Large Language Models (part 4)

(Many slides from Greg Durrett, Daniel Khashabi, Tatsunori Hashimoto)

Wei Xu

Administrivia

- Practice Midterm is released
- ICE GPU cluster access is granted



Yang et al. (Apr. 2023)



Open-source Efforts

OPT: Open Pre-trained Transformer LMs

- GPT-3 models only released via API access.
- PALM not generally available outside Google
 - Doesn't support reproducible experiments.

OPT (125M-66B-175B), to roughly matches GPT-3, with parameters are shared with the research community



Across a variety of tasks and model sizes, OPT largely matches the reported averages of GPT-3. However, performance varies greatly per task: see Appendix A.

Zhang et al. (2022)



OPT: Open Pre-trained Transformer LMs

Includes 114 page logbook for training 175B model, interesting read

```
2021-11-16 11pm [Myle]: Run 12.08
     Previous run failed with mysterious error: "p2p_plugin.c:141 NCCL WARN NET/IB : Got async event :
      port error"

   New log file:

      /shared/home/namangoyal/checkpoints/175B/175B run12.08.me fp16.fsdp.gpf32.0.relu.transformer I
      m_megatron.nlay96.emb12288.lrnpos.0emb_scale.bm_none.tps2048.gpt2.adam.b2_0.95.eps1e-08.cl1
      .0.lr0.00012.endlr6e-06.wu2000.dr0.1.atdr0.1.0emb_dr.wd0.1.ms8.uf1.mu143052.s1.ngpu992/train.log
CKPT_DIR=/data/users/myleott/175B_run12.07.me_fp16.fsdp.gpf32.0.relu.transformer_lm_megatron.nlay96.emb12288.lrnp
os.0emb_scale.bm_none.tps2048.gpt2.adam.b2_0.95.eps1e-08.cl1.0.lr0.00012.endlr6e-06.wu2000.dr0.1.atdr0.1.0emb_dr.
wd0.1.ms8.uf1.mu143052.s1.ngpu992
BLOB_URL="<<<SCRUBBED FOR RELEASE>>>"
cd $CKPT_DIR
cp --recursive --include-pattern "checkpoint_5_13250*.pt" "$BLOB_URL" checkpoint_5_13250
export RESTORE_FILE=$CKPT_DIR/checkpoint_5_13250/checkpoint_5_13250.pt
export RUN_ID=175B_run12.08
INCLUDED_HOSTS=node-[1-38,40-89,91-94,96-119,121-128] \
   python -m fb_sweep.opt.sweep_opt_en_lm_175b \
    -n 124 -g 8 -t 1 \
    -p $RUN_ID \
     -checkpoints-dir /shared/home/namangoyal/checkpoints/175B/ \
    --restore-file $RESTORE_FILE
After Launch:
sudo scontrol update job=1394 TimeLimit=UNLIMITED
sudo scontrol update job=1394 MailUser=<scrubbed> MailType=ALL
```

Considerations for Release 6

Following the recommendations for individual researchers generated by the Partnership for AI,⁷ along with the governance guidance outlined by NIST,⁸ we are disclosing all of the details involved in training OPT-175B through our logbook,⁹ our code, and providing researchers access to model weights for OPT-175B, along with a suite of smaller baselines mirroring the setup for OPT-175B. We aim to be fully accountable for the development lifecycle of OPT-175B, and only through increasing transparency around LLM development can we start understanding the limitations and risks of LLMs before broader deployment occurs.

By sharing a detailed account of our day-to-day training process, we disclose not only how much compute was used to train the current version of OPT-175B, but also the human overhead required when underlying infrastructure or the training process itself becomes unstable at scale. These details

Zhang et al. (2022)



- 59 languages (46 natural language + 13 programming language)
- 1.6TB of pre-processed text

Code - 10.8%

Indic family - 4.4%

Portuguese - 4.9%

Arabic - 4.6% Chinese (Traditional) - 0.05%

Chinese (Simplified) - 16.2%

Niger-Congo Family - 0.03%

Bloom

A BigScience initiative, open-access, 176B parameter (GPT-2 architecture)



https://huggingface.co/bigscience/bloom





- Released by Meta Al on Feb 27, 2023

			-			
params	dimension	n heads	n layers	learning rate	batch size	n tokens
6.7B	4096	32	32	$3.0e^{-4}$	4M	1.0T
13.0B	5120	40	40	$3.0e^{-4}$	4M	1.0T
32.5B	6656	52	60	$1.5e^{-4}$	4M	1.4T
65.2B	8192	64	80	$1.5e^{-4}$	4M	1.4T

Table 2: Model sizes, architectures, and optimization hyper-parameters.

LLaMA

Weights of all models are publicly available (non-commercial license)



Figure 1: Training loss over train tokens for the 7B, 13B, 33B, and 65 models. LLaMA-33B and LLaMA-65B were trained on 1.4T tokens. The smaller models were trained on 1.0T tokens. All models are trained with a batch size of 4M tokens.

- Trained only on publicly available
 - English CommonCrawl
 - C4 (another CommonCrawl data
 - GitHub (from Google BigQuery)
 - Wikipedia of 20 languages,
 - Gutenberg and Books3 (from ThePile)
 - ArXiv (latex files)
 - StackExchange.
- Split all numbers into individual digits, and fall back to bytes for unknown UTF-8 characters

LLaMA

e data:	Dataset	Sampling prop.	Epochs	Disk
	CommonCraw	l 67.0%	1.10	3.3
	C4	15.0%	1.06	783
	Github	4.5%	0.64	328
asel)	Wikipedia	4.5%	2.45	83
	Books	4.5%	2.23	85
)	ArXiv	2.5%	1.06	92
	StackExchange	e 2.0%	1.03	78

Table 1: Pre-training data. Data mixtures used for pretraining, for each subset we list the sampling proportion, number of epochs performed on the subset when training on 1.4T tokens, and disk size. The pre-training runs on 1T tokens have the same sampling proportion.

LLaMA-13B matches and outperforms OPT and (old) GPT-3 for zero-shot and few-shot performance

		BoolQ	PIQA	SIQA	HellaSwag	WinoGrande	ARC-e	ARC-c	OBQA			0-shot	1-shot	5-shot	64-:
GPT-3	175B	60.5	81.0	_	78.9	70.2	68.8	51.4	57.6	GPT-3	175B	14.6	23.0	-	29
Gopher	280B	79.3	81.8	50.6	79.2	70.1	-	-	-	Gopher	280B	10.1	-	24.5	28
Chinchilla	70B	83.7	81.8	51.3	80.8	74.9	-	-	-	Chinchill	a 70B	16.6	-	31.5	35
PaLM	62B	84.8	80.5	-	79.7	77.0	75.2	52.5	50.4		8B	8.4	10.6	_	14
PaLM-cont	62B	83.9	81.4	-	80.6	77.0	-	-	-	PaLM	62B	18.1	26.5	-	27
PaLM	540B	88.0	82.3	-	83.4	81.1	76.6	53.0	53.4		540B	21.2	29.3	-	39
	7B	76.5	79.8	48.9	76.1	70.1	72.8	47.6	57.2		7B	16.8	18 7	22.0	26
ΤΤοΜΑ	13 B	78.1	80.1	50.4	79.2	73.0	74.8	52.7	56.4		13B	20.1	23.4	28.1	31
LLaMA	33B	83.1	82.3	50.4	82.8	76.0	80.0	57.8	58.6	LLaMA	33B	20.1 24.9	28.3	32.9	36
	65B	85.3	82.8	52.3	84.2	77.0	78.9	56.0	60.2		65B	23.8	31.0	35.0	39

Table 3: Zero-shot performance on Common Sense Reasoning tasks.

LLaMA

Table 4: NaturalQuestions. Exact match performance.

Transformer variations that have been used in different LLMs

Transformer

LLaMA

Image Credit: Rajesh Kavadiki

LLaMA

- Transformer variations that have been used in different LLMs
- Pre-normalization layer using RMSNorm
- SwiGLU activation function combines Swish and Gated Linear Unit (GLU), also used in Google's PaLM model
- Rotary positional embeddings (RoPE)
- AdamW Optimizer

Transformer Variants

Fig. 3. Taxonomy of Transformers

Positional Embeddings LayerNorm

3 main types: encoder, decoder, enc-dec

Lin et al. (2021)

Normalization

Original Transformer — "Add" before "Norm", or "Norm" before "Add"?

LayerNorm(x + SubLayer(x))

or

x + SubLayer(LayerNorm(x))

(Baevski & Auli, 2018; Child et al., 2019; Wang et al., 2019)

Pre-normalization Transformer (b) to have better-behaved gradients at initialization than in the original Transformer (a)

- Pre-normalization Transformer (b) to have better-behaved gradients at initialization than in the original Transformer (a)
- In (b), LayerNorm does not disrupt residual

Post-norm produces noisy gradients with many tall spikes, needs warm up Pre-norm has fewer noisy gradients with smaller sizes, even without warmup

Nguyen & Salazar (2019)

RMSNorm (a) instead of standard LayerNorm (b)

(used in LLaMA1/2/3, PaLM, T5 ...)

(used in GPT1/2/3, OPT ...) Zhang and Sennrich (2019)

RMSNorm (a) instead of standard LayerNorm (b)

more computationally efficient

Zhang and Sennrich (2019)

RMSNorm (a) instead of standard LayerNorm (b)

more computationally efficient ??

Zhang and Sennrich (2019)

more computationally efficient ??

Matrix multiplications make up the majority of GPU FLOPs (and memory) Below is runtime analysis of the encoder layer of (Transformer-based) BERT

Table 1. Proportions for operator classes in PyTorch.

or class	% flop	% Runtime
sor contraction	99.80	61.0
normalization	0.17	25.5
nent-wise	0.03	13.5

biases, dropout, activations, and residual connections

Ivanov et al. (2021)

Yet, RMSNorm runtime gains have been observed in papers

Model	Params	\mathbf{Ops}	Step/s	Early loss	Final loss	SGLUE	XSum	$\mathbf{Web}\mathbf{Q}$	WMT EnDe
Vanilla Transformer	223M	11.1T	3.50	2.182 ± 0.005	1.838	71.66	17.78	23.02	26.62
RMS Norm	223M	11.1T	3.68	2.167 ± 0.008	1.821	75.45	17.94	24.07	27.14

more computationally efficient ??

Narang et al. (2021)

Model	Params	Ops	Step/s	Early loss	Final loss	SGLUE	XSum	WebQ	WMT EnDe
Vanilla Transformer	223M	11.1T	3.50	2.182 ± 0.005	1.838	71.66	17.78	23.02	26.62
GeLU	223M	11.1T	3.58	2.179 ± 0.003	1.838	75.79	17.86	25.13	26.47
Swish	223M	11.1T 11.1T	3.62	2.186 ± 0.003	1.847	73.77	17.74	24.34	26.75
ELU	223M	11.1T	3.56	2.270 ± 0.007	1.932	67.83	16.73	23.02	26.08
GLU	223M	11.1T	3.59	2.174 ± 0.003	1.814	74.20	17.42	24.34	27.12
GeGLU	223M	11.1T	3.55	2.130 ± 0.006	1.792	75.96	18.27	24.87	26.87
ReGLU	223M	11.1T	3.57	2.145 ± 0.004	1.803	76.17	18.36	24.87	27.02
SeLU	223M	11.1T	3.55	2.315 ± 0.004	1.948	68.76	16.76	22.75	25.99
SwiGLU	223M	11.1T	3.53	2.127 ± 0.003	1.789	76.00	18.20	24.34	27.02
LiGLU	223M	11.1T	3.59	2.149 ± 0.005	1.798	75.34	17.97	24.34	26.53
Sigmoid	223M	11.1T	3.63	2.291 ± 0.019	1.867	74.31	17.51	23.02	26.30
Softplus	223M	11.11	3.47	2.207 ± 0.011	1.850	72.45	17.05	24.34	26.89
RMS Norm	223M	11.1T	3.68	2.167 ± 0.008	1.821	75.45	17.94	24.07	27.14
Rezero	223M 222M	11.1T 11.1T	3.51 2.96	2.262 ± 0.003	1.939	01.09 70.49	15.64	20.90	26.37
Rezero + LayerNorm	223M 222M	11.1I 11.1T	3.20 2.24	2.223 ± 0.000 2.221 ± 0.000	1.838 1.875	70.42 70.22	17.08 17.20	23.02	20.29
Fixup	223M 223M	11.11 11.1T	$\begin{array}{c} 0.04 \\ 0.05 \end{array}$	2.221 ± 0.009 2.382 ± 0.012	1.875 2.067	70.55 58 56	17.32	23.02	20.19
24 large d 1520 U C	00414	11 177	2.90	2.002 ± 0.012	1.049	74.00	17.74	20.02	20.01
24 layers, $d_{\rm ff} = 1536, H = 6$	224 <i>M</i> 22214	11.1T 11.1T	3.33	2.200 ± 0.007	1.843	74.89	17.75	25.13	26.89
10 layers, $a_{\rm ff} = 2048$, $H = 8$	4431VI 2221M	11.11 11.1T	3.38 2.60	2.100 ± 0.005 2.100 ± 0.005	1.831 1.947	10.45 71 50	10.83 17 60	⊿4. 34 วହ วอ	21.10 26.85
8 layers, $a_{\rm ff} = 4008$, $H = 18$ 6 layers, $d_{\rm ff} = 6144$, $H = 24$	223M 223M	11.11 11.1T	3.09	2.190 ± 0.003 2.201 ± 0.010	1.047 1.857	73.55	17.09 17.50	20.20 24.60	20.85
0 layers, $a_{\rm ff} = 0144$, $II = 24$	2231/1	11.11	0.10	2.201 ± 0.010	1.007	10.00	11.09	24.00	20.00
Block sharing	65M	11.1T	3.91	2.497 ± 0.037	2.164	64.50	14.53	21.96	25.48
+ Factorized embeddings	45M	9.4T	4.21	2.631 ± 0.305	2.183	60.84	14.00	19.84	25.27
+ Factorized & snared em-	201 <i>M</i>	9.11	4.37	2.907 ± 0.313	2.380	53.95	11.37	19.84	25.19
Encoder only block sharing	170M	$11 \ 1T$	3 68	2.298 ± 0.023	1 929	69.60	16 23	23 02	26 23
Decoder only block sharing	144M	11.1T 11.1T	3.70	2.250 ± 0.029 2.352 ± 0.029	2.082	67.93	16.20 16.13	23.81	26.08
	00714	0.477	2.00		1.002	70.41	15.00	00.75	20.00
Factorized Embedding	227M	9.4T	3.80	2.208 ± 0.006 2.200 ± 0.010	1.855 1.052	70.41 68.60	15.92 16.22	22.75	26.50
dings	Z0ZM	9.11	5.92	2.320 ± 0.010	1.952	08.09	10.35	22.22	20.44
Tied encoder/decoder in-	248M	$11 \ 1T$	355	2.192 ± 0.002	1 840	71.70	17.72	24.34	26 49
put embeddings	210101	11.11	0.00	2.102 ± 0.002	1.010	11110	11112	- 110 1	20.10
Tied decoder input and out-	248M	11.1T	3.57	2.187 ± 0.007	1.827	74.86	17.74	24.87	26.67
put embeddings									
Untied embeddings	273M	11.1T	3.53	2.195 ± 0.005	1.834	72.99	17.58	23.28	26.48
Adaptive input embeddings	204M	9.2T	3.55	2.250 ± 0.002	1.899	66.57	16.21	24.07	26.66
Adaptive softmax	204M	9.2T	3 60	2.364 ± 0.005	1 982	72.91	16 67	21.16	25 56
Adaptive softmax without	223M	10.8T	3.43	2.229 ± 0.009	1.914	71.82	17.10	23.02	25.72
projection			0.10	0 0.000	1.011				
Mixture of softmaxes	232M	16.3T	2.24	2.227 ± 0.017	1.821	76.77	17.62	22.75	26.82
Transparent attention	223M	11 1 <i>T</i>	3 33	2.181 ± 0.014	1 874	54 31	10.40	21 16	26.80
Dynamic convolution	257M	11.8T	2.65	2.403 ± 0.009	2.047	59.01	12.67	21.10 21.16	17 03
Lightweight convolution	224M	10.4T	4.07	2.370 ± 0.010	1.989	63.07	14.86	23.02	24.73
Evolved Transformer	217M	9.9T	3.09	2.220 ± 0.003	1.863	73.67	10.76	24.07	26.58
Synthesizer (dense)	224M	11.4T	3.47	2.334 ± 0.021	1.962	61.03	14.27	16.14	26.63
Synthesizer (dense plus)	243M	12.6T	3.22	2.191 ± 0.010	1.840	73.98	16.96	23.81	26.71
Synthesizer (dense plus al-	243M	12.6T	3.01	2.180 ± 0.007	1.828	74.25	17.02	23.28	26.61
pha)									
Synthesizer (factorized)	207M	10.1T	3.94	2.341 ± 0.017	1.968	62.78	15.39	23.55	26.42
Synthesizer (random)	254M	10.1T	4.08	2.326 ± 0.012	2.009	54.27	10.35	19.56	26.44
Synthesizer (random plus)	292M	12.0T	3.63	2.189 ± 0.004	1.842	73.32	17.04	24.87	26.43
Synthesizer (random plus	292M	12.0T	3.42	2.186 ± 0.007	1.828	75.24	17.08	24.08	26.39
alpha)				a 16 a 1 a			.	.	
Universal Transformer	84M	40.0T	0.88	2.406 ± 0.036	2.053	70.13	14.09	19.05	23.91
Mixture of experts	648M	11.7T	3.20	2.148 ± 0.006	1.785	74.55	18.13	24.08	26.94
Switch Transformer	1100M	11.7T	3.18	2.135 ± 0.007	1.758	75.38	18.02	26.19	26.81
Funnel Transformer	223M	1.9T	4.30	2.288 ± 0.008	1.918	67.34	16.26	22.75	23.20
Weighted Transformer	280 <i>M</i>	71.0T	0.59	2.378 ± 0.021	1.989	69.04	16.98	23.02	26.30
Product key memory	421M	386.67	0.25	2.155 ± 0.003	1.798	75.16	17.04	23.55	26.73

Table 1: Results for all architecture variants. The baseline model is the vanilla Transformer with relative attention. The early loss represents the mean and standard deviation of perplexity at 65,536 steps. The final perplexity is reported at the end of pre-training (524, 288 steps). SGLUE refers to SuperGLUE and WebQ refers to WebQuestions dataset. We report average, ROUGE-2, accuracy, and BLEU score for SuperGLUE, XSum, WebQuestions, and WMT EnDe, respectively, on the validation sets. Note: Results on WMT English to German are reported without any pre-training. The scores which outperform the vanilla Transformer are highlighted in **boldface**.

Narang et al. (2021)

Bias Term

Standard feedforward network layer:

$$FFN(x, W_1, W_2, b_1, b_2) = f(xW_1 + b_1)W_2 + b_2$$

- Original Transformer uses ReLU as activation function $FFN(x, W_1, W_2, b_1, b_2) = max(0, xW_1 + b_1)W_2 + b_2$
- Many implementations (if they are not gated), e.g. T5, PaLM, DALL-E-mini ... $FFN_{ReLU}(x, W_1, W_2) = max(xW_1, 0)W_2$

Geiping & Goldstein (2022)

- Basically everyone does pre-norm Intuition: keep the good parts of residual connections – Observations: nicer gradient propagation, fewer spike
- Most people do RMSnorm
 - In practice, works as well as LayerNorm
- People more generally drop bias terms - since the compute/param tradeoffs are not great. – without compromising performance

Recap so far ...

– But, has fewer parameters to move around, saves on wallclock time

Activation Function

Activation Functions

A lot different ones used in training LLMs:

ReLU, GeLU, Swish, ELU, GLU, GeGLU, ReGLU, SeLU, SwiGLU, LiGLU, ...

Not much consensus ...

Image Credit: <u>ml-explained.com</u>

- also used in Google's PaLM model
- $FFN_{ReLU}(x, W_1, W_2) = max(xW_1, 0)W_2$
- Replace ReLU by Swish: $FFN_{Swish}(x, W_1, W_2) = Swish_1(xW_1)W_2$

SwiGLU in LLaMA

SwiGLU activation function — combines Swish and Gated Linear Unit (GLU),

Feedforward layer in the Transformer using ReLU (with no bias shown here):

Shazeer (2020)

https://medium.com/@tariqanwarph/activation-function-and-glu-variants-for-transformer-models-a4fcbe85323f

Swish Activation

Swish can be loosely viewed as a smooth function which nonlinearly interpolates between the linear function and ReLU

$Swish_{\beta}(x) = x * sigmoid(\beta x)$ $= \frac{x}{1+e^{-\beta x}}$

Ramachandran et al. (2017)

Gated Linear Unit (GLU)

- Similar to the gating mechanism in LSTM.
- Element-wise product of two linear transformations of the input, one is sigmoid-activated.

$\operatorname{GLU}(x, W, V, b, c) = \sigma(xW + b) \otimes (xV + c)$

Dauphin et al. (2017)

Sigmoid of a Vector

Image Credit: Gabriel Furnieles

SwiGLU

SwiGLU activation function — combines Swish and Gated Linear Unit (GLU), also used in Google's PaLM model

$\operatorname{GLU}(x, W, V, b, c) = \sigma(xW + b) \otimes (xV + c)$

 $\operatorname{SwiGLU}(x, W, V, b, c, \beta) = \operatorname{Swish}_{\beta}(xW + b) \otimes (xV + c)$

Dauphin et al. (2017)

- SwiGLU activation function combines Swish and Gated Linear Unit (GLU), also used in Google's PaLM model
- Feedforward layer in the Transformer using ReLU (with no bias shown here): $FFN_{ReLU}(x, W_1, W_2) = \max(xW_1, 0)W_2$
- Replace ReLU by Swish or SwiGLU: $\operatorname{FFN}_{\operatorname{Swish}}(x, W_1, W_2) = \operatorname{Swish}_1(xW_1)W_2$ $\text{FFN}_{\text{SwiGLU}}(x, W, V, W_2) = (\text{Swish}_1(xW) \otimes xV)W_2$ Shazeer (2020)

SwiGLU in LLaMA

https://medium.com/@tariqanwarph/activation-function-and-glu-variants-for-transformer-models-a4fcbe85323f

SwiGLU activation function — combines Swish and Gated Linear Unit (GLU), also used in Google's PaLM model

Training Steps	$65,\!536$	$524,\!288$
$FFN_{ReLU}(baseline)$	1.997~(0.005)	1.677
$\mathrm{FFN}_{\mathrm{GELU}}$	$1.983\ (0.005)$	1.679
$\mathrm{FFN}_{\mathrm{Swish}}$	1.994~(0.003)	1.683
$\mathrm{FFN}_{\mathrm{GLU}}$	$1.982 \ (0.006)$	1.663
$\mathrm{FFN}_{\mathrm{Bilinear}}$	$1.960\ (0.005)$	1.648
$\mathrm{FFN}_{\mathrm{GEGLU}}$	$1.942\ (0.004)$	1.633
$\mathrm{FFN}_{\mathrm{SwiGLU}}$	$1.944 \ (0.010)$	1.636
$\mathrm{FFN}_{\mathrm{ReGLU}}$	$1.953\ (0.003)$	1.645

LLaMA

Held-out log-perplexity on C4 corpus (used in T5 model)

Shazeer (2020)

https://medium.com/@tariqanwarph/activation-function-and-glu-variants-for-transformer-models-a4fcbe85323f
Gated Linear Unit (GLU)

GLU variants generally works pretty well

Model	Params	Ops	Step/s	Early loss	Final loss	SGLUE	XSum	WebQ
Vanilla Transformer	223M	11.1T	3.50	2.182 ± 0.005	1.838	71.66	17.78	23.02
GeLU	223M	11.1T	3.58	2.179 ± 0.003	1.838	75.79	17.86	25.13
Swish	223M	11.1T	3.62	2.186 ± 0.003	1.847	73.77	17.74	24.34
ELU	223M	11.1T	3.56	2.270 ± 0.007	1.932	67.83	16.73	23.02
GLU	223M	11.1T	3.59	2.174 ± 0.003	1.814	74.20	17.42	24.34
GeGLU	223M	11.1T	3.55	2.130 ± 0.006	1.792	75.96	18.27	24.87
ReGLU	223M	11.1T	3.57	2.145 ± 0.004	1.803	76.17	18.36	24.87
SeLU	223M	11.1T	3.55	2.315 ± 0.004	1.948	68.76	16.76	22.75
SwiGLU	223M	11.1T	3.53	2.127 ± 0.003	1.789	76.00	18.20	24.34
LiGLU	223M	11.1T	3.59	2.149 ± 0.005	1.798	75.34	17.97	24.34
Sigmoid	223M	11.1T	3.63	2.291 ± 0.019	1.867	74.31	17.51	23.02
Softplus	223M	11.1T	3.47	2.207 ± 0.011	1.850	72.45	17.65	24.34

Narang et al. (2021)

Sine embeddings in the original Transformer:





- a one-hot vector

Positional Embeddings

Augment word embedding with position embeddings, each dim is a sine/cosine wave of a different frequency. Closer points = higher dot products

Works essentially as well as just encoding position as Vaswani et al. (2017)

Sine embeddings in the original Transformer:





Positional Embeddings

Image Credit: Mehreen Saeed



- Absolute positional embeddings are added to input token embeddings
 - fixed encoding for each position (e.g., sine embeddings)
 - or learned encoding for each position

- Limitations:
 - can't generalize well to arbitrary long sequences

 - embedding for each position (e.g., 1, 2, 3, ..., 1000, ... 5000) – can't capture relative distance between two tokens



Relative positional embedding encodes the distance between tokens

0	1	2	3	4
-1	0	1	2	3
-2	-1	0	1	2
-3	-2	-1	0	1
-4	-3	-2	-1	0

Relative Positions Pattern in 5 token Attention matrix

Positional Embeddings

Shaw et al. (2018)

input

 $A = \exp$

- Relative positional embedding encodes the distance between tokens
- added directly to the self-attention matrix

0	1	2	3	4
-1	0	1	2	3
-2	-1	0	1	2
-3	-2	-1	0	1
-4	-3	-2	-1	0

Relative Positions Pattern in 5 token Attention matrix

Positional Embeddings



Shaw et al. (2018)

- <u>Relative positional embedding encodes the distance between tokens</u>
- added directly to the self-attention matrix
- Limitations: slow



Press et al. (2020)



- <u>Relative positional embedding encodes the distance between tokens</u>
- added directly to the self-attention matrix
- Limitations: slow (why?)



Press et al. (2020)



- <u>Relative positional embedding encodes the distance between tokens</u> added directly to the self-attention matrix
- Limitations: slow (why? changes KV values all the time, can't do KV caching)



Press et al. (2020)





KV Caching

- Accelerate LLM inference by reducing redundant computations
- Have the key and value projections cached





Image Credit: Cameron R. Wolfe



Rotary Positional Embeddings

Rotary Positional Embeddings (RoPE)



Figure 3: Evaluation of RoPE in language modeling pre-training. Left: training loss for BERT and RoFormer.





ROFORMER: ENHANCED TRANSFORMER WITH ROTARY POSITION EMBEDDING

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April 21, 2021

ABSTRACT

Position encoding in transformer architecture provides supervision for dependency modeling between elements at different positions in the sequence. We investigate various methods to encode positional information in transformer-based language models and propose a novel implementation named Rotary Position Embedding(RoPE). The proposed RoPE encodes absolute positional information with rotation matrix and naturally incorporates explicit relative position dependency in self-attention formulation. Notably, RoPE comes with valuable properties such as flexibility of being expand to any sequence lengths, decaying inter-token dependency with increasing relative distances, and capability of equipping the linear self-attention with relative position encoding. As a result, the enhanced transformer with rotary position embedding, or RoFormer, achieves superior performance in tasks with long texts. We release the theoretical analysis along with some preliminary experiment results on Chinese data. The undergoing experiment for English benchmark will soon be updated.

Apr 2021 20 [cs.CL] 864v1 5 04.0





Figure 1: Implementation of Rotary Position Embedding(RoPE).



Rotation instead of addition!





- Rotation instead of addition, such that embeddings are invariant to absolute position — inner products are invariant to arbitrary rotation captures both absolute position and relative distance!



Position independent embedding

Rotate by '2 positions'

Embedding "of course we know"



Embedding "we know that"

Rotate by '0 positions'



In 2D, a rotation matrix can be defined in the following form:

$$R_{\theta, m} = \begin{pmatrix} \cos m\theta & -\sin m\theta \\ \sin m\theta & \cos m\theta \end{pmatrix}$$

• The rotation increases with increasing θ and m.

Apply rotation after getting Q and K vectors (not V)







- In practice, rotate d dimensional embedding matrices.
- Idea: rotate different dimensions with different angles $\Theta = \{\theta_0, \theta_1, \theta_2, \theta_3, \dots, \theta_{d/2}\}$









A more computational efficient realization, taking advantage of the sparsity









Inner product decays as relative distance increases



Figure 2: Long-term decay of RoPE.



Optimization

AdamW

AdamW (Adam w/ weight decay) optimizer



Adam and AdamW with LR=0.001 and different weight decays 1000 1200 1400 1600 1800 800 Epochs

Loshchilov and Hutter (2017)

https://towardsdatascience.com/why-adamw-matters-736223f31b5d



AdamW (Adam w/ weight decay)

$$x_t \leftarrow x_{t-1} - \alpha \frac{\beta_1 m_{t-1} + (1 - \beta_1) (\nabla f_t + w)}{\sqrt{v_t} + \epsilon}$$

weight is regularized less when v is large (insert line 6,7,8 into line 12; ignore 9,10)

AdamW Optimizer



https://towardsdatascience.com/why-adamw-matters-736223f31b5d



AdamW (Adam w/ weight decay) optimizer

weight decay after (first and secor moments of) gradient calculation parameter-wise adaptive learning

AdamW Optimizer

	Algorithm 2 Adam with L ₂ regularization and
	Adam with weight decay (AdamW)
	 given α = 0.001, β₁ = 0.9, β₂ = 0.999, ε = 10⁻⁸, w ∈ ℝ initialize time step t ← 0, parameter vector x_{t=0} ∈ ℝⁿ, first moment vector m_{t=0} ← 0, second moment vector v_{t=0} ← 0 schedule multiplier η_{t=0} ∈ ℝ
	3: repeat
	4: $t \leftarrow t+1$
	5: $\nabla f_t(\mathbf{x}_{t-1}) \leftarrow \text{SelectBatch}(\mathbf{x}_{t-1}) \triangleright \text{select batch and}$ return the corresponding gradient
	6: $\boldsymbol{g}_t \leftarrow \nabla f_t(\boldsymbol{x}_{t-1}) + \boldsymbol{y}_{t-1}$
	7: $m_t \leftarrow \beta_1 m_{t-1} + (1 - \beta_1) g_t$ \triangleright here and below all
	operations are element-wise
-	8: $\boldsymbol{v}_t \leftarrow \beta_2 \boldsymbol{v}_{t-1} + (1 - \beta_2) \boldsymbol{g}_t^2$
nd	9: $\hat{m}_t \leftarrow m_t/(1 - \beta_1^t)$ $\triangleright \beta_1$ is taken to the power of t
	10: $v_t \leftarrow v_t/(1-\beta_2)$ $\triangleright \beta_2$ is taken to the power of t
for	11: $\eta_t \leftarrow \text{SetScheduleiviultipHer}(t) \triangleright can be fixed, decay, of also be used for warm restarts$
TOT	also be used for warm restarts 12
	12: $\mathbf{x}_t \leftarrow \mathbf{x}_{t-1} - \eta_t \left(\alpha \mathbf{m}_t / (\sqrt{\mathbf{v}_t + \epsilon}) + w \mathbf{x}_{t-1} \right)$
rate	13: until stopping criterion is met
jate	14: return optimized parameters x_t

Loshchilov and Hutter (2017)

https://towardsdatascience.com/why-adamw-matters-736223f31b5d





The non-google world uses BPE. Google uses the SentencePiece library, which (sometimes) refers to a non-BPE subword tokenizer

Model	Tokenizer
Original transformer	BPE
GPT 1/2/3	BPE
T5 / mT5 / T5v1.1	SentencePiece (Unigram)
Gopher/Chinchilla	SentencePiece (??)
PaLM	SentencePiece (??)
LLaMA	BPE

Monolingual models (30-50k vocab)

Model	Token count
Original transformer	37000
GPT	40257
GPT2/3	50257
T5/T5v1.1	32128
LLaMA	32000

Multilingual / Production Systems (100-250k vocab)

Model	Token count
mT5	250000
PaLM	256000
GPT4	100276
BLOOM	250680
DeepSeek	100000
Qwen 15B	152064
Yi	64000



Multi-whitespace tokenization

Different treatments for white space, and digits ... mainly for math/code

Tokenizer. We tokenize the data with the bytepair encoding (BPE) algorithm (Sennrich et al., 2015), using the implementation from Sentence-Piece (Kudo and Richardson, 2018). Notably, we split all numbers into individual digits, and fallback to bytes to decompose unknown UTF-8 characters.

Individual digit tokenization (LLaMA/DeepSeek)

Aa Name	# Year	Norm	Parallel Layer	Pre-norm
Original transformer	2017	LayerNorm	Serial	
GPT	2018	LayerNorm	Serial	
T5 (11B)	2019	RMSNorm	Serial	
GPT2	2019	LayerNorm	Serial	V
T5 (XXL 11B) v1.1	2020	RMSNorm	Serial	
mT5	2020	RMSNorm	Serial	
GPT3 (175B)	2020	LayerNorm	Serial	
GPTJ	2021	LayerNorm	Parallel	
LaMDA	2021			
Gopher (280B)	2021	RMSNorm	Serial	
GPT-NeoX	2022	LayerNorm	Parallel	
BLOOM (175B)	2022	LayerNorm	Serial	
OPT (175B)	2022	LayerNorm	Serial	
PaLM (540B)	2022	RMSNorm	Parallel	
Chinchilla	2022	RMSNorm	Serial	
Mistral (7B)	2023	RMSNorm	Serial	
LLaMA2 (70B)	2023	RMSNorm	Serial	
LLaMA (65B)	2023	RMSNorm	Serial	
Qwen (14B)	2024	RMSNorm	Serial	
DeepSeek (67B)	2024	RMSNorm	Serial	
Yi (34B)	2024	RMSNorm	Serial	

What are being used?

 Position embedding 	 Activations
Sine	ReLU
Absolute	GeLU
Relative	ReLU
Sine	GeLU
Relative	GeGLU
Relative	GeGLU
Sine	GeLU
RoPE	GeLU
Relative	GeGLU
Relative	ReLU
RoPE	GeLU
AliBi	GeLU
Absolute	ReLU
RoPE	SwiGLU
Relative	ReLU
RoPE	SwiGLU

Mostly follow previous successful choices.

Image Credit: Tatsu Hashimoto



- There are many architectural variations.
- Major differences? Position embeddings, activations, tokenization
- best practices.

Aa Name	🕤 Has pa	🔗 Link	# Year	⑦ Tokenizer type	# Vocab count	 Norm 	Parallel Layer	Pre-norm	Position embedding	 Activations 	☑ MoE	# MLP factor	# num_layers	# mode
Original transformer	Yes	arxiv.org/abs03762	2017	BPE	37000	LayerNorm	Serial		Sine	ReLU		4		6
GPT	Yes	cdn.openai.com/reser.pdf	2018	BPE	40257	LayerNorm	Serial		Absolute	GeLU		4		12
GPT2	Yes	cdn.openai.com/betrs.pdf	2019	BPE	50257	LayerNorm	Serial	\checkmark	Sine	GeLU		4		48
T5 (11B)	Yes	arxiv.org/abs10683	2019	SentencePiece	32128	RMSNorm	Serial		Relative	ReLU		64		24
GPT3 (175B)	Yes	arxiv.org/abs14165	2020	BPE	50257	LayerNorm	Serial	\checkmark	Sine	GeLU		4		96
mT5	Yes	arxiv.org/abs11934	2020	SentencePiece	250000	RMSNorm	Serial	\checkmark	Relative	GeGLU		2.5		24
T5 (XXL 11B) v1.1	Kind of	github.com/good#t511	2020	SentencePiece	32128	RMSNorm	Serial		Relative	GeGLU		2.5		24
Gopher (280B)	Yes	arxiv.org/abs11446	2021	SentencePiece	32000	RMSNorm	Serial		Relative	ReLU		4		80
Anthropic LM (not claude)	Yes	arxiv.org/abs00861	2021	BPE	65536							4		64
LaMDA	Yes	arxiv.org/abs08239	2021	BPE	32000				Relative	GeGLU		8		64
GPTJ	Kind of	huggingface.co/Elet-j-6b	2021	BPE	50257	LayerNorm	Parallel		RoPE	GeLU				28
Chinchilla	Yes	arxiv.org/abs15556	2022	SentencePiece	32000	RMSNorm	Serial		Relative	ReLU		4		80
PaLM (540B)	Yes	arxiv.org/abs02311	2022	SentencePiece	256000	RMSNorm	Parallel		RoPE	SwiGLU		4	1	118
OPT (175B)	Yes	arxiv.org/abs01068	2022	BPE	50272	LayerNorm	Serial		Absolute	ReLU		4		96
BLOOM (175B)	Yes	arxiv.org/abs05100	2022	BPE	250680	LayerNorm	Serial		AliBi	GeLU		4		70
GPT-NeoX	Yes	arxiv.org/pdf45.pdf	2022	BPE	50257	LayerNorm	Parallel		RoPE	GeLU		4		44
GPT4 OPEN	Ad	arxiv.org/abs08774	2023	BPE	100000									
LLaMA (65B)	Yes	arxiv.org/abs13971	2023	BPE	32000	RMSNorm	Serial		RoPE	SwiGLU		2.6875		80
LLaMA2 (70B)	Yes	arxiv.org/abs09288	2023	BPE	32000	RMSNorm	Serial		RoPE	SwiGLU		3.5		80
Mistral (7B)	Yes	arxiv.org/abs06825	2023	BPE	32000	RMSNorm	Serial		RoPE	SwiGLU		3.5		32

What are being used?

This is an evolving field; a lot of empirical analysis is going into identifying

Image Credit: Tatsu Hashimoto







Other Open-source Efforts

- Released by Stanford on March 13, 2023
- generated (Self-Instruct) using GPT-3.5 (text-davinci-003) for \$500.



Alpaca

Fine-tuned Meta's LLaMA-7B on 52k instruction-following demonstrated



Address the labor-intense process for creating human-written instructions



Figure 1: A high-level overview of SELF-INSTRUCT. The process starts with a small seed set of tasks (one instruction and one input-output instance for each task) as the task pool. Random tasks are sampled from the task pool, and used to prompt an off-the-shelf LM to generate both new instructions and corresponding instances, followed by filtering low-quality or similar generations, and then added back to the initial repository of tasks. The resulting data can be used for the instruction tuning of the language model itself later to follow instructions better. Tasks shown in the figure are generated by GPT3. See Table 10 for more creative examples.

Wang et al. (2022)





Using multiple prompting templates to (a) generate the instruction, (c) generating non-classification or classification instances

Come	up	with a series	of task	KS:		
Task	1:	{instruction	for exi	isting	task	1}
Task	2:	{instruction	for exi	isting	task	2}
Task	3:	{instruction	for exi	isting	task	3}
Task	4:	{instruction	for exi	isting	task	4}
Task	5:	{instruction	for exi	isting	task	5}
Task	6:	{instruction	for exi	isting	task	6}
Task	7:	{instruction	for exi	isting	task	7}
Task	8:	{instruction	for exi	isting	task	8}
Task	9:			•		

Table 6: Prompt used for generating new instructions. 8 existing instructions are randomly sampled from the task pool for in-context demonstration. The model is allowed to generate instructions for new tasks, until it stops its generation, reaches its length limit or generates "Task 16" tokens.

(b) classifying whether an instruction represents a classification task or not,

Wang et al. (2022)





```
Given the classification task definition and the class labels, generate an input that
corresponds to each of the class labels. If the task doesn't require input, just generate the
correct class label.
```

```
Task: Classify the sentiment of the sentence into positive, negative, or mixed.
Class label: mixed
Sentence: I enjoy the flavor of the restaurant but their service is too slow.
Class label: Positive
Sentence: I had a great day today. The weather was beautiful and I spent time with friends.
Class label: Negative
Sentence: I was really disappointed by the latest superhero movie. I would not recommend it.
...
Task: Tell me the first number of the given list.
Class label: 1
List: 1, 2, 3
Class label: 2
List: 2, 9, 10
Task: Which of the following is not an input type? (a) number (b) date (c) phone number (d)
email address (e) all of these are valid inputs.
Class label: (e)
      {instruction for the target task}
Task:
```

Table 9: Prompt used for the output-first approach of instance generation. The model is prompted to generate the class label first, and then generate the corresponding input. This prompt is used for generating the instances for classification tasks.





Figure 5: Performance of GPT3 model and its instruction-tuned variants, evaluated by human experts on our 252 user-oriented instructions (§5.4). Human evaluators are instructed to rate the models' responses into four levels. The results indicate that GPT3_{SELF-INST} outperforms all the other GPT3 variants trained on publicly available instruction datasets. Additionally, $GPT3_{SELF-INST}$ scores nearly as good as Instruct GPT_{001} (c.f., footnote 1).

Wang et al. (2022)


- Released by AI2 on Feb 28, 2024
- pre-training data (Dolma dataset) and intermediate checkpoints

Size	Layers	Hidden Size	Attention Heads	Tokens Trained
1 B	16	2048	16	2T
7B	32	4086	32	2.46T
65B*	80	8192	64	

Table 1: OLMo model sizes and the maximum number of tokens trained to. * At the time of writing our 65B model is still training.

OLMO

Open-source not only the training code and model weights, but the full

Groeneveld et al. (2024)



Chatbot Arena: Elo Rankings

- Accepted as one of the premiere rankings for LLMs
- Style control was introduced as it was believed that the "style" of responses had a big effect

Rank* (UB)	Rank (StyleCtrl)	Model	Arena Score	95% CI 🔺	Votes 🔺	Organization	Lic€
1	2	Grok-3-Preview-02-24	1407	+7/-7	7580	XAI	Prop
1	1	GPT-4.5-Preview	1404	+7/-9	6024	OpenAI	Prop
3	6	<u>Gemini-2.0-Flash-Thinking-Exp-</u> 01-21	1384	+5/-5	19837	Google	Prop
3	3	<u>Gemini-2.0-Pro-Exp-02-05</u>	1380	+4/-4	17695	Google	Prop
3	2	<u>ChatGPT-40-latest (2025-01-29)</u>	1375	+4/-5	19587	OpenAI	Prop
6	4	DeepSeek-R1	1361	+5/-6	10474	DeepSeek	MIT
6	10	<u>Gemini-2.0-Flash-001</u>	1355	+4/-5	15416	Google	Prop
6	3	01-2024-12-17	1353	+4/-4	22010	OpenAI	Prop
9	10	Gemma-3-27B-it	1339	+9/-11	3870	Google	Gemn
9	10	<u>Qwen2.5-Max</u>	1338	+5/-5	14258	Alibaba	Prop
9	7	<u>ol-preview</u>	1335	+4/-4	33195	OpenAI	Prop
9	10	o3-mini-high	1328	+6/-5	11409	OpenAI	Prop

leaderboard on Mar 12, 2025



Takeaways

New and actively developing situation. A lot is going on ...

