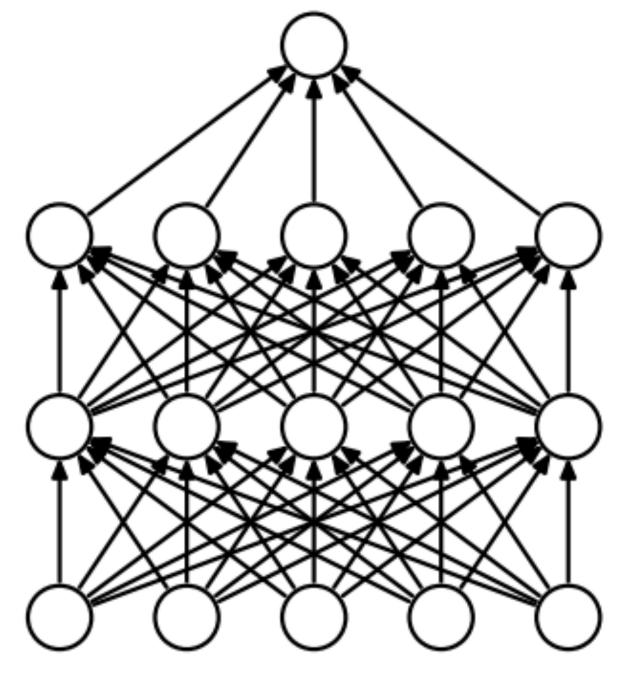
Batch normalization (loffe and Szegedy, 2015): periodically shift+rescale each layer to have mean 0 and variance 1 over a batch (useful if net is deep)





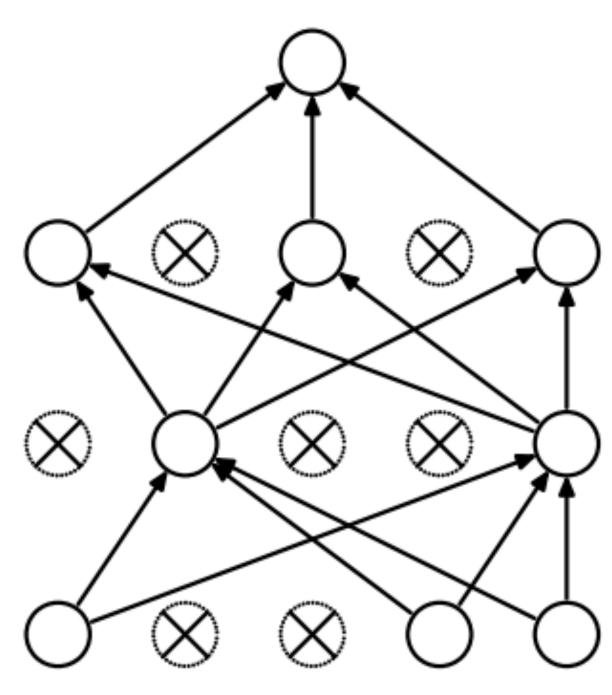
Regularization: Dropout

- Probabilistically zero out parts of the network during training to prevent overfitting, use whole network at test time
- Form of stochastic regularization
- Similar to benefits of ensembling: network needs to be robust to missing signals, so it has redundancy



One line in Pytorch/Tensorflow

(a) Standard Neural Net



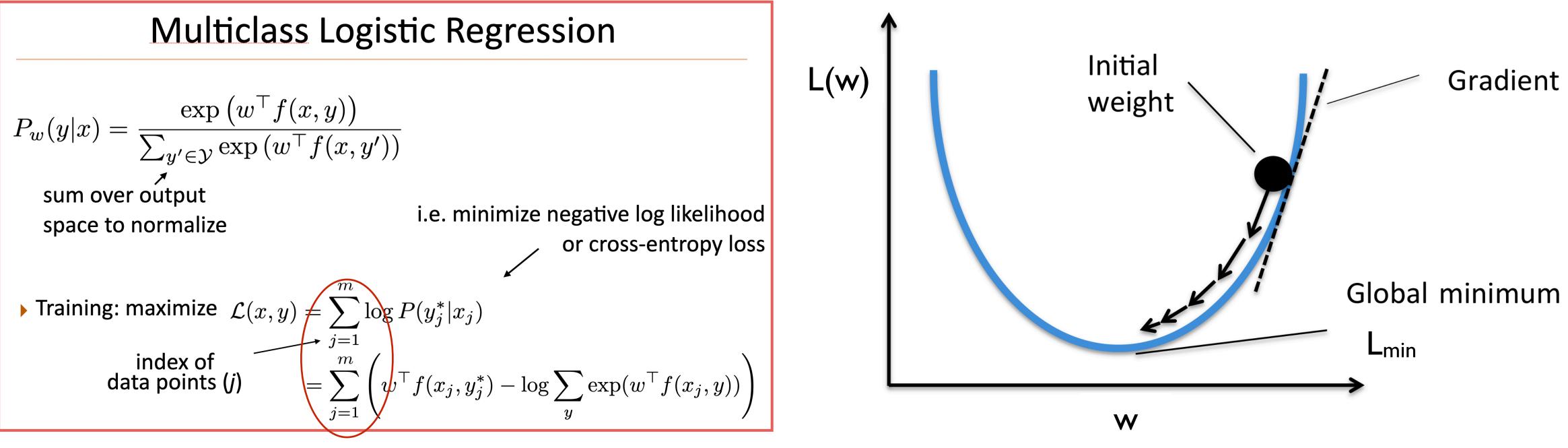
(b) After applying dropout.

Srivastava et al. (2014)



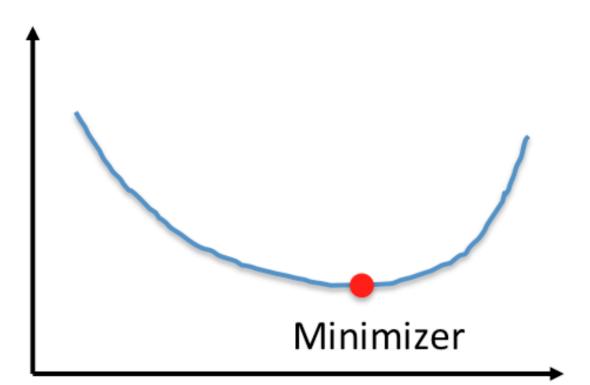
Optimization

- Gradient descent
 - **Batch update** for logistic regression
 - Each update is based on a computation over the entire dataset



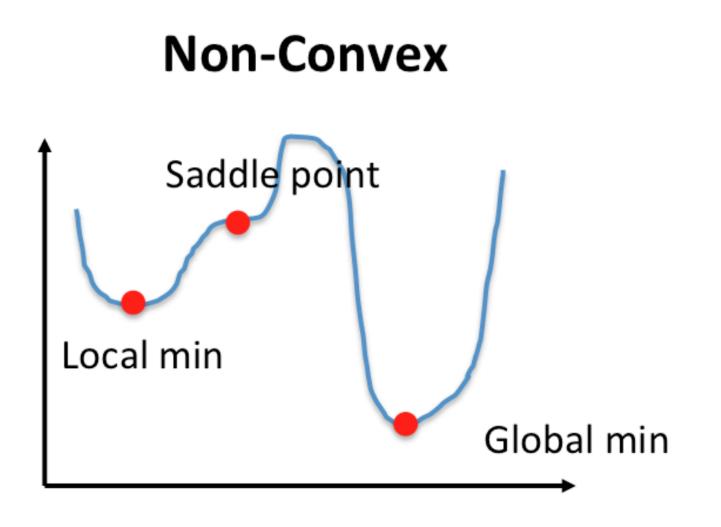
- Stochastic gradient descent
 - Approx. gradient is computed on a single instance
 - What if the loss function has a local minima or saddle point?

Convex



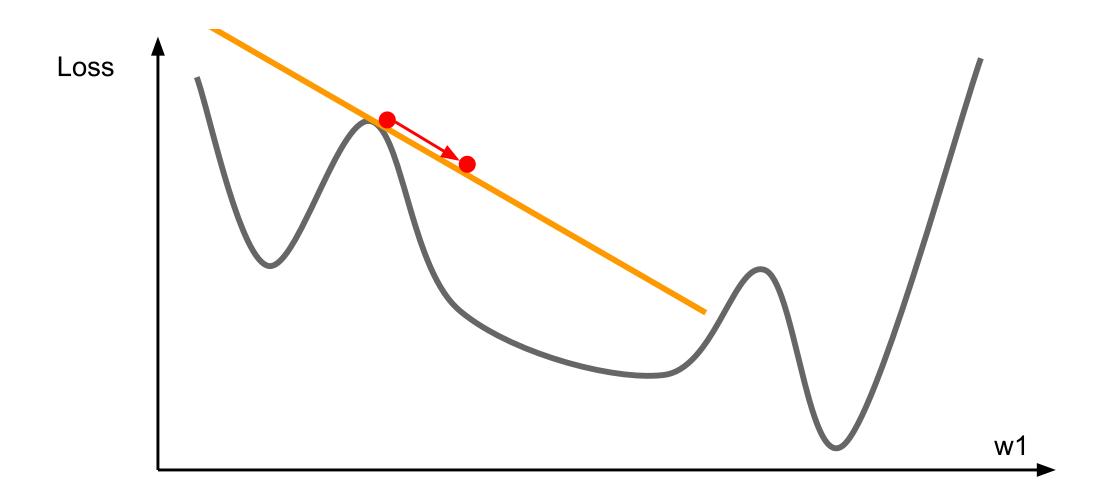
Optimization

$$w \leftarrow w - \alpha g, \quad g = \frac{\partial}{\partial w} \mathcal{L}$$



Dauphin et al. (2014) Image credit: Paweł Cislo

- Stochastic gradient descent
 - Approx. gradient is computed on a single instance "First-order" technique: only relies on having gradient



Optimization

$$w \leftarrow w - \alpha g, \quad g = \frac{\partial}{\partial w} \mathcal{L}$$

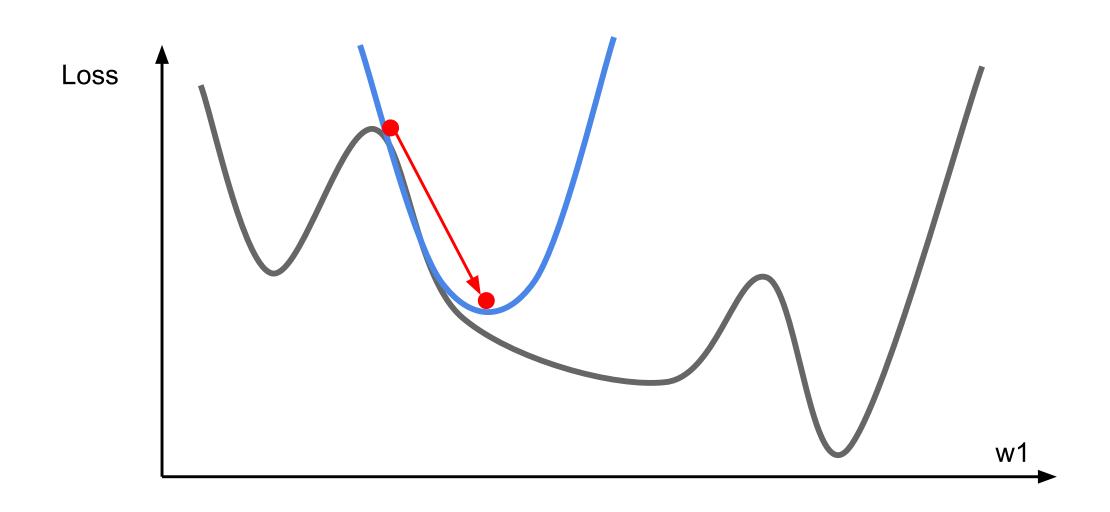


Image credit: Stanford CS231N



Momentum

Gradients come from a single instance or a mini-batchcan be noisy

Use "velocity" to accumulates the gradients from the past steps

Standard SGD

while True: $dx = compute_gradient(x)$ x += learning_rate * dx

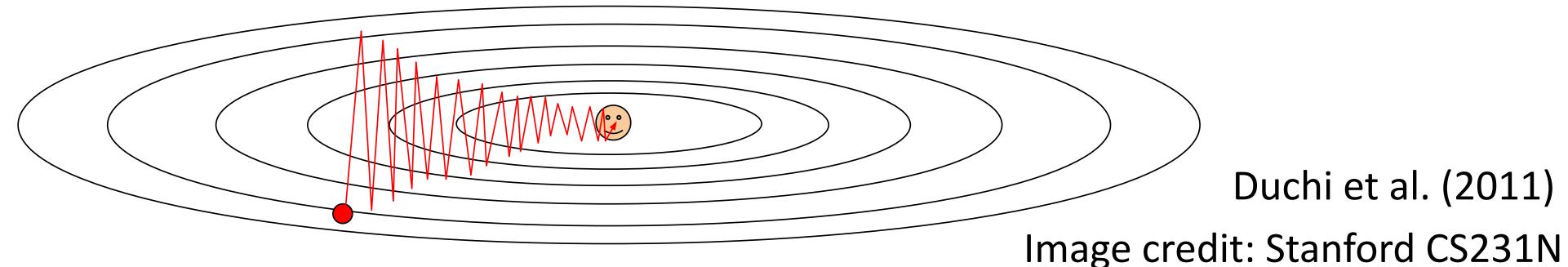
SGD with Momentum

```
VX = 0
while True:
  dx = compute_gradient(x)
  vx = rho * vx + dx
  x += learning_rate * vx
```

Polyak (1964), Sutskever et al. (2013) Image credit: Stanford CS231N

- Optimized for problems with sparse features
- that get updated frequently

```
grad_squared = 0
while True:
  dx = compute_gradient(x)
 grad_squared += dx * dx
 x -= learning_rate * dx / (np.sqrt(grad_squared) + 1e-7)
```



AdaGrad

Per-parameter learning rate: smaller updates are made to parameters

- Optimized for problems with sparse features
- that get updated frequently

$$w_i \leftarrow w_i + \alpha \frac{1}{\sqrt{\epsilon + \sum_{\tau=1}^t g_{\tau,i}^2}} g$$

Generally more robust than SGD, requires less tuning of learning rate

AdaGrad

Per-parameter learning rate: smaller updates are made to parameters

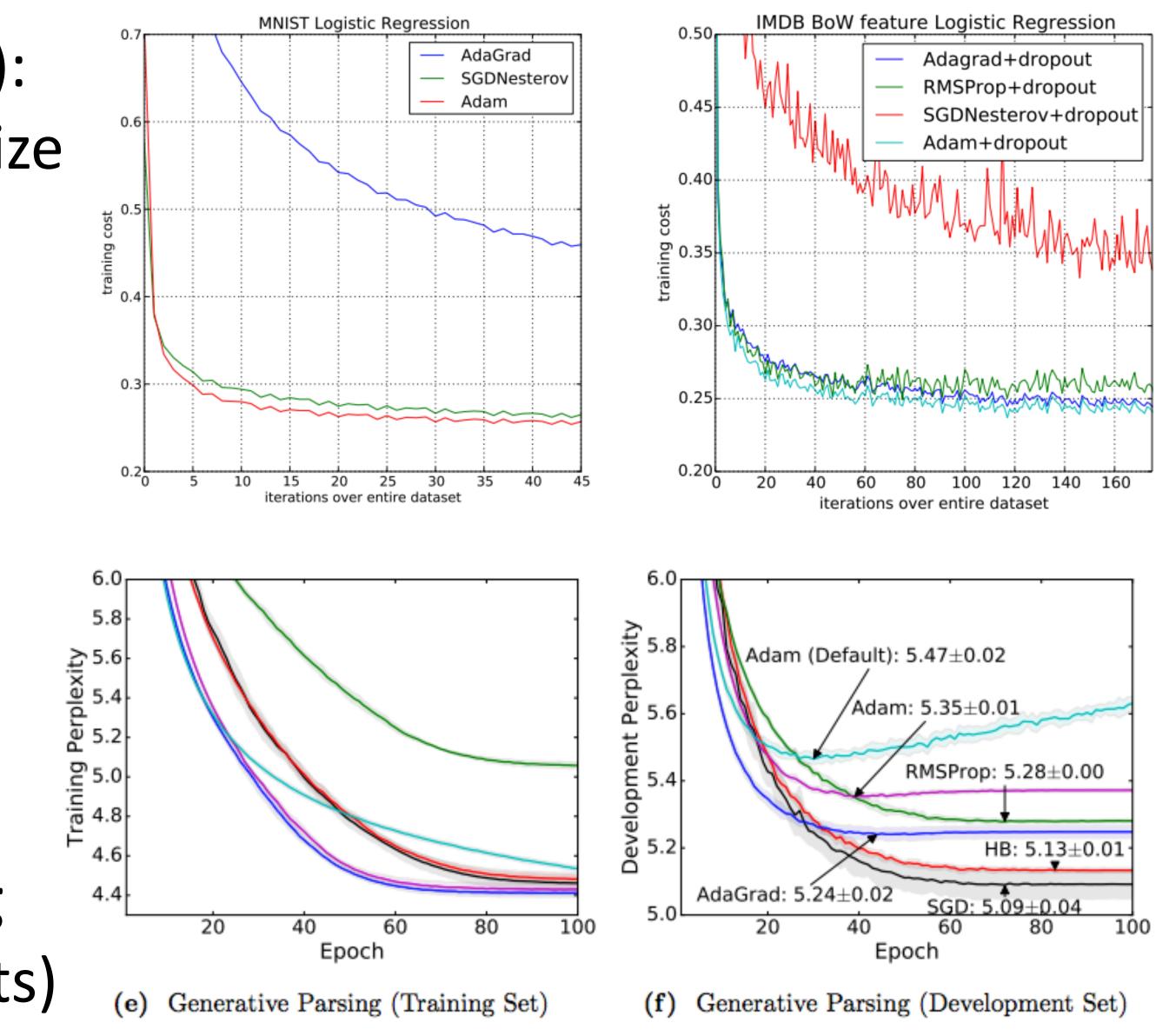
t_i (smoothed) sum of squared gradients from all updates

Duchi et al. (2011)

Optimizer

 Adam (Kingma and Ba, ICLR 2015): very widely used. Adaptive step size
 + momentum

- Wilson et al. NIPS 2017: adaptive methods can actually perform badly at test time (Adam is in pink, SGD in black)
- One more trick: gradient clipping
 (set a max value for your gradients)



- Computing gradients is hard!

$$y = x * x - (y, dy) = codegen$$

- Use a library like PyTorch or TensorFlow. This class: PyTorch

Computation Graphs

Automatic differentiation: instrument code to keep track of derivatives

(x * x, 2 * x * dx)

Computation is now something we need to reason about symbolically

Computation Graphs in Pytorch

• Define forward pass for $P(\mathbf{y}|\mathbf{x}) = \operatorname{softmax}(Wg(Vf(\mathbf{x})))$

class FFNN(nn.Module): def init (self, inp, hid, out): super(FFNN, self). init () self.V = nn.Linear(inp, hid) self.g = nn.Tanh()self.W = nn.Linear(hid, out) self.softmax = nn.Softmax(dim=0)

> def forward(self, x): return self.softmax(self.W(self.g(self.V(x))))



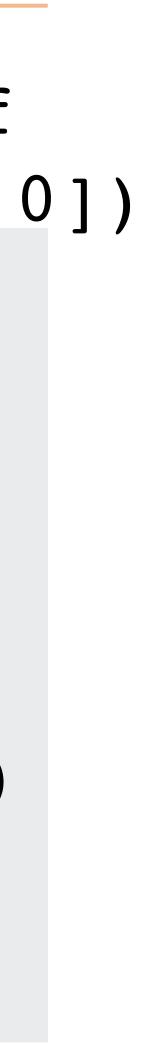
Computation Graphs in Pytorch

 $P(\mathbf{y}|\mathbf{x}) = \operatorname{softmax}(Wg(Vf(\mathbf{x})))$ ffnn = FFNN(in_d, hi_d, out_d) def make update(input, gold label): ffnn.zero grad() # clear gradient variables probs = ffnn.forward(input) loss.backward() optimizer.step()

 $\mathcal{L}(\mathbf{x}, i^*) = \log P(y = i^* | \mathbf{x}) = \log (\operatorname{softmax}(W\mathbf{z}) \cdot e_{i^*})$

- ei*: one-hot vector of the label(e.g.,[0, 1, 0])
- optimizer = optim.Adam(ffnn.parameters(), lr=0.01)

 - loss = torch.neg(torch.log(probs)).dot(gold label)



Training a Model

Define a computation graph For each epoch: For each batch of data: Compute loss on batch Autograd to compute gradients and take step Check performance on dev set periodically to identify overfitting

Batching (aka, mini-batch)

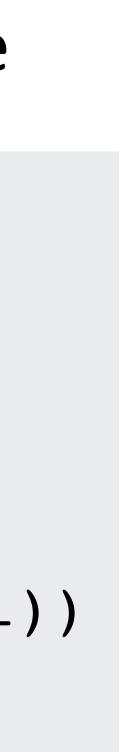
- Batching data gives speedups due to more efficient matrix operations
- Need to make the computation graph process a batch at the same time

input is [batch size, num feats] # gold label is [batch size, num classes] def make update(input, gold label)

• • •

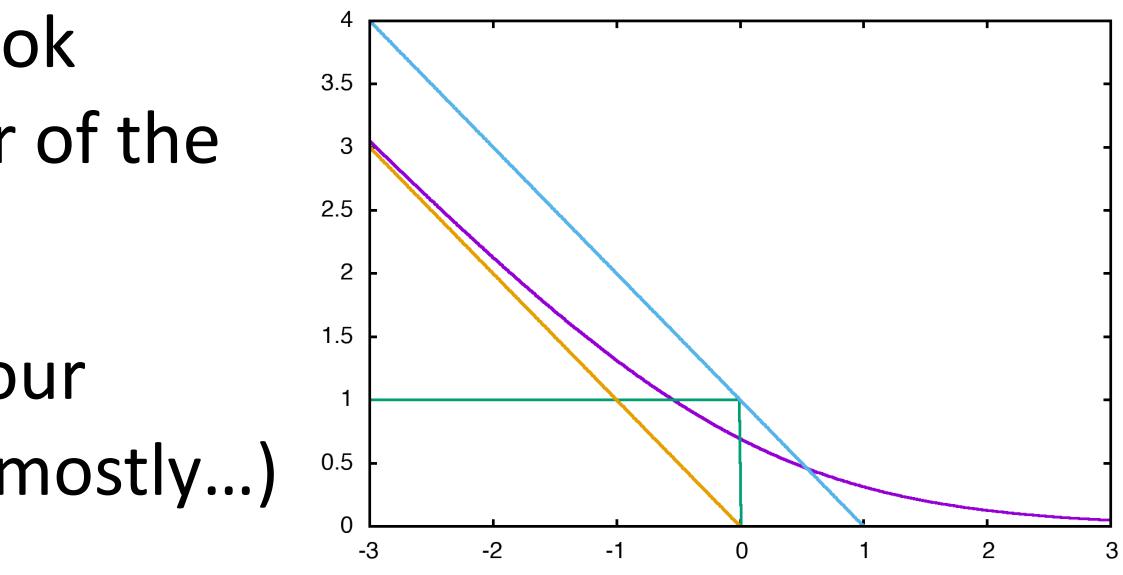
probs = ffnn.forward(input) # [batch size, num classes] loss = torch.sum(torch.neg(torch.log(probs)).dot(gold label))

Batch sizes from 1-100 often work well



- Model: feedforward, RNNs, CNNs can be defined in a uniform framework
- Objective: many loss functions look similar, just changes the last layer of the neural network
- Inference: define the network, your library of choice takes care of it (mostly...)
- Training: lots of choices for optimization/hyperparameters

Four Elements of NNs





- Word representations
- word2vec/GloVe
- Evaluating word embeddings

Next Up