

Perceptron

$$a = w^T x$$

$$= w_1 x_1 + w_2 x_2 + \dots + w_n x_n + \underbrace{w_0 x_0}_{\substack{|| \\ b \\ | \\ \text{"bias"}}$$

observe an example in training $(x, y) = 1$
model made a mistake, namely $a < 0$.

for simplicity
we suppose this is
a positive example

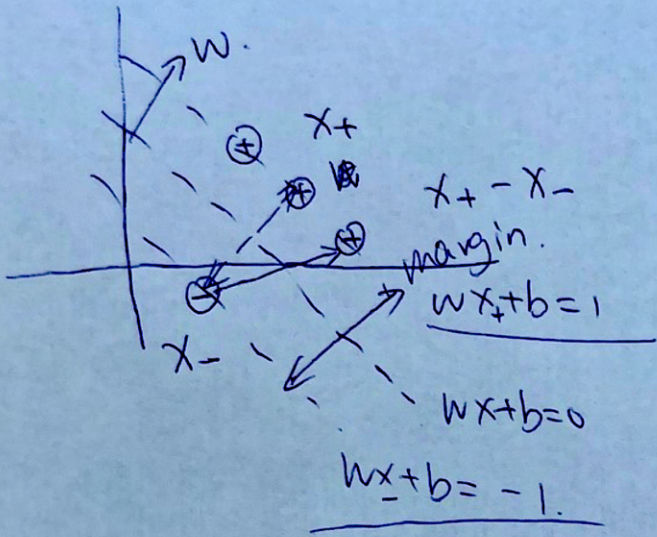
so, we make a update $w' = w + x$.

observe this example again

$$a' = w'^T x = (w + x)^T x = \underbrace{w^T x}_a + \underbrace{x^T x}_{\sum_{i=0}^n x_i^2} > a + 1$$

$x_0 = 1$

SVM



margin

$$= (x_+ - x_-) \cdot \frac{w}{\|w\|_2}$$

↑
unit vector.

$$= \frac{2}{\|w\|_2} \frac{w}{\|w\|_2}$$

~~margin~~

$$x_+ - x_- = \frac{2}{\|w\|_2}$$

$$= \frac{2}{\|w\|_2}$$

$$\begin{aligned} wx_+ + b &= 1 \\ wx_- + b &= -1 \end{aligned}$$

$$\sqrt{w_1^2 + w_2^2 + \dots + w_n^2}$$

$$w(x_+ - x_-) = 1 - b - (-1 - b) = 2$$